

Example 4b: Multivariate General Linear Models for Family (Triadic) Data
Part 1 in SAS MIXED and STATAMIXED; Part 2 also in Mplus and STATA SEM
(complete syntax and output available for SAS and STATA electronically)

These data were collected as part of a study of family dynamics conducted at Penn State University. The sample for this example includes 141 families with data from three family members: a mother, a father, and an adult child. The example outcome is a scale mean (range from 1–4) of attitudes about gender roles in marriage, in which higher scores indicate more conservative attitudes. The example predictors are the gender of the adult child (0=girl, 1=boy) and the years of education of each family member (centered such that 0=12 years). The observed outcome distributions of the showed some positive skew (with an observed floor effect for the adult children), but a conditional multivariate normal distribution appears to be adequate. This is evidenced in the final model by a Pearson $\chi^2/DF \approx .30$ for each outcome, as well as predicted outcomes that stayed within the outcome bounds without the use a link function to do so.

We will predict all family members' outcomes simultaneously two ways. In Part 1 we will estimate multivariate general linear models in SAS MIXED and STATA MIXED with conditional normal distributions using residual maximum likelihood (REML), and we will text fixed effects using Satterthwaite denominator degrees of freedom. Note that STATA provides incorrect AIC and BIC values using REML (it counts all parameters instead of variance parameters only), so those values are not referred to below. In Part 2, we will estimate the same models using path analysis in Mplus and STATA SEM, whose software restrictions mean we must switch to maximum likelihood and text fixed effects without denominator degrees of freedom. Finally, we will use an unstructured **R** matrix for all models (in which all variances and covariances are estimated separately without constraints).

Part 1: Multivariate General Linear Models via Univariate MIXED Software

Original data in wide format (was one row per family, person variables in separate columns):

	FamilyID: Family ID Number	KidBoy: Kid's Gender (0=girl, 1=boy)	KidEd12: Kid's Years of Education (0=12)	MomEd12: Mother's Years of Education (0=12)	DadEd12: Father's Years of Education (0=12)	KidMarital: Kid's Marital Gender Attitudes Mean (1-4)	MomMarital: Mom's Marital Gender Attitudes Mean (1-4)	DadMarital: Dad's Marital Gender Attitudes Mean (1-4)
1	3996	1	2	2	2	1	1.8333333333	1
2	4425	1	3	0	0	1	1.3333333333	2.5

New data in stacked format (one row per person per family) after transformation code below:

	FamilyID: Family ID Number	KidBoy: Kid's Gender (0=girl, 1=boy)	KidEd12: Kid's Years of Education (0=12)	MomEd12: Mother's Years of Education (0=12)	DadEd12: Father's Years of Education (0=12)	DV: 1K,2M,3D	kid: Is Adult Child (0=no, 1=yes)	mom: Is Mother (0=no, 1=yes)	dad: Is Father (0=no, 1=yes)	ed12: Person's Years of Education (0=12)	marital: Marital Gender Attitudes Mean (1-4)
1	3996	1	2	2	2	1.Kid	1	0	0	2	1
2	3996	1	2	2	2	2.Mom	0	1	0	2	1.8333333333
3	3996	1	2	2	2	3.Dad	0	0	1	2	1
4	4425	1	3	0	0	1.Kid	1	0	0	3	1
5	4425	1	3	0	0	2.Mom	0	1	0	0	1.3333333333
6	4425	1	3	0	0	3.Dad	0	0	1	0	2.5

STATA Syntax for Importing and Stacking Wide into Univariate (now one row per person per family):

```
// Define global variable for file location to be replaced in code below
global filesave "C:\Dropbox\20_PSQF7375_Generalized\PSQF7375_Generalized_Example4b"

// Import example 4b multivariate data
use "%filesave\Example4bWide.dta", clear

// Rename variables with numeric suffix to use with reshape (old)(new)
rename (kidmarital mommarital dadmarital) (marital1 marital2 marital3)

// Stack data: list multivariate variables first, i(higher index) j(repeated)
reshape long marital, i(familyid) j(DV)
```

```
// Create value labels and apply to dv
label define dvlabel 1 "1.Kid" 2 "2.Mom" 3 "3.Dad"
label values DV dvlabel

// Create dummy codes
gen kid=0
gen mom=0
gen dad=0
recode kid (0=1) if DV==1
recode mom (0=1) if DV==2
recode dad (0=1) if DV==3

// Label new variables
label variable DV      "DV: 1K,2M,3D"
label variable kid     "kid: Is Adult Child (0=no, 1=yes)"
label variable mom     "mom: Is Mother (0=no, 1=yes)"
label variable dad     "dad: Is Father (0=no, 1=yes)"
label variable marital "marital: Marital Gender Attitudes Mean (1-4)"
```

SAS Syntax for Importing and Stacking Wide into Univariate (now one row per person per family):

```
* Define global variable for file location to be replaced in code below;
%LET filesave= C:\Dropbox\20_PSQF7375_Generalized\PSQF7375_Generalized_Example4b;
* Location for SAS files for these models (uses macro variable filesave);
LIBNAME filesave "&filesave.";

* Import example 4b multivariate data into work library and stack it;
DATA work.Example4b; SET filesave.Example4bWide; * Adding own ed for demo purposes;
  DV="1.Kid"; kid=1; mom=0; dad=0; ed12=KidEd12; marital=KidMarital; OUTPUT;
  DV="2.Mom"; kid=0; mom=1; dad=0; ed12=MomEd12; marital=MomMarital; OUTPUT;
  DV="3.Dad"; kid=0; mom=0; dad=1; ed12=DadEd12; marital=DadMarital; OUTPUT;
LABEL DV=      "DV: 1K,2M,3D"
  kid=        "kid: Is Adult Child (0=no, 1=yes)"
  mom=        "mom: Is Mother (0=no, 1=yes)"
  dad=        "dad: Is Father (0=no, 1=yes)"
  ed12=       "ed12: Person's Years of Ed (0=12)"
  marital=    "marital: Marital Gender Attitudes Mean (1-4)";
DROP KidMarital MomMarital DadMarital; * Remove original outcomes; RUN;
```

Model 0: Empty Means, Unstructured Variance Model for Marital Conservative Gender Attitudes Two Ways for DV-Specific Intercept Version: $\widehat{Marital}_{fi} = \beta_{00}(Dad_{fi}) + \beta_{01}(Kid_{fi}) + \beta_{02}(Mom_{fi})$

```
display as result "STATA Empty Means, Unstructured Variance Model for Marital Attitudes"
display as result "STATA DV-Specific Intercept Version using Dummy Codes"
mixed marital c.kid c.mom c.dad, ///
  noconstant /// Remove fixed intercept
  || familyid: , noconstant variance reml residuals(unstructured,t(DV)) ///
  dfmethod(satterthwaite) dftable(pvalue)
estat wcorrelation, covariance, // R matrix
estat wcorrelation, // RCORR matrix
test (c.kid=c.mom)(c.kid=c.dad), small // DF=2 Diff in Intercept
lincom c.kid*-1 + c.mom*1, small // Kid vs. Mom: Intercept Diff
lincom c.kid*-1 + c.dad*1, small // Kid vs. Dad: Intercept Diff
lincom c.mom*-1 + c.dad*1, small // Mom vs. Dad: Intercept Diff

display as result "STATA DV-Specific Intercept Version using Categorical DV"
mixed marital ibn.DV, ///
  noconstant /// Remove fixed intercept and keep all DV levels
  || familyid: , noconstant variance reml residuals(unstructured,t(DV)) ///
  dfmethod(satterthwaite) dftable(pvalue)
estat wcorrelation, covariance, // R matrix
estat wcorrelation, // RCORR matrix
test (1.DV=2.DV)(1.DV=3.DV), small // DF=2 Diff in Intercept
lincom 1.DV*-1 + 2.DV*1, small // Kid vs. Mom: Intercept Diff
lincom 1.DV*-1 + 3.DV*1, small // Kid vs. Dad: Intercept Diff
lincom 2.DV*-1 + 3.DV*1, small // Mom vs. Dad: Intercept Diff
```

```
TITLE2 "SAS DV-Specific Intercept Version using Dummy Codes";
PROC MIXED DATA=work.Example4b NOCLPRINT COVTEST NAMELEN=100 METHOD=REML;
  CLASS FamilyID DV;
  MODEL marital = kid mom dad / NOINT SOLUTION DDFM=Satterthwaite;
  REPEATED DV / R RCORR TYPE=UN SUBJECT=FamilyID;
  CONTRAST "DF=2 Diff in Intercept?" kid -1 mom 1, kid -1 dad 1;
  ESTIMATE "Kid vs. Mom: Intercept Diff" kid -1 mom 1;
  ESTIMATE "Kid vs. Dad: Intercept Diff" kid -1 dad 1;
  ESTIMATE "Mom vs. Dad: Intercept Diff" mom -1 dad 1;
RUN; TITLE2;
```

```
TITLE2 "SAS DV-Specific Intercept Version using Categorical DV";
PROC MIXED DATA=work.Example4b NOCLPRINT COVTEST NAMELEN=100 METHOD=REML;
  CLASS FamilyID DV;
  MODEL marital = DV / NOINT SOLUTION DDFM=Satterthwaite;
  REPEATED DV / R RCORR TYPE=UN SUBJECT=FamilyID;
  CONTRAST "DF=2 Diff in Intercept?" DV -1 0 1, DV -1 1 0;
  ESTIMATE "Kid vs. Mom: Intercept Diff" DV -1 1 0;
  ESTIMATE "Kid vs. Dad: Intercept Diff" DV -1 0 1;
  ESTIMATE "Mom vs. Dad: Intercept Diff" DV 0 -1 1;
RUN; TITLE2;
```

