Example 7b: Longitudinal Invariance CFA (using MLR) Example in Mplus v. 8.8 (N = 151; 6 indicators over 3 occasions) (Complete syntax and output files using Mplus and R lavaan are available electronically)

These (real) data measuring a latent trait of social functioning were collected at a Psychiatric Rehabilitation center, in which occasion 1 was admittance, and occasions 2 and 3 were collected at subsequent six-month intervals. There were six subscales that were completed by the hospital staff for each patient, including positively-oriented measures of Social Competence, Social Interest, and Personal Neatness, and negatively-oriented measures of Psychoticism, Motor Retardation, and Irritability. As shown below, the negatively-oriented subscales were reflected (*-1) prior to analysis. Initial models examined the fit of one-factor versus two-factor models given the two valences of the subscales, but the fit of the two-factor model was not a significant improvement, and thus a one-factor model with all six items was used here.

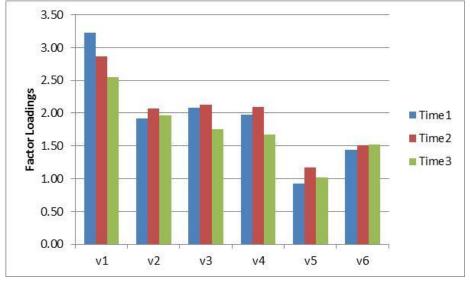
Mplus Code to Read in Data:

TITLE:

```
Longitudinal Invariance
DATA:
           FILE = Example7b.csv;
                                                 ! Don't need path if data in same folder
           FORMAT = free; TYPE = INDIVIDUAL;
                                                 ! Defaults
VARIABLE: NAMES = ID v1T1 v1T2 v1T3 v2T1 v2T2 v2T3
                                                                ! Every variable in data set
                       v3T1 v3T2 v3T3 v4T1 v4T2 v4T3
                       v5T1 v5T2 v5T3 v6T1 v6T2 v6T3;
           USEVARIABLES = v1T1 v1T2 v1T3 v2T1 v2T2 v2T3
                                                                ! Every variable in MODEL
                           v3T1 v3T2 v3T3 v4T1 v4T2 v4T3
                           v5T1 v5T2 v5T3 v6T1 v6T2 v6T3;
                                                                            Note: Mplus v. 7 and up offers a simplified set of syntax
                                                                            commands to assess invariance. However, I will teach you the
           MISSING = ALL (9999);
                                        ! Specify all missing values
                                                                            manual version so that you learn what you are doing first (then
                                        ! Specify person ID variable
           IDVARIABLE = ID;
                                                                            you can take their shortcuts on your own).
! Reverse-coding items so that higher = better
DEFINE:
            v4T1 = v4T1*(-1);
                                                                            Likewise, R lavaan also has shortcuts that I am not using via the
            v4T2 = v4T2*(-1);
                                                                            semTools package. However, because the modification indices I
            v4T3 = v4T3*(-1);
                                                                            am using to diagnose non-invariant parameters (as well as some
            v5T1 = v5T1*(-1);
                                                                            of the LRT results to compare models) do not match those of
            v5T2 = v5T2*(-1);
                                                                            Mplus, I am showing only Mplus results here.
            v5T3 = v5T3*(-1);
            v6T1 = v6T1*(-1);
            v6T2 = v6T2*(-1);
            v6T3 = v6T3*(-1);
ANALYSIS: ESTIMATOR = MLR;
                             ! For continuous items whose residuals may not be normal
          MODINDICES (3.84); ! For modification indices of p<.05 for DF=1
OUTPUT:
          STDYX RESIDUAL:
                              ! Fully standardized solution, local model fit
MODEL:
          ! Model syntax goes here, to be changed for each model
```

Model 1. Configural Longitudinal Invariance Model (all parameters estimated separately over time except for identification constraints)

```
MODEL:
!!!!! Model 1: Configural Longitudinal Invariance
! Factor loadings all freely estimated, not labeled
 Time1 BY v1T1* v2T1* v3T1* v4T1* v5T1* v6T1*;
 Time2 BY v1T2* v2T2* v3T2* v4T2* v5T2* v6T2*;
 Time3 BY v1T3* v2T3* v3T3* v4T3* v5T3* v6T3*;
! Item intercepts all freely estimated, not labeled
  [v1T1* v1T2* v1T3*]; [v2T1* v2T2* v2T3*];
  [v3T1* v3T2* v3T3*]; [v4T1* v4T2* v4T3*];
  [v5T1* v5T2* v5T3*]; [v6T1* v6T2* v6T3*];
! Residual variances all freely estimated, not labeled
 v1T1* v1T2* v1T3*; v2T1* v2T2* v2T3*;
 v3T1* v3T2* v3T3*; v4T1* v4T2* v4T3*;
 v5T1* v5T2* v5T3*; v6T1* v6T2* v6T3*;
! Factor variances all fixed=1 for identification
 Time1@1 Time2@1 Time3@1;
! Factor means all fixed=0 for identification
  [Time1@0 Time2@0 Time3@0];
! Factor covariances all freely estimated
 Time1 Time2 Time3 WITH Time1* Time2* Time3*;
! Residual covariances estimated for same item over time
 v1T1 v1T2 v1T3 WITH v1T1* v1T2* v1T3*;
 v2T1 v2T2 v2T3 WITH v2T1* v2T2* v2T3*;
 v3T1 v3T2 v3T3 WITH v3T1* v3T2* v3T3*;
 v4T1 v4T2 v4T3 WITH v4T1* v4T2* v4T3*;
 v5T1 v5T2 v5T3 WITH v5T1* v5T2* v5T3*;
 v6T1 v6T2 v6T3 WITH v6T1* v6T2* v6T3*;
```



e	estimated s	eparately over time except for i	dentification	constra
	MODEL FIT	INFORMATION		
	Number of	Free Parameters	75	
	Loglikelih	nood		
	- 5 -	HO Value	-4430.302	
		HO Scaling Correction Factor for MLR	1.4617	
		H1 Value	-4284.045	
		H1 Scaling Correction Factor for MLR	1.2029	
	Informatio	on Criteria		
		Akaike (AIC)	9010.604	
		Bayesian (BIC)	9236.900	
		Sample-Size Adjusted BIC $(n* = (n + 2) / 24)$	8999.533	
	Chi-Square	e Test of Model Fit		
	_	Value	283.247*	
		Degrees of Freedom	114	
		P-Value	0.0000	
		Scaling Correction Factor for MLR	1.0327	
	RMSEA (Roo	ot Mean Square Error Of Approxi	imation)	
		Estimate	0.099	
		90 Percent C.I.	0.085	0.114
		Probability RMSEA <= .05	0.000	
	CFI/TLI			
		CFI	0.903	
		TLI	0.870	
	Chi-Square	e Test of Model Fit for the Bas	seline Model	
		Value	1896.788	
		Degrees of Freedom	153	
		P-Value	0.0000	
	SRMR (Star	ndardized Root Mean Square Resi	idual)	
		Value	0.089	

Although the fit is not great, attempts to improve it logically were unsuccessful, so we proceed from here with this as the configural invariance model. The plot of factor loadings on the left foreshadows what will happen when testing metric invariance next...

UNSTANDARDIZED MODEL RESULTS - ALL MEASUREMENT PARAMETERS DIFFER OVER TIME (FACTOR MEANS=0 AND VARIANCES=1 FOR IDENTIFICATION)

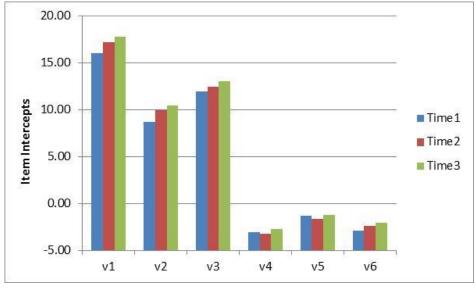
					Two-Tailed					Two-Tailed
		Estimate	S.E.	Est./S.E.	P-Value		Estimate	S.E.	Est./S.E.	P-Value
FACTOR LO	DADINGS	PER OCCASION								
	BY					Means (FACTO	R MEANS FIXED=0 FOR	IDENTIFI	CATION)	
V1T1		3.222	0.267	12.063	0.000	TIME1	0.000	0.000	999.000	999.000
V2T1		1.915	0.274	6.997	0.000	TIME2	0.000	0.000	999.000	999.000
V3T1		2.080	0.209	9.956	0.000	TIME3	0.000	0.000	999.000	999.000
V4T1		1.975	0.271	7.298	0.000					
V5T1		0.931	0.148	6.281	0.000	Intercepts	ARE EXPECTED OUTCOM	E WHEN FA	CTOR IS AT	0)
V6T1		1.441	0.119	12.101	0.000	V1T1	16.077	0.276	58.220	0.000
						V1T2	17.226	0.245	70.294	0.000
TIME2	BY					V1T3	17.756	0.220	80.620	0.000
V1T2		2.863	0.305	9.372	0.000	V2T1	8.672	0.298	29.132	0.000
V2T2		2.072	0.197	10.490	0.000	V2T2	9.981	0.263	37.921	0.000
V3T2		2.133	0.185	11.509	0.000	V2T3	10.442	0.281	37.204	0.000
V4T2		2.098	0.322	6.514	0.000	V3T1	11.970	0.225	53.108	0.000
V5T2		1.175	0.239	4.921	0.000	V3T2	12.467	0.218	57.264	0.000
V6T2		1.512	0.129	11.749	0.000	V3T3	13.029	0.213	61.157	0.000
						V4T1	-3.037	0.271	-11.216	0.000
TIME3	BY					V4T2	-3.211	0.260	-12.349	0.000
V1T3		2.550	0.288	8.865	0.000	V4T3	-2.738	0.249	-11.014	0.000
V2T3		1.961	0.230	8.539	0.000	V5T1	-1.283	0.138	-9.293	0.000
V3T3		1.751	0.210	8.323	0.000	V5T2	-1.664	0.200	-8.338	0.000
V4T3		1.678	0.260	6.448	0.000	V5T3	-1.247	0.166	-7.511	0.000
V5T3		1.021	0.170	6.012	0.000	V6T1	-2.871	0.164	-17.508	0.000
V6T3		1.523	0.159	9.574	0.000	V6T2	-2.413	0.158	-15.316	0.000
						V6T3	-2.075	0.152	-13.618	0.000
TIME1	•	ESTIMATED FACTO								
TIME2		0.786	0.042	18.827	0.000		riances (VARIANCE P			
TIME3	3	0.707	0.084	8.456	0.000	V1T1	0.241	0.395	0.610	0.542
_						V1T2	0.511	0.268	1.907	0.056
TIME2	WITH					V1T3	0.523	0.349	1.497	0.134
TIME3	3	0.671	0.089	7.532	0.000	V2T1	8.672	1.022	8.484	0.000
						V2T2	5.913	0.617	9.581	0.000
		ariances among	same item	n over time	****	V2T3	5.142	0.806	6.379	0.000
V1T1	WITH	0 014	0 050	0 055	0 202	V3T1	2.413	0.398	6.067	0.000
V1T2		-0.214	0.250	-0.855	0.393	V3T2	2.202	0.369	5.972	0.000
V1T3		-0.004	0.247	-0.016	0.987	V3T3	2.381	0.430 1.036	5.542 6.950	0.000
771 m O	T-7 T T T T T T T T T T T T T T T T T T					V4T1 V4T2	7.199 6.765	0.990	6.950	0.000
V1T2 V1T3	WITH	0 112	0 221	0.488	0.626	V4T2 V4T3	6.456	1.078	5.988	0.000
		0.113	0.231	0.488	0.626	V4T3 V5T1	6.456 1.824	0.446	5.988 4.093	0.000
						V5T1 V5T2	4.676	1.439	3.251	0.000
	· /E3/CE01	R VARIANCES FIX	ED-1 ECD	TDENUTETOS	ITOM\	V5T2 V5T3	4.676 2.944	0.752	3.251	0.001
variances TIME1	•	R VARIANCES FIX	0.000	999.000	999.000	V5T3 V6T1	1.694	0.752	6.974	0.000
TIME1		1.000	0.000	999.000	999.000	V6T2	1.103	0.243	6.643	0.000
TIME2		1.000	0.000	999.000	999.000	V6T2 V6T3	0.751	0.160	4.630	0.000
TIMES)	1.000	0.000	333.000	999.000	V 0.1.3	0./31	0.102	4.030	0.000