Two Ways for General Intercept Version: $\widehat{Marital}_{fi} = \beta_{00} + \beta_{01}(Kid_{fi}) + \beta_{02}(Mom_{fi})$

```
display as result "STATA General Intercept Version using Dummy Codes"
mixed marital c.kid c.mom, ///
  || familyid: , noconstant variance reml residuals(unstructured,t(DV)) ///
  dfmethod(satterthwaite) dftable(pvalue)
  estat wcorrelation, covariance, // R matrix
  estat wcorrelation, // RCORR matrix
  test (c.kid=0)(c.mom=0), small // DF=2 Diff in Intercept
  lincom _cons*1 + c.kid*1, small // Kid Intercept
  lincom _cons*1 + c.mom*1, small // Mom Intercept
  lincom c.kid*-1 + c.mom*1, small // Kid vs. Mom: Intercept Diff
```

```
display as result "STATA General Intercept Version using Categorical DV"
mixed marital ib(last).DV, ///
  || familyid: , noconstant variance reml residuals(unstructured,t(DV)) ///
  dfmethod(satterthwaite) dftable(pvalue)
  estat wcorrelation, covariance, // R matrix
  estat wcorrelation, // RCORR matrix
  test (1.DV=2.DV)(1.DV=3.DV), small // DF=2 Diff in Intercept
  lincom _cons*1 + 1.DV*1, small // Kid Intercept
  lincom _cons*1 + 2.DV*1, small // Mom Intercept
  lincom 1.DV*-1 + 2.DV*1, small // Kid vs. Mom: Intercept Diff
```

```
TITLE2 "SAS General Intercept Version using Dummy Codes";
PROC MIXED DATA=work.Example4b NOCLPRINT COVTEST NAMELEN=100 METHOD=REML;
  CLASS FamilyID DV;
  MODEL marital = kid mom / SOLUTION DDFM=Satterthwaite;
  REPEATED DV / R RCORR TYPE=UN SUBJECT=FamilyID;
  CONTRAST "DF=2 Diff in Intercept?" kid 1, mom 1;
  ESTIMATE "Kid Intercept" intercept 1 kid 1 mom 0;
  ESTIMATE "Mom Intercept" intercept 1 kid 0 mom 1;
  ESTIMATE "Kid vs. Mom: Intercept Diff" kid -1 mom 1;
RUN; TITLE2;
```

```
TITLE2 "SAS General Intercept Version using Categorical DV";
PROC MIXED DATA=work.Example4b NOCLPRINT COVTEST NAMELEN=100 METHOD=REML;
  CLASS FamilyID DV;
  MODEL marital = DV / SOLUTION DDFM=Satterthwaite;
  REPEATED DV / R RCORR TYPE=UN SUBJECT=FamilyID;
  CONTRAST "DF=2 Diff in Intercept?" DV -1 0 1, DV -1 1 0;
  ESTIMATE "Kid Intercept" intercept 1 DV 1 0 0;
  ESTIMATE "Mom Intercept" intercept 1 DV 0 1 0;
  ESTIMATE "Kid vs. Mom: Intercept Diff" DV -1 1 0;
RUN; TITLE2; TITLE1;
```

SAS Output—Variance parameters, fit statistics, and contrasts are the same from all four Model 0 variants:

Iteration History				Criterion
Iteration	Evaluations	-2 Res Log Like		
0	1	729.02493914		0.00000000
1	2	706.95470511		

For your homework using SAS, get your -2LL value from this table to get two digits after the decimal.

Estimated R Matrix for FAMILYID 3996				Estimated R Correlation Matrix for FAMILYID 3996			
Row	Col1	Col2	Col3	Row	Col1	Col2	Col3
1	0.3312	0.04133	0.08240	1	1.0000	0.1264	0.2533
2	0.04133	0.3230	0.09371	2	0.1264	1.0000	0.2917
3	0.08240	0.09371	0.3196	3	0.2533	0.2917	1.0000

Covariance Parameter Estimates					
Cov Parm	Subject	Estimate	Standard Error	Z Value	Pr > Z
UN(1,1)	FamilyID	0.3312	0.03973	8.34	<.0001
UN(2,1)	FamilyID	0.04133	0.02796	1.48	0.1394
UN(2,2)	FamilyID	0.3230	0.03875	8.34	<.0001
UN(3,1)	FamilyID	0.08240	0.02847	2.89	0.0038
UN(3,2)	FamilyID	0.09371	0.02839	3.30	0.0010
UN(3,3)	FamilyID	0.3196	0.03834	8.34	<.0001

Fit Statistics	
-2 Res Log Likelihood	706.95
AIC (Smaller is Better)	719.0
AICC (Smaller is Better)	719.2
BIC (Smaller is Better)	736.6

Contrasts				
Label	Num DF	Den DF	F Value	Pr > F
DF=2 Diff in Intercept?	2	139	16.19	<.0001

Model-Estimated Fixed Effects from DV-Specific Intercept Version using Dummy Codes:

$$\text{Solution for Fixed Effects } \widehat{Marital}_{fi} = \beta_{00}(Dad_{fi}) + \beta_{01}(Kid_{fi}) + \beta_{02}(Mom_{fi})$$

Effect	Estimate	Standard Error	DF	t Value	Pr > t	
kid	1.6295	0.04864	139	33.50	<.0001	Kid intercept B01
mom	1.8998	0.04803	139	39.55	<.0001	Mom intercept B02
dad	1.9560	0.04778	139	40.94	<.0001	Dad intercept B00

Model-Estimated Fixed Effects from DV-Specific Intercept Version using Categorical DV:

$$\text{Solution for Fixed Effects } \widehat{Marital}_{fi} = \beta_{00}(Dad_{fi}) + \beta_{01}(Kid_{fi}) + \beta_{02}(Mom_{fi})$$

Effect	DV:	Estimate	Standard Error	DF	t Value	Pr > t	
DV	1.Kid	1.6295	0.04864	139	33.50	<.0001	Kid intercept B01
DV	2.Mom	1.8998	0.04803	139	39.55	<.0001	Mom intercept B02
DV	3.Dad	1.9560	0.04778	139	40.94	<.0001	Dad intercept B00

Requested Linear Combination Estimates from DV-Specific Intercept Version either way:

Estimates						
Label	Estimate	Standard Error	DF	t Value	Pr > t	
Kid vs. Mom: Intercept Diff	0.2702	0.06389	139	4.23	<.0001	B02 - B01
Kid vs. Dad: Intercept Diff	0.3264	0.05892	139	5.54	<.0001	B00 - B01
Mom vs. Dad: Intercept Diff	0.05619	0.05702	139	0.99	0.3261	B00 - B02

Model-Estimated Fixed Effects from General Intercept Version using Dummy Codes:

$$\text{Solution for Fixed Effects } \widehat{\text{Marital}}_{fi} = \beta_{00} + \beta_{01}(\text{Kid}_{fi}) + \beta_{02}(\text{Mom}_{fi})$$

Effect	Estimate	Standard Error	DF	t Value	Pr > t		
Intercept	1.9560	0.04778	139	40.94	<.0001	Dad intercept	B00
kid	-0.3264	0.05892	139	-5.54	<.0001	Kid intercept diff	B01
mom	-0.05619	0.05702	139	-0.99	0.3261	Mom intercept diff	B02

Model-Estimated Fixed Effects from General Intercept Version using Categorical DV:

$$\text{Solution for Fixed Effects } \widehat{\text{Marital}}_{fi} = \beta_{00} + \beta_{01}(\text{Kid}_{fi}) + \beta_{02}(\text{Mom}_{fi})$$

Effect	DV:	Estimate	Standard Error	DF	t Value	Pr > t		
Intercept	1K,2M,3D	1.9560	0.04778	139	40.94	<.0001	Dad intercept	B00
DV	1.Kid	-0.3264	0.05892	139	-5.54	<.0001	Kid intercept diff	B01
DV	2.Mom	-0.05619	0.05702	139	-0.99	0.3261	Mom intercept diff	B02
DV	3.Dad	0

Requested Linear Combination Estimates from General Intercept Version either way:

Label	Estimate	Standard Error	DF	t Value	Pr > t		
Kid Intercept	1.6295	0.04864	139	33.50	<.0001	B00 + B01	
Mom Intercept	1.8998	0.04803	139	39.55	<.0001	B00 + B02	
Kid vs. Mom: Intercept Diff	0.2702	0.06389	139	4.23	<.0001	B02 - B01	

To avoid confusion, we will proceed using the first of the four approaches: DV-specific intercepts implemented via dummy codes. This approach also aligns most directly with path model variants of these models (Part 2).