Model 2a. Metric Invariance Model (ALL loadings held equal across time – identified model using Time1 Factor Variance = 1)

```
MODEL:
!!!!! Model 2a: Metric Longitudinal Invariance
                                                             MODEL FIT INFORMATION
                                                             Number of Free Parameters
                                                                                                             65
! Factor loadings NOW CONSTRAINED EQUAL ACROSS TIME
 Time1 BY v1T1* v2T1* v3T1* v4T1* v5T1* v6T1* (L1-L6);
                                                             Loglikelihood
 Time2 BY v1T2* v2T2* v3T2* v4T2* v5T2* v6T2* (L1-L6);
                                                                       HO Value
                                                                                                      -4442.401
 Time3 BY v1T3* v2T3* v3T3* v4T3* v5T3* v6T3* (L1-16);
                                                                       HO Scaling Correction Factor
                                                                                                       1.4921
! Item intercepts all freely estimated, not labeled
                                                                       for MLR
  [v1T1* v1T2* v1T3*]; [v2T1* v2T2* v2T3*];
                                                                      H1 Value
                                                                                                     -4284.045
                                                                      H1 Scaling Correction Factor
  [v3T1* v3T2* v3T3*]; [v4T1* v4T2* v4T3*];
                                                                                                       1.2029
  [v5T1* v5T2* v5T3*]; [v6T1* v6T2* v6T3*];
                                                                        for MLR
! Residual variances all freely estimated, not labeled
 v1T1* v1T2* v1T3*; v2T1* v2T2* v2T3*;
                                                             Information Criteria
 v3T1* v3T2* v3T3*; v4T1* v4T2* v4T3*;
                                                                       Akaike (AIC)
                                                                                                       9014.803
 v5T1* v5T2* v5T3*; v6T1* v6T2* v6T3*;
                                                                      Bavesian (BIC)
                                                                                                       9210.926
! Factor variance AT TIME 1 fixed=1 for identification
                                                                      Sample-Size Adjusted BIC
                                                                                                       9005.208
                                                                        (n* = (n + 2) / 24)
 Time1@1 Time2* Time3*;
! Factor means all fixed=0 for identification
  [Time1@0 Time2@0 Time3@0];
                                                             Chi-Square Test of Model Fit
! Factor covariances all freely estimated
                                                                       Value
                                                                                                        301.234*
 Time1 Time2 Time3 WITH Time1* Time2* Time3*;
                                                                       Degrees of Freedom
                                                                                                            124
! Residual covariances estimated for same item over time
                                                                       P-Value
                                                                                                         0.0000
 v1T1 v1T2 v1T3 WITH v1T1* v1T2* v1T3*;
                                                                       Scaling Correction Factor
                                                                                                         1.0514
 v2T1 v2T2 v2T3 WITH v2T1* v2T2* v2T3*;
                                                                         for MLR
 v3T1 v3T2 v3T3 WITH v3T1* v3T2* v3T3*;
 v4T1 v4T2 v4T3 WITH v4T1* v4T2* v4T3*;
                                                             RMSEA (Root Mean Square Error Of Approximation)
 v5T1 v5T2 v5T3 WITH v5T1* v5T2* v5T3*;
                                                                       Estimate
                                                                                                          0.097
 v6T1 v6T2 v6T3 WITH v6T1* v6T2* v6T3*;
                                                                       90 Percent C.I.
                                                                                                         0.083 0.111
                                                                       Probability RMSEA <= .05
                                                                                                        0.000
Does the metric model (2a) fit worse than the configural model (1)?
                                                             CFI/TLI
Yes, -2\Delta LL(df=10) = 19.14, p = .04
                                                                                                          0.898
                                                                       CFI
                                                                       TLI
                                                                                                          0.875
                                                             SRMR (Standardized Root Mean Square Residual)
                                                                       Value
                                                                                                          0.094
                                                             MODEL MODIFICATION INDICES (relevant for testing invariance)
                                                             BY Statements
                                                                                    M.I.
                                                                                             E.P.C. Std E.P.C. StdYX E.P.C.
                                                             BY Statements
                                                             TIME1
                                                                      BY V1T1
                                                                                   10.377
                                                                                              0.182
                                                                                                         0.182
                                                                                                                      0.058
                                                             TIME1
                                                                      BY V5T1
                                                                                 6.062
                                                                                             -0.054
                                                                                                        -0.054
                                                                                                                     -0.033
                                                             TIME3 BY V6T3
                                                                                    7.603
                                                                                              0.201
                                                                                                         0.175
                                                                                                                      0.105
                                                             Modification indices suggest that freeing the loading for v1 at Time1
                                                             would help, and that matches our observations, so let's try that.
```

Model 2b. Partial Metric Invariance Model with loading for v1 at Time 1 free

```
MODEL:
! Model 2b: Partial Metric Invariance without v1T1
! Factor loadings NOW CONSTRAINED EQUAL ACROSS TIME EXCEPT v1T1
 Time1 BY v1T1* v2T1* v3T1* v4T1* v5T1* v6T1* (L1a L2-L6);
 Time2 BY v1T2* v2T2* v3T2* v4T2* v5T2* v6T2* (L1-L6);
 Time3 BY v1T3* v2T3* v3T3* v4T3* v5T3* v6T3* (L1-16);
! Item intercepts all freely estimated, not labeled
  [v1T1* v1T2* v1T3*]; [v2T1* v2T2* v2T3*];
  [v3T1* v3T2* v3T3*]; [v4T1* v4T2* v4T3*];
  [v5T1* v5T2* v5T3*]; [v6T1* v6T2* v6T3*];
! Residual variances all freely estimated, not labeled
 v1T1* v1T2* v1T3*; v2T1* v2T2* v2T3*;
 v3T1* v3T2* v3T3*; v4T1* v4T2* v4T3*;
 v5T1* v5T2* v5T3*; v6T1* v6T2* v6T3*;
! Factor variance AT TIME 1 fixed=1 for identification
 Time1@1 Time2* Time3*;
! Factor means all fixed=0 for identification
  [Time1@0 Time2@0 Time3@0];
! Factor covariances all freely estimated
 Time1 Time2 Time3 WITH Time1* Time2* Time3*;
! Residual covariances estimated for same item over time
 v1T1 v1T2 v1T3 WITH v1T1* v1T2* v1T3*;
 v2T1 v2T2 v2T3 WITH v2T1* v2T2* v2T3*;
 v3T1 v3T2 v3T3 WITH v3T1* v3T2* v3T3*;
 v4T1 v4T2 v4T3 WITH v4T1* v4T2* v4T3*;
 v5T1 v5T2 v5T3 WITH v5T1* v5T2* v5T3*;
 v6T1 v6T2 v6T3 WITH v6T1* v6T2* v6T3*;
```



	INFORMATION Free Parameters	66	
Loglikeli	hood H0 Value H0 Scaling Correction Factor for MLR H1 Value H1 Scaling Correction Factor for MLR	-4284.045	
Informati	on Criteria Akaike (AIC) Bayesian (BIC) Sample-Size Adjusted BIC (n* = (n + 2) / 24)	9003.337 9202.478 8993.595	
Chi-Squar	Value Degrees of Freedom P-Value Scaling Correction Factor for MLR	290.301* 123 0.0000 1.0446	
RMSEA (Ro	oot Mean Square Error Of Approx Estimate 90 Percent C.I. Probability RMSEA <= .05	ximation) 0.095 0.081 0.000	0.109
CFI/TLI	CFI TLI	0.904 0.881	
SRMR (Sta	ndardized Root Mean Square Re Value	sidual) 0.091	

Does the partial metric model (2b) fit *better* than the full metric model (2a)? Yes, $-2\Delta LL(df=1) = 7.16$, p < .01

Does the partial metric model (2b) fit worse than the configural model (1)? No, $-2\Delta LL(df=9) = 8.98$, p = .44

No large invariance-related modification indices were found, so we'll call it good! Onto the next model! The plot of intercepts on the left foreshadow what we will find with testing scalar invariance...

2b UNSTANDARDIZED PARTIAL METRIC MODEL RESULTS - ALL FACTOR LOADINGS ARE HELD EQUAL EXCEPT v1T1

2b UNSTANDARDIZE	D PARTIAL METRI	C MODEL F			ADINGS ARE HELD E	EQUAL EXCEPT v1T1	_		
			7	Two-Tailed				-	Two-Tailed
	Estimate	S.E.	Est./S.E.	P-Value		Estimate	S.E.	Est./S.E.	P-Value
TIME1 BY					Means (FACTOR M	EANS FIXED=0 FOR		,	
V1T1	3.233	0.261	12.362	0.000	TIME1	0.000	0.000	999.000	999.000
V2T1	1.950	0.201	9.706	0.000	TIME2	0.000	0.000	999.000	999.000
V3T1	1.967	0.198	9.910	0.000	TIME3	0.000	0.000	999.000	999.000
V4T1	1.899	0.224	8.481	0.000					
V5T1	0.968	0.137	7.055	0.000	Intercepts - S	CALED SO SHOULD	BE EQUAL	ACROSS TIME	
V6T1	1.476	0.131	11.247	0.000	V1T1	16.078	0.276	58.267	0.000
					V1T2	17.225	0.245	70.282	0.000
TIME2 BY					V1T3	17.756	0.222	80.036	0.000
V1T2	2.644	0.234	11.315	0.000	V2T1	8.672	0.298	29.071	0.000
V2T2	1.950	0.201	9.706	0.000	V2T2	9.980	0.264	37.872	0.000
V3T2	1.967	0.198	9.910	0.000	V2T3	10.434	0.280	37.245	0.000
V4T2	1.899	0.224	8.481	0.000	V3T1	11.978	0.225	53.192	0.000
V5T2	0.968	0.137	7.055	0.000	V3T2	12.468	0.217	57.325	0.000
V6T2	1.476	0.131	11.247	0.000	V3T3	13.041	0.212	61.441	0.000
					V4T1	-3.034	0.267	-11.343	0.000
TIME3 BY					V4T2	-3.210	0.260	-12.365	0.000
V1T3	2.644	0.234	11.315	0.000	V4T3	-2.720	0.254	-10.720	0.000
V2T3	1.950	0.201	9.706	0.000	V5T1	-1.288	0.137	-9.377	0.000
V3T3	1.967	0.198	9.910	0.000	V5T2	-1.663	0.199	-8.340	0.000
V4T3	1.899	0.224	8.481	0.000	V5T3	-1.246	0.169	-7.373	0.000
V5T3	0.968	0.137	7.055	0.000	V6T1	-2.871	0.164	-17.506	0.000
V6T3	1.476	0.131	11.247	0.000	V6T2	-2.414	0.158	-15.319	0.000
					V6T3	-2.087	0.154	-13.571	0.000
TIME1 WITH									
TIME2	0.847	0.078	10.837	0.000	Residual Varia	nces - ITEM VARIA		IS NOT THE	
TIME3	0.682	0.124	5.508	0.000	V1T1	0.170	0.374	0.454	0.650
					V1T2	0.548	0.265	2.070	0.038
TIME2 WITH					V1T3	0.509	0.314	1.618	0.106
TIME3	0.699	0.128	5.473	0.000	V2T1	8.702	1.026	8.483	0.000
					V2T2	5.895	0.605	9.746	0.000
*** Residual cov	ariances among	same iten	n over time '	***	V2T3	5.177	0.795	6.514	0.000
					V3T1	2.502	0.386	6.484	0.000
V1T1 WITH					V3T2	2.178	0.352	6.183	0.000
V1T2	-0.225	0.249	-0.904	0.366	V3T3	2.309	0.416	5.548	0.000
V1T3	-0.012	0.236	-0.049	0.961	V4T1	7.172	1.021	7.021	0.000
					V4T2	6.759	0.967	6.990	0.000
V1T2 WITH					V4T3	6.613	1.128	5.860	0.000
V1T3	0.132	0.230	0.573	0.566	V5T1	1.829	0.443	4.131	0.000
					V5T2	4.678	1.430	3.272	0.001
					V5T3	2.944	0.760	3.872	0.000
Variances (FACTO	R VARIANCE AT T	IME1=1 FC	OR IDENTIFICA	ATION)	V6T1	1.707	0.242	7.059	0.000
TIME1	1.000	0.000	999.000	999.000	V6T2	1.090	0.165	6.599	0.000
TIME2	1.162	0.185	6.270	0.000	V6T3	0.784	0.170	4.618	0.000
TIME3	0.941	0.157	5.999	0.000					

PSQF6249 Example 7b page 7
Model 3a. Scalar Invariance Model (all intercepts held equal across over time except v1T1); identified by Time1 mean=0

Model:	
! Model 3a: Full Scalar Invariance without v1T1	MODEL FIT INFORMATION
. House our rare boards invariance who house vire	Number of Free Parameters 57
! Factor loadings still constrained equal over time except v1T1	Trained of From Faramoods
Time1 BY v1T1* v2T1* v3T1* v4T1* v5T1* v6T1* (L1a L2-L6);	Loglikelihood
Time2 BY v1T2* v2T2* v3T2* v4T2* v5T2* v6T2* (L1-L6);	H0 Value -4461.842
Time3 BY v1T3* v2T3* v3T3* v4T3* v5T3* v6T3* (L1-16);	HO Scaling Correction Factor 1.5846
! Item intercepts NOW CONSTRAINED EQUAL ACROSS TIME EXCEPT v1T1	for MLR
[v1T1*]; [v1T2* v1T3*] (I1); ! 3a: I1 applies only to 2 and 3	H1 Value -4284.045
[v2T1* v2T2* v2T3*] (I1);	H1 Scaling Correction Factor 1.2029
[v3T1* v3T2* v3T3*] (I2);	for MLR
[v4T1* v4T2* v4T3*] (I4);	TOT MER
	Tr.farmatica Cuitania
[v5T1* v5T2* v5T3*] (I5);	Information Criteria
[v6T1* v6T2* v6T3*] (I6);	Akaike (AIC) 9037.685
! Residual variances all freely estimated, not labeled	Bayesian (BIC) 9209.670
v1T1* v1T2* v1T3*; v2T1* v2T2* v2T3*;	Sample-Size Adjusted BIC 9029.271
v3T1* v3T2* v3T3*; v4T1* v4T2* v4T3*;	$(n^* = (n + 2) / 24)$
v5T1* v5T2* v5T3*; v6T1* v6T2* v6T3*;	
! Factor variance AT TIME 1 fixed=1 for identification	Chi-Square Test of Model Fit
Time1@1 Time2* Time3*;	Value 342.530*
! Factor mean AT TIME 1 fixed=0 for identification	Degrees of Freedom 132
[Time100 Time2* Time3*];	P-Value 0.0000
! Factor covariances all freely estimated	Scaling Correction Factor 1.0381
Time1 Time2 Time3 WITH Time1* Time2* Time3*;	for MLR
! Residual covariances estimated for same item over time	
v1T1 v1T2 v1T3 WITH v1T1* v1T2* v1T3*;	RMSEA (Root Mean Square Error Of Approximation)
v2T1 v2T2 v2T3 WITH v2T1* v2T2* v2T3*;	Estimate 0.103
v3T1 v3T2 v3T3 WITH v3T1* v3T2* v3T3*;	90 Percent C.I. 0.089 0.116
v4T1 v4T2 v4T3 WITH v4T1* v4T2* v4T3*;	Probability RMSEA <= .05 0.000
v5T1 v5T2 v5T3 WITH v5T1* v5T2* v5T3*;	
v6T1 v6T2 v6T3 WITH v6T1* v6T2* v6T3*;	CFI/TLI
	CFI 0.879
Does the full scalar model (3a) fit worse than the partial metric model	TLI 0.860
(2b)? Yes, $-2\Delta LL(df=9) = 55.13$, $p < .01$	
(20) : 163, $2\Delta LL(di-3) = 33.13$, $p < .01$	SRMR (Standardized Root Mean Square Residual)
	Value 0.093
Modification indices suggest that freeing these intercepts would help, so	MODEL MODIFICATION INDICES (relevant for invariance testing)
let's try v5T1 first (biggest χ^2 change suggested).	Means/Intercepts/Thresholds
let a try vor i lilat (biggeat X. change auggeateu).	
	M.I. E.P.C. Std E.P.C. StdYX E.P.C.
	[V2T1] 14.761 -0.696 -0.696 -0.189
	[V2T2] 5.578 0.307 0.307 0.094
	[V4T1] 10.400 0.366 0.366 0.113
	[V4T2] 5.167 -0.271 -0.271 -0.084
	[V5T1] 20.890 -0.027 -0.027 -0.017
	[V5T2] 14.191 -0.596 -0.596 -0.241
	1 11.131 0.030 0.030 0.241