Model 1: DV-Specific Intercept Version adding Kid's Gender as Predictor for Each Attitude

$$\widehat{\text{Marital}}_{fi} = \beta_{00}(\text{Dad}_{fi}) + \beta_{01}(\text{Kid}_{fi}) + \beta_{02}(\text{Mom}_{fi}) + \beta_{10}(\text{Dad}_{fi})(\text{KidBoy}_f) + \beta_{11}(\text{Kid}_{fi})(\text{KidBoy}_f) + \beta_{12}(\text{Mom}_{fi})(\text{KidBoy}_f)$$

```
display as result "STATA DV-Specific Intercept Version -- Add Kid Gender"
mixed marital c.kid c.mom c.dad c.kid#c.kidboy c.mom#c.kidboy c.dad#c.kidboy, ///
    noconstant /// Remove fixed intercept
    || familyid: , noconstant variance reml residuals(unstructured,t(DV)) ///
    dfmethod(satterthwaite) dftable(pvalue)
estat wcorrelation, covariance, // R matrix
estat wcorrelation, // RCORR matrix
test (c.kid#c.kidboy=c.mom#c.kidboy) (c.kid#c.kidboy=c.dad#c.kidboy), small // DF=2 Diff in Kidboy Effect
lincom c.kid#c.kidboy*-1 + c.mom#c.kidboy*1, small // Kid vs. Mom: Kidboy Effect Diff
lincom c.kid#c.kidboy*-1 + c.dad#c.kidboy*1, small // Kid vs. Dad: Kidboy Effect Diff
lincom c.mom#c.kidboy*-1 + c.dad#c.kidboy*1, small // Mom vs. Dad: Kidboy Effect Diff
lincom 0.5*(c.mom#c.kidboy*1 + c.dad#c.kidboy*1), small // Parent: Kidboy Effect
lincom 0.5*(c.kid#c.kidboy*-2 + c.mom#c.kidboy*1 + c.dad#c.kidboy*1), small // M vs. D: Kidboy Effect Diff
```

```
TITLE "SAS DV-Specific Intercept Version -- Add Kid Gender";
PROC MIXED DATA=work.Example4b NOCLPRINT COVTEST NAMELEN=100 METHOD=REML;
CLASS FamilyID DV;
MODEL marital = kid mom dad kid*KidBoy mom*KidBoy dad*KidBoy
    / NOINT SOLUTION DDFM=Satterthwaite;
REPEATED DV / R RCORR TYPE=UN SUBJECT=FamilyID;
CONTRAST "DF=2 Diff in KidBoy Effect?" kid*KidBoy -1 Mom*KidBoy 1, kid*KidBoy -1 Dad*KidBoy 1;
ESTIMATE "Kid vs. Mom: KidBoy Effect Diff" kid*KidBoy -1 Mom*KidBoy 1;
ESTIMATE "Kid vs. Dad: KidBoy Effect Diff" kid*KidBoy -1 Dad*KidBoy 1;
ESTIMATE "Mom vs. Dad: KidBoy Effect Diff" Mom*KidBoy -1 Dad*KidBoy 1;
ESTIMATE "Parent KidBoy Effect" Mom*KidBoy 1 Dad*KidBoy 1 / DIVISOR=2;
ESTIMATE "Kid vs. Parents: KidBoy Effect Diff" Kid*KidBoy -2 Mom*KidBoy 1 Dad*KidBoy 1 / DIVISOR=2;
RUN; TITLE;
```

SAS Output for Model 1:

Estimated R Matrix for FAMILYID 3996

Row	Col1	Col2	Col3
1	0.3136	0.03725	0.07733
2	0.03725	0.3244	0.09315
3	0.07733	0.09315	0.3203

Estimated R Correlation Matrix for FAMILYID 3996

Row	Col1	Col2	Col3
1	1.0000	0.1168	0.2440
2	0.1168	1.0000	0.2890
3	0.2440	0.2890	1.0000

Fit Statistics

-2 Res Log Likelihood	707.01
AIC (Smaller is Better)	719.0
AICC (Smaller is Better)	719.2
BIC (Smaller is Better)	736.7

Contrasts

Label	Num DF	Den DF	F Value	Pr > F
DF=2 Diff in KidBoy Effect?	2	138	1.90	0.1529

Solution for Fixed Effects

Effect	Estimate	Standard Error	DF	t Value	Pr > t	
kid	1.4950	0.06554	138	22.81	<.0001	Kid intercept B01
mom	1.8703	0.06666	138	28.06	<.0001	Mom intercept B02
dad	1.9178	0.06624	138	28.95	<.0001	Dad intercept B00
kid*KidBoy	0.2811	0.09474	138	2.97	0.0035	girl vs boy for Kid B11
mom*KidBoy	0.06152	0.09636	138	0.64	0.5242	girl vs boy for Mom B12
dad*KidBoy	0.07970	0.09575	138	0.83	0.4066	girl vs boy for Dad B10

Estimates

Label	Estimate	Standard Error	DF	t Value	Pr > t	
Kid vs. Mom: Diff in KidBoy Effect	-0.2196	0.1270	138	-1.73	0.0860	B12 - B11
Kid vs. Dad: Diff in KidBoy Effect	-0.2014	0.1171	138	-1.72	0.0877	B10 - B11
Mom vs. Dad: Diff in KidBoy Effect	0.01818	0.1145	138	0.16	0.8741	B10 - B12
Parent KidBoy Effect	0.07061	0.07711	138	0.92	0.3614	.5*(B10+B12)
Kid vs. Parents: KidBoy Effect Diff	-0.2105	0.1079	138	-1.95	0.0531	.5*(B10+B12)-B11

It looks like we need to control for the effect of kid gender only for the kid. In the next model we'll test the effects of each person's education on their own attitude, followed by the incremental effect of dad's education on kid and mom attitudes after controlling for their own education.

Model 2: DV-Specific Intercept Version adding Own Education as Predictor of Own Attitude

$$\widehat{Marital}_{fi} = \beta_{00}(Dad_{fi}) + \beta_{01}(Kid_{fi}) + \beta_{02}(Mom_{fi}) + \beta_{11}(Kid_{fi})(KidBoy_f) \\ + \beta_{20}(Dad_{fi})(DadEd_f - 12) + \beta_{31}(Kid_{fi})(KidEd_f - 12) + \beta_{42}(Mom_{fi})(MomEd_f - 12)$$

```
display as result "STATA DV-Specific Intercept Version -- KidBoy on Kid Only, Add Own Education"
```

```
mixed marital c.kid c.mom c.dad c.kid#c.kidboy ///
      c.kid#c.kided12 c.mom#c.momed12 c.dad#c.daded12, ///
      noconstant /// Remove fixed intercept
      || familyid: , noconstant variance reml residuals(unstructured,t(DV)) ///
      dfmethod(satterthwaite) dftable(pvalue)
estat wcorrelation, covariance, // R matrix
estat wcorrelation, // RCORR matrix
```

```
TITLE "SAS DV-Specific Intercept Version -- KidBoy on Kid Only, Add Own Education";
```

```
PROC MIXED DATA=work.Example4b NOCLPRINT COVTEST NAMELEN=100 METHOD=REML;
```

```
CLASS FamilyID DV;
```

```
MODEL marital = kid mom dad kid*KidBoy kid*KidEd12 mom*MomEd12 dad*DadEd12
```

```
      / NOINT SOLUTION DDFM=Satterthwaite;
```

```
REPEATED DV / R RCORR TYPE=UN SUBJECT=FamilyID;
```

```
RUN; TITLE;
```

SAS Output for Model 2:

Estimated R Matrix for FAMILYID 3996

Row	Col1	Col2	Col3
1	0.3156	0.03837	0.07669
2	0.03837	0.3205	0.08441
3	0.07669	0.08441	0.2979

Estimated R Correlation Matrix for FAMILYID 3996

Row	Col1	Col2	Col3
1	1.0000	0.1207	0.2501
2	0.1207	1.0000	0.2732
3	0.2501	0.2732	1.0000

Fit Statistics

-2 Res Log Likelihood	708.64
AIC (Smaller is Better)	720.6
AICC (Smaller is Better)	720.8
BIC (Smaller is Better)	738.3

Solution for Fixed Effects

Effect	Estimate	Standard Error	DF	t Value	Pr > t	
kid	1.5117	0.09814	141	15.40	<.0001	Kid intercept B01
mom	1.9359	0.05976	142	32.39	<.0001	Mom intercept B02
dad	2.0700	0.05663	145	36.55	<.0001	Dad intercept B00
kid*KidBoy	0.2641	0.09204	137	2.87	0.0048	girl vs boy for Kid B11
kid*KidEd12	-0.00280	0.02344	138	-0.12	0.9052	Kid Ed for kid B31
mom*MomEd12	-0.01725	0.01711	142	-1.01	0.3150	Mom Ed for mom B42
dad*DadEd12	-0.05447	0.01570	143	-3.47	0.0007	Dad Ed for dad B20

Model 3: DV-Specific Intercept Version adding Dad Education as Predictor of Kid and Mom Attitudes

$$\widehat{Marital}_{fi} = \beta_{00}(Dad_{fi}) + \beta_{01}(Kid_{fi}) + \beta_{02}(Mom_{fi}) + \beta_{11}(Kid_{fi})(KidBoy_f) + \beta_{20}(Dad_{fi})(DadEd_f - 12) + \beta_{31}(Kid_{fi})(KidEd_f - 12) + \beta_{42}(Mom_{fi})(MomEd_f - 12) + \beta_{21}(Kid_{fi})(DadEd_f - 12) + \beta_{22}(Mom_{fi})(DadEd_f - 12)$$

```
display as result "STATA DV-Specific Intercept Version -- Add Dad Educ (Control for Own Educ)"
mixed marital c.kid c.mom c.dad c.kid#c.kidboy c.kid#c.kided12 c.mom#c.momed12 ///
      c.dad#c.daded12 c.kid#c.daded12 c.mom#c.daded12, ///
      noconstant /// Remove fixed intercept
      || familyid: , noconstant variance reml residuals(unstructured,t(DV)) ///
      dfmethod(satterthwaite) dftable(pvalue)
estat wcorrelation, covariance, // R matrix
estat wcorrelation, // RCORR matrix
lincom c.kid#c.daded12*-1 + c.mom#c.daded12*1, small // Kid vs. Mom: Dad Educ Effect Diff
lincom c.kid#c.daded12*-1 + c.dad#c.daded12*1, small // Kid vs. Dad: Dad Educ Effect Diff
lincom c.mom#c.daded12*-1 + c.dad#c.daded12*1, small // Mom vs. Dad: Dad Educ Effect Diff
```

```
TITLE "SAS DV-Specific Intercept Version -- Add Dad Educ (Controlling for Own Educ)";
PROC MIXED DATA=work.Example4b NOCLPRINT COVTEST NAMELEN=100 METHOD=REML;
CLASS FamilyID DV;
MODEL marital = kid mom dad kid*KidBoy Kid*KidEd12 Mom*MomEd12 Dad*DadEd12
      Kid*DadEd12 Mom*DadEd12 / NOINT SOLUTION DDFM=Satterthwaite;
REPEATED DV / R RCORR TYPE=UN SUBJECT=FamilyID;
ESTIMATE "Kid vs. Mom: Dad Educ Effect Diff" kid*DadEd12 -1 mom*DadEd12 1;
ESTIMATE "Kid vs. Dad: Dad Educ Effect Diff" kid*DadEd12 -1 dad*DadEd12 1;
ESTIMATE "Mom vs. Dad: Dad Educ Effect Diff" mom*DadEd12 -1 dad*DadEd12 1;
RUN; TITLE;
```

SAS Output for Model 3:

Estimated R Matrix for FAMILYID 3996

Row	Col1	Col2	Col3
1	0.3179	0.03856	0.07720
2	0.03856	0.3229	0.08514
3	0.07720	0.08514	0.2982

Estimated R Correlation Matrix for FAMILYID 3996

Row	Col1	Col2	Col3
1	1.0000	0.1204	0.2508
2	0.1204	1.0000	0.2744
3	0.2508	0.2744	1.0000

Fit Statistics

-2 Res Log Likelihood	720.78
AIC (Smaller is Better)	732.8
AICC (Smaller is Better)	733.0
BIC (Smaller is Better)	750.4

Solution for Fixed Effects

Effect	Estimate	Standard Error	DF	t Value	Pr > t	
kid	1.5123	0.1003	140	15.08	<.0001	Kid intercept B01
mom	1.9373	0.06305	138	30.73	<.0001	Mom intercept B02
dad	2.0707	0.05769	138	35.89	<.0001	Dad intercept B00
kid*KidBoy	0.2639	0.09258	136	2.85	0.0050	girl vs boy for Kid B11
kid*KidEd12	-0.00264	0.02458	136	-0.11	0.9147	Kid Ed for kid B31
mom*MomEd12	-0.01624	0.02068	137	-0.79	0.4338	Mom Ed for mom B42
dad*DadEd12	-0.05484	0.01654	138	-3.32	0.0012	Dad Ed for dad B20
kid*DadEd12	-0.00048	0.01791	138	-0.03	0.9787	Dad Ed for kid B21
mom*DadEd12	-0.00169	0.02069	141	-0.08	0.9349	Dad Ed for mom B22

Estimates

Label	Estimate	Standard Error	DF	t Value	Pr > t	
Kid vs. Mom: Dad Educ Effect Diff	-0.00121	0.02601	162	-0.05	0.9629	B22 - B21
Kid vs. Dad: Dad Educ Effect Diff	-0.05436	0.02127	143	-2.56	0.0117	B20 - B21
Mom vs. Dad: Dad Educ Effect Diff	-0.05314	0.02335	154	-2.28	0.0242	B20 - B22

Moral of the story? Multivariate models can be estimated in univariate software to capture the relationships between person-specific predictors and person-specific outcomes (such as in “actor–partner” models for dyadic data as well).

Example results section for Part 1 Models 0–3:

The extent to which gender and education predicted marital attitudes was examined in 141 families, in which responses were collected from adult children, their mothers, and their fathers, and in which higher outcomes indicated more conservative marital attitudes (i.e., gender-traditional attitudes measured as the mean across items on a scale of 1 to 4). Given that the outcomes were correlated within families, multivariate general linear models (i.e., with conditionally multivariate normal residuals) were used to predict all three outcomes for each family simultaneously. All models were estimated using residual maximum likelihood and Satterthwaite denominator degrees of freedom. All models allowed separate means and residual variances across the three outcomes for the three types of family members, as well as covariances among the residuals from the same family. ESTIMATE statements were used to estimate simple slopes and simple slope differences as linear combinations of the model fixed effects. Prior to adding predictors, an empty means model (i.e., an unconditional model with no predictors) revealed significant differences in marital attitudes across type of family member, $F(2,139) = 1.19, p < .001$. Although mean attitudes were similar across mothers and fathers (1.90 and 1.96, respectively, $p = .27$), the mean attitudes of children (1.63) were significantly less conservative on average than those of their parents ($p < .001$ for both comparisons).

To begin, we examined the extent to which the gender of the adult child (coded 0=woman, 1=man) who was surveyed was related to the marital attitudes of each type of family member. Although the attitudes of adult male children were significantly more conservative than those of adult female children (diff = 0.28, $p = .004$), there were no significant effects of the gender of the adult child for the marital attitudes of their mothers or fathers. Thus, we retained a predictor for the gender of the adult child only for the adult child’s outcome.

We then examined the extent to which the education (centered at 12 years) of each type of family member predicted their own attitudes, which was significant only for the father: for every additional year of father’s education, his own attitudes were expected to be less conservative by 0.05 ($p < .001$). Next, we examined whether father’s education incrementally predicted the marital attitudes of the mother or adult child after controlling for their own education, but neither effect was significant (and the effect of father’s education on his own attitudes was significantly larger).