Model 3b. Partial Scalar Invariance Model (all intercepts held equal across over time except v1T1 and v5T1)

Model 3b. Partial Scalar Invariance Model (all Intercepts neid equal a	oross over time except viri and vori
MODEL: ! Model 3b: Partial Scalar Invariance, no v1T1 v5T1	
	MODEL FIT INFORMATION
! Factor loadings still constrained equal over time except v1T1	Number of Free Parameters 58
Time1 BY v1T1* v2T1* v3T1* v4T1* v5T1* v6T1* (L1a L2-L6);	
Time2 BY v1T2* v2T2* v3T2* v4T2* v5T2* v6T2* (L1-L6);	Loglikelihood
Time3 BY v1T3* v2T3* v3T3* v4T3* v5T3* v6T3* (L1-16);	HO Value -4450.001
! Item intercepts NOW CONSTRAINED EQUAL ACROSS TIME	HO Scaling Correction Factor 1.5626
! no v1T1 v5T1	for MLR
[v1T1*]; [v1T2* v1T3*] (I1); ! 3a: I1 applies only to 2 and 3	H1 Value -4284.045
[v2T1* v2T2* v2T3*] (I2);	H1 Scaling Correction Factor 1.2029
[v3T1* v3T2* v3T3*] (I3);	for MLR
[v4T1* v4T2* v4T3*] (I4);	
<pre>[v5T1*]; [v5T2* v5T3*] (I5); ! 3b: I5 applies only to 2 and 3</pre>	Information Criteria
[v6T1* v6T2* v6T3*] (I6);	Akaike (AIC) 9016.001
! Residual variances all freely estimated, not labeled	Bayesian (BIC) 9191.004
v1T1* v1T2* v1T3*; v2T1* v2T2* v2T3*;	Sample-Size Adjusted BIC 9007.440
v3T1* v3T2* v3T3*; v4T1* v4T2* v4T3*;	$(n^* = (n + 2) / 24)$
v5T1* v5T2* v5T3*; v6T1* v6T2* v6T3*;	
! Factor variance AT TIME 1 fixed=1 for identification	Chi-Square Test of Model Fit
Time1@1 Time2* Time3*;	Value 318.018*
· '	
! Factor mean AT TIME 1 fixed=0 for identification	Degrees of Freedom 131
[Time1@0 Time2* Time3*];	P-Value 0.0000
! Factor covariances all freely estimated	Scaling Correction Factor 1.0437
Time1 Time2 Time3 WITH Time1* Time2* Time3*;	for MLR
! Residual covariances estimated for same item over time	
v1T1 v1T2 v1T3 WITH v1T1* v1T2* v1T3*;	RMSEA (Root Mean Square Error Of Approximation)
v2T1 v2T2 v2T3 WITH v2T1* v2T2* v2T3*;	Estimate 0.097
v3T1 v3T2 v3T3 WITH v3T1* v3T2* v3T3*;	90 Percent C.I. 0.084 0.111
v4T1 v4T2 v4T3 WITH v4T1* v4T2* v4T3*;	Probability RMSEA <= .05 0.000
v5T1 v5T2 v5T3 WITH v5T1* v5T2* v5T3*;	-
v6T1 v6T2 v6T3 WITH v6T1* v6T2* v6T3*;	CFI/TLI
1000 1000 1000 1000 1000 ,	CFI 0.893
	TLI 0.875
Does the partial scalar model (3b) fit <i>better</i> than the full scalar model (3a)?	0.675
Yes, $-2\Delta LL(df=1) = 15.16$, $p < .01$	CDMD (Chandandinal Deat Man Course Decidual)
	SRMR (Standardized Root Mean Square Residual)
Does the partial scalar model (3b) fit worse than the partial metric model	Value 0.086
(2b)? Yes, $-2\Delta LL(df=8) = 27.84$, $p < .01$	
(2b): 165, $-2\Delta LL(ui-0) = 27.04$, $p < .01$	MODEL MODIFICATION INDICES (relevant for invariance testing)
	Means/Intercepts/Thresholds
	M.I. E.P.C. Std E.P.C. StdYX
Modification indices still suggest that freeing these intercepts would help,	E.P.C.
	[V2T1] 11.529 -0.599 -0.599 -0.164
so let's try v4T1 next (biggest χ^2 change suggested).	[V2T2] 4.390 0.278 0.278 0.085
	[V4T1] 13.795 0.425 0.425 0.132
	[V4T2] 6.398 -0.306 -0.306 -0.096
	1 0.350 0.300 0.300 0.050

Model 3c. Partial Scalar Invariance Model (all intercepts held equal across over time except v1T1, v5T1, v4T1)

```
MODEL: ! Model 3c: Partial Scalar Invariance, no v1T1 v5T1 v4T1
                                                                     MODEL FIT INFORMATION
                                                                    Number of Free Parameters
! Factor loadings still constrained equal over time except v1T1
                                                                                                                      59
 Time1 BY v1T1* v2T1* v3T1* v4T1* v5T1* v6T1* (L1a L2-L6);
 Time2 BY v1T2* v2T2* v3T2* v4T2* v5T2* v6T2* (L1-L6);
                                                                     Loglikelihood
 Time3 BY v1T3* v2T3* v3T3* v4T3* v5T3* v6T3* (L1-16);
                                                                               HO Value
                                                                                                              -4442,214
! Item intercepts NOW CONSTRAINED EQUAL ACROSS TIME
                                                                               HO Scaling Correction Factor
                                                                                                                 1.5647
! no v1T1 v5T1 v4T1
                                                                               for MLR
  [v1T1*]; [v1T2* v1T3*] (I1); ! 3a: I1 applies only to 2 and 3
                                                                               H1 Value
                                                                                                              -4284.045
                                                                              H1 Scaling Correction Factor
           v2T2* v2T3*] (I2);
                                                                                                               1.2029
  [v3T1*
            v3T2* v3T3*] (I3);
                                                                                 for MLR
  [v4T1*]; [v4T2* v4T3*] (I4); ! 3c: I4 applies only to 2 and 3
  [v5T1*]; [v5T2* v5T3*] (I5); ! 3b: I5 applies only to 2 and 3
                                                                    Information Criteria
  [v6T1*
            v6T2* v6T3*] (I6);
                                                                               Akaike (AIC)
                                                                                                               9002.427
! Residual variances all freely estimated, not labeled
                                                                               Bavesian (BIC)
                                                                                                               9180.447
 v1T1* v1T2* v1T3*; v2T1* v2T2* v2T3*;
                                                                               Sample-Size Adjusted BIC
                                                                                                               8993.718
                                                                                (n* = (n + 2) / 24)
 v3T1* v3T2* v3T3*; v4T1* v4T2* v4T3*;
 v5T1* v5T2* v5T3*; v6T1* v6T2* v6T3*;
! Factor variance AT TIME 1 fixed=1 for identification
                                                                    Chi-Square Test of Model Fit
 Time1@1 Time2* Time3*;
                                                                               Value
                                                                                                                304.536*
! Factor mean AT TIME 1 fixed=0 for identification
                                                                               Degrees of Freedom
                                                                                                                    130
  [Time1@0 Time2* Time3*];
                                                                               P-Value
                                                                                                                 0.0000
! Factor covariances all freely estimated
                                                                               Scaling Correction Factor
                                                                                                                 1.0387
 Time1 Time2 Time3 WITH Time1* Time2* Time3*;
                                                                                 for MLR
! Residual covariances estimated for same item over time
 v1T1 v1T2 v1T3 WITH v1T1* v1T2* v1T3*;
                                                                    RMSEA (Root Mean Square Error Of Approximation)
 v2T1 v2T2 v2T3 WITH v2T1* v2T2* v2T3*;
                                                                               Estimate
                                                                                                                  0.094
 v3T1 v3T2 v3T3 WITH v3T1* v3T2* v3T3*;
                                                                               90 Percent C.I.
                                                                                                                  0.081 0.108
 v4T1 v4T2 v4T3 WITH v4T1* v4T2* v4T3*;
                                                                               Probability RMSEA <= .05
                                                                                                                  0.000
 v5T1 v5T2 v5T3 WITH v5T1* v5T2* v5T3*;
 v6T1 v6T2 v6T3 WITH v6T1* v6T2* v6T3*;
                                                                    CFI/TLI
                                                                               CFI
                                                                                                                  0.900
                                                                               TLI
                                                                                                                  0.882
Does the partial scalar model (3c) fit better than the partial scalar model
(3b)? Yes, -2\Delta LL(df=1) = 9.24, p < .01
                                                                     SRMR (Standardized Root Mean Square Residual)
                                                                               Value
                                                                                                                  0.092
Does the partial scalar model (3c) fit worse than the partial metric model
(2b)? Eh, -2\Delta LL(df=7) = 13.99, p = .05
                                                                     MODEL MODIFICATION INDICES (relevant for invariance testing)
                                                                    Means/Intercepts/Thresholds
                                                                                        M.I. E.P.C. Std E.P.C. StdYX E.P.C.
                                                                    [ V2T1 ]
                                                                                        8.560 -0.497 -0.497
                                                                                                                         -0.137
Although fit is close to not worse than the partial metric model,
there is a significant modification index for v2T1, suggesting
localized strain. So let's see what happens if we free that one, too.
```