But how do we know if Model 3 is sufficient?? Stay tuned for Part 2 using path analysis (and Model 4 using MIXED)!

estat residuals // Print how far off each predicted covariance is
 estat mindices, minchi2(3.84) showpclass(all) // Print voodoo to improve model fit at p<.05

Structural equation model Number of obs = 140
 Estimation method = mlmv
 Log likelihood = -1374.4822 → Does NOT match Mplus, but rest of the fit tests do match

UNSTANDARDIZED SOLUTION		OIM					IN MIXED	
		Coef.	Std. Err.	z	P> z	[95% Conf. Interval]		
Structural								
kidmarital <-								
	kidboy	.2638938	.0914365	2.89	0.004	.0846816	.4431059	B11
	kided12	-.002641	.0242338	-0.11	0.913	-.0501385	.0448565	B31
	daded12	-.0004795	.0176566	-0.03	0.978	-.0350857	.0341268	B21
	_cons	1.512271	.0989087	15.29	0.000	1.318414	1.706129	B01
mommarital <-								
	momed12	-.0162593	.0211854	-0.77	0.443	-.0577819	.0252634	B42
	daded12	-.0016793	.0206962	-0.08	0.935	-.0422431	.0388845	B22
	_cons	1.937305	.062596	30.95	0.000	1.814619	2.059991	B02
dadmarital <-								
	daded12	-.0548368	.016422	-3.34	0.001	-.0870233	-.0226502	B20
	_cons	2.070718	.0572756	36.15	0.000	1.95846	2.182976	B00

These unstandardized <- paths are the fixed slopes in MIXED.

Below are the residual variances and covariances from the R matrix in MIXED.							
var(e.kidmarital)	.3091381	.0369567			.2445646	.3907613	UN(1,1)
var(e.mommarital)	.3161529	.0379111			.2499347	.3999152	UN(2,2)
var(e.dadmarital)	.2938981	.0351275			.2325192	.3714795	UN(3,3)
cov(e.kidmarital,e.mommarital)	.0380059	.0266924	1.42	0.154	-.0143102	.090322	UN(2,1)
cov(e.kidmarital,e.dadmarital)	.0761007	.0263037	2.89	0.004	.0245463	.1276551	UN(3,1)
cov(e.mommarital,e.dadmarital)	.0839167	.0273732	3.07	0.002	.0302662	.1375671	UN(3,2)

LR test of model vs. saturated: chi2(6) = 10.93, Prob > chi2 = 0.0906

. lincom _b[mommarital:daded12] - _b[kidmarital:daded12] // Kid v. Mom: Dad Educ Effect Diff
 (1) - [kidmarital]daded12 + [mommarital]daded12 = 0

	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]		
(1)	-.0011998	.0258607	-0.05	0.963	-.0518858	.0494862	B22 - B21

. lincom _b[mommarital:daded12] - _b[kidmarital:daded12] // Kid v. Mom: Dad Educ Effect Diff
 (1) - [kidmarital]daded12 + [mommarital]daded12 = 0

	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]		
(1)	-.0011998	.0258607	-0.05	0.963	-.0518858	.0494862	B20 - B21

. lincom _b[mommarital:daded12] - _b[kidmarital:daded12] // Kid v. Mom: Dad Educ Effect Diff
 (1) - [kidmarital]daded12 + [mommarital]daded12 = 0

	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]		
(1)	-.0011998	.0258607	-0.05	0.963	-.0518858	.0494862	B20 - B22

. sem, coeflegend // Print parameter labels, too (to use in lincom)

	Coef.	Legend
Structural		
kidmarital <-		
	kidboy	_b[kidmarital:kidboy]
	kided12	_b[kidmarital:kided12]
	daded12	_b[kidmarital:daded12]
	_cons	_b[kidmarital:_cons]
mommarital <-		
	momed12	_b[mommarital:momed12]
	daded12	_b[mommarital:daded12]

This table from sem, coeflegend provides the parameter names for the LINCOS statements above.

```

      _cons |      1.937305      _b[mommarital:_cons]
-----+-----
dadmarital <-
      daded12 |     -.0548368      _b[dadmarital:daded12]
      _cons |      2.070718      _b[dadmarital:_cons]
-----+-----
      var(e.kidmarital) |     .3091381      _b[var(e.kidmarital):_cons]
      var(e.mommarital) |     .3161529      _b[var(e.mommarital):_cons]
      var(e.dadmarital) |     .2938981      _b[var(e.dadmarital):_cons]
-----+-----
cov(e.kidmarital,e.mommarital) |     .0380059      _b[cov(e.kidmarital,e.mommarital):_cons]
cov(e.kidmarital,e.dadmarital) |     .0761007      _b[cov(e.kidmarital,e.dadmarital):_cons]
cov(e.mommarital,e.dadmarital) |     .0839167      _b[cov(e.mommarital,e.dadmarital):_cons]
-----+-----
LR test of model vs. saturated: chi2(6) =      10.93, Prob > chi2 = 0.0906

```

. sem, standardized // Print fully standardized solution, too

Standardized Solution: All variables M=0, SD=1		OIM					
		Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
These standardized <- paths are standardized regression coefficients.							
Structural							
kidmarital <-							
	kidboy	.2306503	.0770785	2.99	0.003	.0795792	.3817214
	kided12	-.0090898	.0834042	-0.11	0.913	-.1725591	.1543794
	daded12	-.0023406	.0861915	-0.03	0.978	-.1712728	.1665916
	_cons	2.645964	.2466043	10.73	0.000	2.162628	3.129299
mommarital <-							
	momed12	-.0782303	.1019932	-0.77	0.443	-.2781333	.1216728
	daded12	-.0083038	.1023122	-0.08	0.935	-.208832	.1922244
	_cons	3.433518	.2280257	15.06	0.000	2.986595	3.88044
dadmarital <-							
	daded12	-.2716069	.0768234	-3.54	0.000	-.422178	-.1210357
	_cons	3.676054	.2200636	16.70	0.000	3.244738	4.107371
	var(e.kidmarital)	.9463698	.0355442			.8792068	1.018663
	var(e.mommarital)	.9930701	.0139521			.9660976	1.020796
	var(e.dadmarital)	.9262297	.0417315			.8479448	1.011742

These standardized covariances are residual correlations (in RCORR).

cov(e.kidmarital,e.mommarital)	.12157	.0835428	1.46	0.146	-.0421709	.2853109
cov(e.kidmarital,e.dadmarital)	.2524724	.0792209	3.19	0.001	.0972022	.4077426
cov(e.mommarital,e.dadmarital)	.2752969	.0801933	3.43	0.001	.1181209	.432473

. estat gof, stats(all) // Print fit statistics

Fit statistic	Value	Description (from STATA!)	Notes from Lesa:
Likelihood ratio			
chi2_ms(6)	10.929	model vs. saturated	This is -2ALL for our H0-H1
p > chi2	0.091		Test of exact fit: NS is good!
chi2_bs(15)	52.998	baseline vs. saturated	This is -2ALL for H0-H1 if
p > chi2	0.000		H0 had no paths at all
Population error			
RMSEA	0.077	Root mean squared error of approximation	Should be < .08 or so
90% CI, lower bound	0.000		
upper bound	0.148		
pclose	0.229	Probability RMSEA <= 0.05	Test of exact fit: NS is good!
Information criteria			
AIC	2778.964	Akaike's information criterion	Does not match Mplus
BIC	2823.089	Bayesian information criterion	Does not match Mplus
Baseline comparison			
CFI	0.870	Comparative fit index	Should be > .9 or so
TLI	0.676	Tucker-Lewis index	Should be > .9 or so
Size of residuals			
SRMR	0.039	Standardized root mean squared residual	Should be < .05 or so
CD	0.132	Coefficient of determination	Like an overall R2 across DVs


```

OUTPUT:      CINTERVAL;           ! Print confidence intervals;
            STDYX;                ! Print fully standardized solution, too;
            RESIDUAL;            ! Print how far off each predicted covariance is;
            MODINDICES (3.84);   ! Print voodoo to improve our model fit at p<.05;

```

```

MODEL: ! * --> Estimated parameter (all listed below for clarity);

```

```

! All residual variances estimated separately (by default);
KidMarit* MomMarit* DadMarit*;

```

```

! All possible pairwise residual covariances (not estimated by default);
KidMarit MomMarit DadMarit WITH KidMarit* MomMarit* DadMarit*;

```

```

! All intercepts estimated separately (by default);
[KidMarit* MomMarit* DadMarit*];

```

```

! Regressions: y outcomes ON x predictors (label to do math on later);
KidMarit ON KidBoy* KidEd12*;
MomMarit ON MomEd12*;
KidMarit MomMarit DadMarit ON DadEd12* (DadEd2K DadEd2M DadEd2D);

```

```

! Getting differences in effect of DadEd for each person;

```

```

MODEL CONSTRAINT:

```

```

NEW (KvMDadEd KvDDadEd MvDDadEd); ! List names of linear combinations here;

```

```

KvMDadEd = DadEd2M - DadEd2K;      ! Kid v. Mom: Dad Educ Effect Diff;

```

```

KvDDadEd = DadEd2D - DadEd2K;      ! Kid v. Dad: Dad Educ Effect Diff;

```

```

MvDDadEd = DadEd2D - DadEd2M;      ! Mom v. Dad: Dad Educ Effect Diff;

```

```

THE MODEL ESTIMATION TERMINATED NORMALLY
MODEL FIT INFORMATION

```

Model Fit Information	Value	Notes
Number of Free Parameters	15	Notes from Lesa:
Loglikelihood		
H0 Value	-337.106	For our model: Larger is better
H1 Value	-331.641	For model with all possible paths estimated
Information Criteria		
Akaike (AIC)	704.211	For our model: Smaller is better
Bayesian (BIC)	748.336	
Sample-Size Adjusted BIC	700.878	
(n* = (n + 2) / 24)		
Chi-Square Test of Model Fit		
Value	10.929	This is -2ΔLL for our H0-H1
Degrees of Freedom	6	This is counting the covariances between X's and Y's too
P-Value	0.0906	Test of exact fit: Nonsignificant is good!
RMSEA (Root Mean Square Error Of Approximation)		
Estimate	0.077	Should be < .08 or so
90 Percent C.I.	0.000 0.148	
Probability RMSEA <= .05	0.229	Test of close fit: Nonsignificant is good!
CFI/TLI		
CFI	0.870	Should be > .9 or so
TLI	0.676	Should be > .9 or so
Chi-Square Test of Model Fit for the Baseline Model		
Value	52.998	This is -2ΔLL for H0-H1 if H0 had no paths at all
Degrees of Freedom	15	
P-Value	0.0000	
SRMR (Standardized Root Mean Square Residual)		
Value	0.046	Should be < .05 or so

MODEL RESULTS (UNSTANDARDIZED SOLUTION; Mplus reorders them to list paths first)

	Estimate	S.E.	Est./S.E.	Two-Tailed P-Value	IN MIXED
KIDMARIT ON					
KIDBOY	0.264	0.091	2.886	0.004	B11
KIDED12	-0.003	0.024	-0.109	0.913	B31
DADED12	0.000	0.018	-0.027	0.978	B21
MOMMARIT ON					
MOMED12	-0.016	0.021	-0.767	0.443	B42
DADED12	-0.002	0.021	-0.081	0.935	B22
DADMARIT ON					
DADED12	-0.055	0.016	-3.339	0.001	B20
KIDMARIT WITH					
MOMMARIT	0.038	0.027	1.424	0.154	UN (2, 1)
DADMARIT	0.076	0.026	2.893	0.004	UN (3, 1)
MOMMARIT WITH					
DADMARIT	0.084	0.027	3.066	0.002	UN (3, 2)
Intercepts					
KIDMARIT	1.512	0.099	15.290	0.000	B01
MOMMARIT	1.937	0.063	30.949	0.000	B02
DADMARIT	2.071	0.057	36.154	0.000	B00
Residual Variances					
KIDMARIT	0.309	0.037	8.365	0.000	UN (1, 1)
MOMMARIT	0.316	0.038	8.339	0.000	UN (2, 2)
DADMARIT	0.294	0.035	8.367	0.000	UN (3, 3)
New/Additional Parameters (FROM MODEL CONSTRAINT, like ESTIMATE or LINCOM)					
KVMDADED	-0.001	0.026	-0.046	0.963	B22 - B21
KVDDADED	-0.054	0.021	-2.586	0.010	B20 - B21
MVDDADED	-0.053	0.023	-2.279	0.023	B20 - B22

These unstandardized ON paths are the fixed slopes from MIXED.

These unstandardized WITH covariances are residual covariances (in R).

Note that because we are using ML, the residual variances are smaller than in MIXED (that used REML instead to avoid this downward bias).

STANDARDIZED MODEL RESULTS - ALL VARIABLES HAVE MEAN=0, SD=1

STDYX Standardization

	Estimate	S.E.	Est./S.E.	Two-Tailed P-Value
KIDMARIT ON				
KIDBOY	0.231	0.078	2.950	0.003
KIDED12	-0.009	0.083	-0.109	0.913
DADED12	-0.002	0.086	-0.027	0.978
MOMMARIT ON				
MOMED12	-0.078	0.102	-0.766	0.444
DADED12	-0.008	0.102	-0.081	0.935
DADMARIT ON				
DADED12	-0.272	0.078	-3.470	0.001
KIDMARIT WITH				
MOMMARIT	0.122	0.084	1.455	0.146
DADMARIT	0.252	0.079	3.187	0.001
MOMMARIT WITH				
DADMARIT	0.275	0.080	3.433	0.001
Intercepts				
KIDMARIT	2.646	0.247	10.723	0.000
MOMMARIT	3.434	0.228	15.057	0.000
DADMARIT	3.676	0.221	16.659	0.000
Residual Variances				
KIDMARIT	0.946	0.036	26.246	0.000
MOMMARIT	0.993	0.014	71.055	0.000
DADMARIT	0.926	0.043	21.782	0.000
R-SQUARE				
Observed				
Variable	Estimate	S.E.	Est./S.E.	Two-Tailed P-Value
KIDMARIT	0.054	0.036	1.487	0.137
MOMMARIT	0.007	0.014	0.496	0.620
DADMARIT	0.074	0.043	1.735	0.083

These standardized ON paths are standardized regression coefficients.

These standardized WITH covariances are residual correlations (in RCORR).

ESTIMATED MODEL AND RESIDUALS (OBSERVED - ESTIMATED)

Residuals for Means	KIDMARIT	MOMMARIT	DADMARIT	KIDBOY	KIDED12	MOMED12	DADED12
	0.000	0.000	0.000	0.000	0.000	0.000	0.000

The means are recovered perfectly because each outcome has its own intercept (and predictor means are not part of the model).

Residuals for Covariances

	KIDMARIT	MOMMARIT	DADMARIT	KIDBOY	KIDED12	MOMED12	DADED12
KIDMARIT	0.002						
MOMMARIT	0.003	0.002					
DADMARIT	0.004	0.005	0.000				
KIDBOY	0.004	0.015	0.014	0.000			
KIDED12	-0.001	0.016	-0.008	0.000	0.000		
MOMED12	0.068	-0.072	-0.280	0.000	0.000	0.000	
DADED12	0.000	0.000	0.000	0.000	0.000	0.000	0.000

After shutting off the MODEL CONSTRAINT code and running it again, we get these “helpful” suggestions for how to improve model fit:

Minimum M.I. value for printing the modification index 3.840
M.I. E.P.C. Std E.P.C. StdYX E.P.C.

The bolded covariances indicate the biggest sources of misfit—it looks like momed12 needs to predict each outcome!

ON Statements

DADMARIT ON MOMMARIT 9.062 3.687 3.687 3.693 This is already in the model as a cov
DADMARIT ON MOMED12 9.061 -0.060 -0.060 -0.289 This is MomEd → DadMarit

WITH Statements

MOMED12 WITH DADMARIT 9.336 -0.294 -0.294 -0.200 This is MomEd ↔ DadMarit
DADED12 WITH DADMARIT 8.134 0.491 0.491 0.324 This is already in the model as a path

Model 4: DV-Specific Intercept Version adding Mom Education as Predictor of Each

$$\begin{aligned} \widehat{Marital}_{fi} = & \beta_{00}(Dad_{fi}) + \beta_{01}(Kid_{fi}) + \beta_{02}(Mom_{fi}) + \beta_{10}(Dad_{fi})(KidBoy_f) \\ & + \beta_{20}(Dad_{fi})(DadEd_f - 12) + \beta_{31}(Kid_{fi})(KidEd_f - 12) + \beta_{42}(Mom_{fi})(MomEd_f - 12) \\ & + \beta_{21}(Kid_{fi})(DadEd_f - 12) + \beta_{22}(Mom_{fi})(DadEd_f - 12) \\ & + \beta_{41}(Kid_{fi})(MomEd_f - 12) + \beta_{40}(Dad_{fi})(MomEd_f - 12) \end{aligned}$$