The intercepts at the end of Model 3d are shown on the left.

Model 3d. Partial Scalar Invariance Model (all intercepts held equal across over time except v1T1, v5T1, v4T1, v2T1)

```
MODEL: ! Model 3d: Partial Scalar Invariance,
                                                                    MODEL FIT INFORMATION
        ! no v1T1 v5T1 v4T1 v2T1
                                                                    Number of Free Parameters
                                                                                                                      60
! Factor loadings still constrained equal over time except v1T1
                                                                     Loglikelihood
 Time1 BY v1T1* v2T1* v3T1* v4T1* v5T1* v6T1* (L1a L2-L6);
                                                                               HO Value
                                                                                                               -4437.665
  Time2 BY v1T2* v2T2* v3T2* v4T2* v5T2* v6T2* (L1-L6);
                                                                               HO Scaling Correction Factor
                                                                                                                1.5560
 Time3 BY v1T3* v2T3* v3T3* v4T3* v5T3* v6T3* (L1-16);
                                                                                for MLR
! Item intercepts NOW CONSTRAINED EQUAL ACROSS TIME,
                                                                               H1 Value
                                                                                                               -4284.045
! no v1T1 v5T1 v4T1 v2T1
                                                                               H1 Scaling Correction Factor
                                                                                                                1.2029
  [v1T1*]; [v1T2* v1T3*] (I1); ! 3a: I1 applies only to 2 and 3
                                                                                 for MLR
  [v2T1*]; [v2T2* v2T3*] (I2); ! 3d: I2 applies only to 2 and 3
            v3T2* v3T3*] (I3);
                                                                     Information Criteria
  [v4T1*]; [v4T2* v4T3*] (I4); ! 3c: I4 applies only to 2 and 3
                                                                               Akaike (AIC)
                                                                                                                8995.330
  [v5T1*]; [v5T2* v5T3*] (I5); ! 3b: I5 applies only to 2 and 3
                                                                               Bayesian (BIC)
                                                                                                                9176.366
            v6T2* v6T3*] (I6);
                                                                               Sample-Size Adjusted BIC
                                                                                                                8986.473
! Residual variances all freely estimated, not labeled
                                                                                 (n* = (n + 2) / 24)
 v1T1* v1T2* v1T3*; v2T1* v2T2* v2T3*;
 v3T1* v3T2* v3T3*; v4T1* v4T2* v4T3*;
                                                                     Chi-Square Test of Model Fit
 v5T1* v5T2* v5T3*; v6T1* v6T2* v6T3*;
                                                                               Value
                                                                                                                 295.788*
! Factor variance AT TIME 1 fixed=1 for identification
                                                                               Degrees of Freedom
                                                                                                                     129
 Time1@1 Time2* Time3*;
                                                                               P-Value
                                                                                                                  0.0000
! Factor mean AT TIME 1 fixed=0 for identification
                                                                               Scaling Correction Factor
                                                                                                                  1.0387
  [Time1@0 Time2* Time3*];
                                                                                 for MLR
! Factor covariances all freely estimated
 Time1 Time2 Time3 WITH Time1* Time2* Time3*;
                                                                    RMSEA (Root Mean Square Error Of Approximation)
! Residual covariances estimated for same item over time
                                                                               Estimate
                                                                                                                   0.093
 v1T1 v1T2 v1T3 WITH v1T1* v1T2* v1T3*;
                                                                               90 Percent C.I.
                                                                                                                   0.079 0.106
 v2T1 v2T2 v2T3 WITH v2T1* v2T2* v2T3*;
                                                                               Probability RMSEA <= .05
                                                                                                                   0.000
 v3T1 v3T2 v3T3 WITH v3T1* v3T2* v3T3*;
                                                                    CFI/TLI
 v4T1 v4T2 v4T3 WITH v4T1* v4T2* v4T3*;
                                                                               CFI
                                                                                                                   0.904
 v5T1 v5T2 v5T3 WITH v5T1* v5T2* v5T3*;
                                                                               TIT
                                                                                                                   0.887
  v6T1 v6T2 v6T3 WITH v6T1* v6T2* v6T3*;
                                                                     Chi-Square Test of Model Fit for the Baseline Model
    20
                                                                               Value
                                                                                                                1896.788
                                                                               Degrees of Freedom
                                                                                                                     153
                                                                               P-Value
                                                                                                                  0.0000
    15
                                                                     SRMR (Standardized Root Mean Square Residual)
                                                                               Value
                                                                                                                   0.091
 tem Intercepts
    10
                                                   ■ Time 1
                                                                     Does the partial scalar model (3d) fit better than the partial scalar model
                                                   ■ Time 2
                                                                     (3c)? Yes, -2\Delta LL(df=1) = 8.73, p < .01
     5
                                                   ■ Time 3
                                                                    Does the partial scalar model (3d) fit worse than the partial metric model
                                                                    (2b)? No, -2\Delta LL(df=6) = 4.35, p = .63
     0
                                                                     No invariance-related modification indices remain, so we are done!
```