display as result "STATA DV-Specific Intercept Version -- Add Mom Educ (Control for Own Educ)"

```
mixed marital c.kid c.mom c.dad c.kid#c.kidboy c.kid#c.kided12 c.mom#c.momed12 ///
      c.dad#c.daded12 c.kid#c.daded12 c.mom#c.daded12 ///
      c.kid#c.momed12 c.dad#c.momed12, ///
noconstant /// Remove fixed intercept
|| familyid: , noconstant variance reml residuals(unstructured,t(DV)) ///
dfmethod(satterthwaite) dftable(pvalue)
estat wcorrelation, covariance, // R matrix
estat wcorrelation, // RCORR matrix
predict pred, xb // Add column pred of predicted outcomes to data
lincom c.kid#c.daded12*-1 + c.mom#c.daded12*1, small // Kid vs. Mom: Dad Educ Effect Diff
lincom c.kid#c.daded12*-1 + c.dad#c.daded12*1, small // Kid vs. Dad: Dad Educ Effect Diff
lincom c.mom#c.daded12*-1 + c.dad#c.daded12*1, small // Mom vs. Dad: Dad Educ Effect Diff
lincom c.kid#c.momed12*-1 + c.mom#c.momed12*1, small // Kid vs. Mom: Mom Educ Effect Diff
lincom c.kid#c.momed12*-1 + c.dad#c.momed12*1, small // Kid vs. Dad: Mom Educ Effect Diff
lincom c.mom#c.momed12*-1 + c.dad#c.momed12*1, small // Mom vs. Dad: Mom Educ Effect Diff

// Get correlation of actual and predicted outcomes to form R2
pwcrr marital pred if DV==1, sig
pwcrr marital pred if DV==2, sig
pwcrr marital pred if DV==2, sig
```

TITLE "SAS DV-Specific Intercept Version -- Add Mom Educ (Controlling for Own+Dad Educ)";

```
PROC MIXED DATA=work.Example4b NOCLPRINT COVTEST NAMELEN=100 METHOD=REML;
CLASS FamilyID DV;
MODEL marital = kid mom dad kid*KidBoy kid*KidEd12 mom*MomEd12 dad*DadEd12
      kid*DadEd12 mom*DadEd12 kid*MomEd12 dad*MomEd12
      / NOINT SOLUTION DDFM=Satterthwaite OUTPM=work.PredFinal;
REPEATED DV / R RCORR TYPE=UN SUBJECT=FamilyID;
ESTIMATE "Kid vs. Mom: Dad Educ Effect Diff" kid*DadEd12 -1 mom*DadEd12 1;
ESTIMATE "Kid vs. Dad: Dad Educ Effect Diff" kid*DadEd12 -1 dad*DadEd12 1;
ESTIMATE "Mom vs. Dad: Dad Educ Effect Diff" mom*DadEd12 -1 dad*DadEd12 1;
ESTIMATE "Kid vs. Mom: Mom Educ Effect Diff" kid*MomEd12 -1 mom*MomEd12 1;
ESTIMATE "Kid vs. Dad: Mom Educ Effect Diff" kid*MomEd12 -1 dad*MomEd12 1;
ESTIMATE "Mom vs. Dad: Mom Educ Effect Diff" mom*MomEd12 -1 dad*MomEd12 1;
```

RUN; TITLE;

**SAS Output for Model 4 (estimated with REML and using Satterthwaite denominator degrees of freedom):
Parameters would go in Table 1 for results**

Estimated R Matrix for FAMILYID 3996				Estimated R Correlation Matrix for FAMILYID 3996			
Row	Col1	Col2	Col3	Row	Col1	Col2	Col3
1	0.3193	0.04017	0.08212	1	1.0000	0.1253	0.2726
2	0.04017	0.3220	0.08159	2	0.1253	1.0000	0.2697
3	0.08212	0.08159	0.2842	3	0.2726	0.2697	1.0000

Fit Statistics

-2 Res Log Likelihood	722.90
AIC (Smaller is Better)	734.9
AICC (Smaller is Better)	735.1
BIC (Smaller is Better)	752.6

Solution for Fixed Effects

Effect	Estimate	Standard Error	DF	t Value	Pr > t	
kid	1.5221	0.1003	140	15.17	<.0001	Kid intercept B01
mom	1.9508	0.06321	137	30.86	<.0001	Mom intercept B02
dad	2.1232	0.05938	137	35.76	<.0001	Dad intercept B00
kid*KidBoy	0.2578	0.09226	135	2.79	0.0060	girl vs boy for Kid B11
kid*KidEd12	-0.01067	0.02508	135	-0.43	0.6711	Kid Ed for kid B31
mom*MomEd12	-0.03077	0.02151	137	-1.43	0.1547	Mom Ed for mom B42
dad*DadEd12	-0.02354	0.01966	137	-1.20	0.2333	Dad Ed for dad B20
kid*DadEd12	-0.00725	0.02109	136	-0.34	0.7315	Dad Ed for kid B21
mom*DadEd12	0.006376	0.02093	137	0.30	0.7611	Dad Ed for mom B22
kid*MomEd12	0.01513	0.02191	136	0.69	0.4910	Mom Ed for kid B41
dad*MomEd12	-0.05640	0.02020	137	-2.79	0.0060	Mom Ed for dad B40

Estimates

Label	Estimate	Standard Error	DF	t Value	Pr > t	
Kid vs. Mom: Dad Educ Effect Diff	0.01363	0.02781	138	0.49	0.6249	B22 - B21
Kid vs. Dad: Dad Educ Effect Diff	-0.01629	0.02465	137	-0.66	0.5099	B20 - B21
Mom vs. Dad: Dad Educ Effect Diff	-0.02991	0.02455	137	-1.22	0.2250	B20 - B22
Kid vs. Mom: Mom Educ Effect Diff	-0.04590	0.02876	140	-1.60	0.1127	B42 - B41
Kid vs. Dad: Mom Educ Effect Diff	-0.07153	0.02554	139	-2.80	0.0058	B40 - B41
Mom vs. Dad: Mom Educ Effect Diff	-0.02562	0.02523	137	-1.02	0.3115	B40 - B42

```
* Get R2 per outcome condition (prediction by old and yrs65);
PROC SORT DATA=work.PredFinal; BY DV FamilyID; RUN;
PROC CORR DATA=work.PredFinal; BY DV; VAR marital; WITH pred; RUN;
```

DV=1.Kid → R ² = .0627		DV=2.Mom → R ² = .0175		DV=2.Dad → R ² = .1236	
	marital		marital		marital
Pred	0.25049	Pred	0.13215	Pred	0.35159
Predicted Mean	0.0028	Predicted Mean	0.1196	Predicted Mean	<.0001

STATA Syntax for Model 4 as a Path Model (estimated with ML; no denominator DF):

```
display as result "STATA Model 4: Own + Dad & Mom Education a Predictor of Each Attitude"
sem
  (kidmarit mommarit dadmarit <- _cons)      ///
  (kidmarit <- kidboy kided12)              ///
  (kidmarit mommarit dadmarit <- daded12)    ///
  (kidmarit mommarit dadmarit <- momed12),   ///
  var(e.kidmarit e.mommarit e.dadmarit)     ///
  covariance(e.kidmarit*e.mommarit         ///
             e.mommarit*e.dadmarit        ///
             e.kidmarit*e.dadmarit)       ///
method(mlmv)                                ///
lincom _b[mommarital:daded12] - _b[kidmarital:daded12] // Kid v. Mom: Dad Educ Effect Diff
lincom _b[mommarital:daded12] - _b[kidmarital:daded12] // Kid v. Mom: Dad Educ Effect Diff
lincom _b[mommarital:daded12] - _b[kidmarital:daded12] // Kid v. Mom: Dad Educ Effect Diff
lincom _b[mommarital:momed12] - _b[kidmarital:momed12] // Kid v. Mom: Mom Educ Effect Diff
lincom _b[mommarital:momed12] - _b[kidmarital:momed12] // Kid v. Mom: Mom Educ Effect Diff
lincom _b[mommarital:momed12] - _b[kidmarital:momed12] // Kid v. Mom: Mom Educ Effect Diff
sem, coeflegend                              // Print parameter labels, too (to use in lincom)
sem, standardized                          // Print fully standardized solution, too
estat gof, stats(all)                      // Print fit statistics
estat eggof                                 // Print R2 per variable
estat residuals                             // Print how far off each predicted covariance is
estat mindices, minchi2(3.84) showpclass(all) // Print voodoo to improve model fit at p<.05
```

Mplus Syntax and Output for Model 4 as a Path Model (estimated with ML; no denominator DF):

!!

TITLE: Mplus Model 4: Own Education + Dad & Mom Education a Predictor of Each Attitude;

DATA, VARIABLE, ANALYSIS, and OUTPUT are all the same as Model 3.