v1

v2

v3

3d UNSTANDARDIZED PARTIAL SCALAR MODEL RESULTS

3d UNSTAN	NDARDIZED P	ARTIAL SCALA	R MODEL R			1				
					Two-Tailed					Two-Tailed
		Estimate	S.E.	Est./S.E.	P-Value		Estimate	S.E.	Est./S.E.	P-Value
TIME1	BY					Means (FACT	OR MEAN AT TIME1	FIXED=0 FOR	IDENTIFICAT	ION)
V1T1		3.231	0.262	12.330	0.000	TIME1	0.000	0.000	999.000	999.000
V2T1		1.953	0.201	9.739	0.000	TIME2	0.293	0.081	3.625	0.000
V3T1		1.974	0.198	9.989	0.000	TIME3	0.521	0.093	5.612	0.000
V4T1		1.904	0.220	8.656	0.000					
V5T1		0.983	0.138	7.097	0.000	Intercepts				
V6T1		1.477	0.130	11.353	0.000	V1T1	16.090	0.274	58.684	0.000
						V1T2	16.425	0.281	58.364	0.000
TIME2	BY					V1T3	16.425	0.281	58.364	0.000
V1T2	21	2.629	0.232	11.317	0.000	V2T1	8.674	0.294	29.540	0.000
V2T2		1.953	0.201	9.739	0.000	V2T2	9.413	0.261	36.036	0.000
V3T2		1.974	0.198	9.989	0.000	V2T3	9.413	0.261	36.036	0.000
V4T2		1.904	0.220	8.656	0.000	V3T1	11.950	0.225	53.099	0.000
V5T2		0.983	0.138	7.097	0.000	V3T1	11.950	0.225	53.099	0.000
V6T2		1.477	0.130	11.353	0.000	V312 V3T3	11.950	0.225	53.099	0.000
V012		1.1//	0.130	11.555	0.000	V4T1	-3.024	0.267	-11.334	0.000
TIME3	BY					V4T2	-3.744	0.299	-12.535	0.000
V1T3	DI	2.629	0.232	11.317	0.000	V4T3	-3.744	0.299	-12.535	0.000
V2T3		1.953	0.201	9.739	0.000	V5T1	-1.215	0.131	-9.277	0.000
V213		1.974	0.198	9.989	0.000	V5T2	-1.802	0.207	-8.706	0.000
V4T3		1.904	0.220	8.656	0.000	V5T3	-1.802	0.207		0.000
V413		0.983	0.220	7.097	0.000	V6T1	-2.854	0.161		0.000
V513 V6T3		1.477	0.130	11.353	0.000	V6T2	-2.854	0.161		0.000
V 0 1 3		1.4//	0.130	11.333	0.000	V612 V6T3	-2.854	0.161		0.000
TIME1	WITH					V 013	-2.634	0.161	-17.000	0.000
TIME1		0.850	0.079	10.809	0.000	Posidual V	ariances (ITEM VAI	סדאאורי ייטאיי	TO NOT THE	EV CHOD)
TIME2		0.686	0.079	5.543	0.000	V1T1	0.170	0.374	0.454	0.650
TIMES)	0.000	0.124	3.343	0.000	V1T1 V1T2	0.548	0.265	2.070	0.038
TIME2	WITH					V112 V1T3	0.509	0.263	1.618	0.106
TIME2		0.706	0.128	5.519	0.000	V113 V2T1				0.000
TIMES)	0.706	0.128	5.519	0.000	V2T1 V2T2	8.702 5.895	1.026 0.605	8.483 9.746	0.000
*** 5	11	ances among				V2T2 V2T3				0.000
^^^ Kesio	ual covari	ances among	same item	over time	^ ^ ^ ^		5.177	0.795	6.514	
771 m1	D.T. T. II.					V3T1	2.502	0.386		0.000
	WITH	0.006	0 046	0 000	0 400	V3T2	2.178	0.352	6.183	0.000
V1T2		-0.206	0.246	-0.838	0.402	V3T3	2.309	0.416		0.000
V1T3		-0.010	0.233	-0.043	0.966	V4T1	7.172	1.021	7.021	0.000
1 m 0						V4T2	6.759	0.967	6.990	0.000
V1T2	WITH	0.100	0 003	0 5 5 5	0 555	V4T3	6.613	1.128	5.860	0.000
V1T3		0.130	0.231	0.561	0.575	V5T1	1.829	0.443	4.131	0.000
	• • •					V5T2	4.678	1.430	3.272	0.001
						V5T3	2.944	0.760		0.000
		ARIANCE AT T			·	V6T1	1.707	0.242	7.059	0.000
TIME1		1.000	0.000	999.000	999.000	V6T2	1.090	0.165	6.599	0.000
TIME2		1.167	0.187	6.252	0.000	V6T3	0.784	0.170	4.618	0.000
TIME3	3	0.947	0.156	6.054	0.000					
						1				

Model 4a. Residual Variance Invariance Model (error variances held equal for all except non-invariant items)

Model 4a. Residual variance invariance Model (error variances neid 6	tqual for all except hori-invariant items	
MODEL: ! Model 4a: Residual Variances		
! except for non-invariant items	MODEL FIT INFORMATION	
	Number of Free Parameters 52	
! Factor loadings still constrained equal over time except v1T1		
Time1 BY v1T1* v2T1* v3T1* v4T1* v5T1* v6T1* (L1a L2-L6);	Loglikelihood	
Time2 BY v1T2* v2T2* v3T2* v4T2* v5T2* v6T2* (L1-L6);	HO Value -4454.592	
Time3 BY v1T3* v2T3* v3T3* v4T3* v5T3* v6T3* (L1-16);	HO Scaling Correction Factor 1.5487	
! Item intercepts still constrained equal over time	for MLR	
! no v1T1 v5T1 v4T1 v2T1	H1 Value -4284.045	
[v1T1*]; [v1T2* v1T3*] (I1); ! 3a: I1 applies only to 2 and 3	H1 Scaling Correction Factor 1.2029	
[v2T1*]; [v2T2* v2T3*] (I2); ! 3d: I2 applies only to 2 and 3	for MLR	
[v3T1* v3T2* v3T3*] (I3);		
[v4T1*]; [v4T2* v4T3*] (I4); ! 3c: I4 applies only to 2 and 3	Information Criteria	
[v5T1*]; [v5T2* v5T3*] (I5); ! 3b: I5 applies only to 2 and 3	Akaike (AIC) 9013.185	
[v6T1* v6T2* v6T3*] (I6);	Bayesian (BIC) 9170.083	
! Residual variances NOW CONSTRAINED EQUAL ACROSS TIME	Sample-Size Adjusted BIC 9005.509	
-		
(WHEN POSSIBLE)	(n* = (n + 2) / 24)	
v1T1*; v1T2* v1T3* (E1); !4a: E1 applies only to 2 and 3	Ohi Owen Back of Madel Bit	
v2T1*; v2T2* v2T3* (E2); !4a: E2 applies only to 2 and 3	Chi-Square Test of Model Fit	
v3T1* v3T2* v3T3* (E3);	Value 318.280*	
v4T1*; v4T2* v4T3* (E4); !4a: E4 applies only to 2 and 3	Degrees of Freedom 137	
v5T1*; v5T2* v5T3* (E5); !4a: E5 applies only to 2 and 3	P-Value 0.0000	
v6T1* v6T2* v6T3* (E6);	Scaling Correction Factor 1.0717	
! Factor variance AT TIME 1 fixed=1 for identification	for MLR	
<pre>Time1@1 Time2* Time3*;</pre>		
! Factor mean AT TIME 1 fixed=0 for identification	RMSEA (Root Mean Square Error Of Approximation)	
[Time1@0 Time2* Time3*];	Estimate 0.094	
! Factor covariances all freely estimated	90 Percent C.I. 0.080 0.1	07
<pre>Time1 Time2 Time3 WITH Time1* Time2* Time3*;</pre>	Probability RMSEA <= .05 0.000	
! Residual covariances estimated for same item over time		
v1T1 v1T2 v1T3 WITH v1T1* v1T2* v1T3*;	CFI/TLI	
v2T1 v2T2 v2T3 WITH v2T1* v2T2* v2T3*;	CFI 0.896	
v3T1 v3T2 v3T3 WITH v3T1* v3T2* v3T3*;	TLI 0.884	
v4T1 v4T2 v4T3 WITH v4T1* v4T2* v4T3*;		
v5T1 v5T2 v5T3 WITH v5T1* v5T2* v5T3*;	SRMR (Standardized Root Mean Square Residual)	
v6T1 v6T2 v6T3 WITH v6T1* v6T2* v6T3*;	Value 0.095	
	MODEL MODIFICATION INDICES (relevant for invariance tes	ting)
Door the full recidual model (40) fit wares then the neutial coals: we del	Means/Intercepts/Thresholds	٠,
Does the full residual model (4a) fit worse than the partial scalar model		
(3d)? Yes, $-2\Delta LL(df=8) = 24.72$, $p < .01$	M.I. E.P.C. Std E.P.C. StdYX E	.P.C.
	Variances/Residual Variances	
	Variances, neeradar variances	
	V5T2 12.740 0.755 0.755 0	.153
Modification indices suggest freeing v5 across Time2 and Time3, so let's		.238
		.124
try that next.		.124
	V6T3 7.815 -0.393 -0.393 -0	.124
	1	