MODEL: ! * --> Estimated parameter (all listed below for clarity);

! All residual variances estimated separately (by default);
KidMarit* MomMarit* DadMarit*;

! All possible pairwise residual covariances (not estimated by default);
KidMarit MomMarit DadMarit WITH KidMarit* MomMarit* DadMarit*;

! All intercepts estimated separately (by default);
[KidMarit* MomMarit* DadMarit*];

! Regressions: y outcomes ON x predictors (label to do math on later);
KidMarit ON KidBoy* KidEd12*;
KidMarit MomMarit DadMarit ON DadEd12* (DadEd2K DadEd2M DadEd2D);
KidMarit MomMarit DadMarit ON MomEd12* (MomEd2K MomEd2M MomEd2D); ! New effects here;

! Getting differences in effect of DadEd for each person;
MODEL CONSTRAINT: ! List names of linear combinations here;
NEW (KvMDadEd KvDDadEd MvDDadEd KvMMomEd KvDMomEd MvDMomEd);
KvMDadEd = DadEd2M - DadEd2K; ! Kid v. Mom: Dad Educ Effect Diff;
KvDDadEd = DadEd2D - DadEd2K; ! Kid v. Dad: Dad Educ Effect Diff;
MvDDadEd = DadEd2D - DadEd2M; ! Mom v. Dad: Dad Educ Effect Diff;
KvMMomEd = MomEd2M - MomEd2K; ! Kid v. Mom: Mom Educ Effect Diff;
KvDMomEd = MomEd2D - MomEd2K; ! Kid v. Dad: Mom Educ Effect Diff;
MvDMomEd = MomEd2D - MomEd2M; ! Mom v. Dad: Mom Educ Effect Diff;

THE MODEL ESTIMATION TERMINATED NORMALLY
MODEL FIT INFORMATION

Number of Free Parameters	17	Notes from Lesa:
Loglikelihood		
H0 Value	-332.158	For our model: Larger is better
H1 Value	-331.641	For model with all possible paths estimated
Information Criteria		
Akaike (AIC)	698.316	For our model: Smaller is better
Bayesian (BIC)	748.324	
Sample-Size Adjusted BIC	694.538	
(n* = (n + 2) / 24)		

Chi-Square Test of Model Fit				
Value	1.034			This is -2ΔLL for our H0-H1
Degrees of Freedom	4			This is counting the covariances between X's and Y's too
P-Value	0.9047			Test of exact fit: Nonsignificant is good!
RMSEA (Root Mean Square Error Of Approximation)				
Estimate	0.000			Should be < .08 or so
90 Percent C.I.	0.000	0.052		
Probability RMSEA <= .05	0.947			Test of close fit: Nonsignificant is good!
CFI/TLI				
CFI	1.000			Should be > .9 or so
TLI	1.000			Should be > .9 or so
Chi-Square Test of Model Fit for the Baseline Model				
Value	52.998			This is -2ΔLL for H0-H1 if H0 had no paths at all
Degrees of Freedom	15			
P-Value	0.0000			
SRMR (Standardized Root Mean Square Residual)				
Value	0.020			Should be < .05 or so

MODEL RESULTS

	Estimate	S.E.	Est./S.E.	Two-Tailed P-Value	IN MIXED
KIDMARIT ON					
KIDBOY	0.258	0.091	2.839	0.005	B11
KIDED12	-0.011	0.025	-0.433	0.665	B31
DADED12	-0.007	0.021	-0.350	0.726	B21
MOMED12	0.015	0.022	0.703	0.482	B41
MOMMARIT ON					
DADED12	0.006	0.021	0.308	0.758	B42
MOMED12	-0.031	0.021	-1.447	0.148	B22
DADMARIT ON					
DADED12	-0.024	0.019	-1.210	0.226	B20
MOMED12	-0.056	0.020	-2.822	0.005	B40
KIDMARIT WITH					
MOMMARIT	0.039	0.027	1.478	0.139	UN(2,1)
DADMARIT	0.080	0.026	3.124	0.002	UN(3,1)
MOMMARIT WITH					
DADMARIT	0.080	0.026	3.081	0.002	UN(3,2)
Intercepts					
KIDMARIT	1.522	0.099	15.418	0.000	B01
MOMMARIT	1.951	0.063	31.199	0.000	B02
DADMARIT	2.123	0.059	36.146	0.000	B00
Residual Variances					
KIDMARIT	0.308	0.037	8.363	0.000	UN(1,1)
MOMMARIT	0.315	0.038	8.367	0.000	UN(2,2)
DADMARIT	0.278	0.033	8.367	0.000	UN(3,3)
New/Additional Parameters (FROM MODEL CONSTRAINT, like ESTIMATE or LINCOM)					
KVMDADED	0.014	0.027	0.497	0.619	B22 - B21
KVDDADED	-0.016	0.024	-0.671	0.502	B20 - B21
MVDDADED	-0.030	0.024	-1.232	0.218	B20 - B22
KVMMOMED	-0.046	0.028	-1.620	0.105	B42 - B41
KVDMOMED	-0.072	0.025	-2.845	0.004	B40 - B41
MVDMOMED	-0.026	0.025	-1.027	0.304	B40 - B42

These unstandardized ON paths are the fixed slopes from MIXED.

These unstandardized WITH covariances are residual covariances (in R).

Note that because we are using ML, the residual variances are smaller than in MIXED (that used REML instead to avoid this downward bias).

STANDARDIZED MODEL RESULTS - ALL VARIABLES HAVE MEAN=0, SD=1
STDYX Standardization

	Estimate	S.E.	Est./S.E.	Two-Tailed P-Value
KIDMARIT ON				
KIDBOY	0.225	0.078	2.895	0.004
KIDED12	-0.037	0.085	-0.433	0.665
DADED12	-0.035	0.101	-0.350	0.726
MOMED12	0.072	0.102	0.704	0.481
MOMMARIT ON				
DADED12	0.031	0.102	0.308	0.758
MOMED12	-0.148	0.101	-1.457	0.145
DADMARIT ON				
DADED12	-0.117	0.096	-1.216	0.224
MOMED12	-0.272	0.094	-2.894	0.004
KIDMARIT WITH				
MOMMARIT	0.126	0.083	1.514	0.130
DADMARIT	0.274	0.078	3.503	0.000
MOMMARIT WITH				
DADMARIT	0.270	0.078	3.442	0.001
Intercepts				
KIDMARIT	2.664	0.245	10.891	0.000
MOMMARIT	3.445	0.224	15.373	0.000
DADMARIT	3.769	0.218	17.276	0.000

These standardized ON paths are standardized regression coefficients.

These standardized WITH covariances are residual correlations (in RCORR).

Residual Variances				
KIDMARIT	0.944	0.037	25.769	0.000
MOMMARIT	0.983	0.022	44.766	0.000
DADMARIT	0.876	0.052	16.826	0.000

R-SQUARE				
Observed	Estimate	S.E.	Est./S.E.	Two-Tailed P-Value
KIDMARIT	0.056	0.037	1.529	0.126
MOMMARIT	0.017	0.022	0.796	0.426
DADMARIT	0.124	0.052	2.373	0.018

Residuals for Covariances							
	KIDMARIT	MOMMARIT	DADMARIT	KIDBOY	KIDED12	MOMED12	DADED12
KIDMARIT	0.002						
MOMMARIT	0.004	0.000					
DADMARIT	0.003	0.000	0.000				
KIDBOY	0.005	0.015	0.015				
KIDED12	0.013	0.029	0.043	0.000	0.000		
MOMED12	0.000	0.000	0.000	0.000	0.000	0.000	
DADED12	0.000	0.000	0.000	0.000	0.000	0.000	0.000

Only the kid predictors on the mom and dad outcomes have leftover covariance, and no single added paths would help the model.

Example results section for Part 2 Models 3–4 (picking up from Part 1; using SAS and Mplus output):

Next, we examined whether father’s education incrementally predicted the marital attitudes of the mother or adult child after controlling for their own education, but neither effect was significant (and the effect of father’s education on his own attitudes was significantly larger). The effect of father’s education on his own attitudes remained significant, while the effect of education own their own attitudes for the adult child and mother remained nonsignificant). Finally, we examined the incremental effects of mother’s education on marital attitudes, and results from this final model are shown in Table 1. For every additional year of mother’s education, father’s attitudes were expected to be significantly less conservative by 0.01 ($p = .006$). The effect of mother’s education of adult child attitudes was nonsignificant and significantly smaller than its effect of father’s attitudes.

We re-estimated the final model as a path analysis in *Mplus* (using maximum likelihood) in order to obtain indices of absolute model fit. The model had excellent fit, $\chi^2(4) = 1.03, p = .90, RMSEA = .00 [CI = .00-.05], CFI = 1.00$, indicating that no further paths were needed. This final model is depicted in Figure 1 below.

Figure 1 (line types used to help visually distinguish the paths; standardized coefficients may also be added)