Model 4b. Partial Residual Variance Invariance Model (error variances held equal for all except non-invariant items and v5T2/T3)

```
MODEL: ! Model 4b: Residual Variances
       ! except for non-invariant items, v5T2-v5T3
                                                                   MODEL FIT INFORMATION
                                                                   Number of Free Parameters
                                                                                                                   53
! Factor loadings still constrained equal over time except v1T1
  Time1 BY v1T1* v2T1* v3T1* v4T1* v5T1* v6T1* (L1a L2-L6);
                                                                   Loglikelihood
  Time2 BY v1T2* v2T2* v3T2* v4T2* v5T2* v6T2* (L1-L6);
                                                                             HO Value
                                                                                                            -4447.259
 Time3 BY v1T3* v2T3* v3T3* v4T3* v5T3* v6T3* (L1-16);
                                                                             HO Scaling Correction Factor
                                                                                                             1.5823
! Item intercepts still constrained equal over time
                                                                             for MLR
! no v1T1 v5T1 v4T1 v2T1
                                                                          H1 Value
                                                                                                           -4284.045
  [v1T1*]; [v1T2* v1T3*] (I1); ! 3a: I1 applies only to 2 and 3
                                                                           H1 Scaling Correction Factor 1.2029
  [v2T1*]; [v2T2* v2T3*] (I2); ! 3d: I2 applies only to 2 and 3
                                                                              for MLR
           v3T2* v3T3*] (I3);
  [v4T1*]; [v4T2* v4T3*] (I4); ! 3c: I4 applies only to 2 and 3
                                                                   Information Criteria
  [v5T1*]; [v5T2* v5T3*] (I5); ! 3b: I5 applies only to 2 and 3
                                                                             Akaike (AIC)
                                                                                                             9000.518
           v6T2* v6T3*] (I6);
                                                                             Bavesian (BIC)
                                                                                                            9160.434
! Residual variances NOW CONSTRAINED EQUAL ACROSS TIME
                                                                             Sample-Size Adjusted BIC
                                                                                                             8992.694
  (WHEN POSSIBLE) except v5T2-v5T3
                                                                              (n* = (n + 2) / 24)
  v1T1*; v1T2* v1T3* (E1); !4a: E1 applies only to 2 and 3
 v2T1*; v2T2* v2T3* (E2); !4a: E2 applies only to 2 and 3
                                                                   Chi-Square Test of Model Fit
 v3T1* v3T2* v3T3* (E3);
                                                                             Value
                                                                                                              309.384*
 v4T1*; v4T2* v4T3* (E4); !4a: E4 applies only to 2 and 3
                                                                             Degrees of Freedom
                                                                                                                136
 v5T1*; v5T2*; v5T3*; !4b: 2 and 3 now also separate
                                                                             P-Value
                                                                                                              0.0000
 v6T1* v6T2* v6T3* (E6);
                                                                             Scaling Correction Factor
                                                                                                        1.0551
! Factor variance AT TIME 1 fixed=1 for identification
                                                                               for MLR
 Time1@1 Time2* Time3*;
! Factor mean AT TIME 1 fixed=0 for identification
                                                                   RMSEA (Root Mean Square Error Of Approximation)
  [Time1@0 Time2* Time3*];
                                                                             Estimate
                                                                                                                0.092
! Factor covariances all freely estimated
                                                                             90 Percent C.I.
                                                                                                               0.078 0.105
 Time1 Time2 Time3 WITH Time1* Time2* Time3*;
                                                                             Probability RMSEA <= .05
                                                                                                              0.000
! Residual covariances estimated for same item over time
 v1T1 v1T2 v1T3 WITH v1T1* v1T2* v1T3*;
                                                                   CFI/TLI
                                                                                                                0.901
 v2T1 v2T2 v2T3 WITH v2T1* v2T2* v2T3*;
                                                                             CFI
 v3T1 v3T2 v3T3 WITH v3T1* v3T2* v3T3*;
                                                                             TLI
                                                                                                                0.888
 v4T1 v4T2 v4T3 WITH v4T1* v4T2* v4T3*;
                                                                   SRMR (Standardized Root Mean Square Residual)
 v5T1 v5T2 v5T3 WITH v5T1* v5T2* v5T3*;
 v6T1 v6T2 v6T3 WITH v6T1* v6T2* v6T3*;
                                                                             Value
                                                                                                                0.093
                                                                   MODEL MODIFICATION INDICES (relevant for invariance testing)
Does the partial residual model (4b) fit better than the full residual model
                                                                   Means/Intercepts/Thresholds
(4a)? Yes, -2\Delta LL(df=1) = 10.06, p < .01
                                                                                       M.I. E.P.C. Std E.P.C. StdYX E.P.C.
Does the partial residual model (4b) fit worse than the partial scalar model
                                                                   Variances/Residual Variances
(3d)? Eh, -2\Delta LL(df=7) = 14.14, p = .05
                                                                                      13.772
                                                                   V6T1
                                                                                                   0.419 0.419
                                                                                                                           0.125
                                                                   V6T3
                                                                                       7.149 -0.373
                                                                                                            -0.373
                                                                                                                          -0.118
Modification indices suggest freeing v6 from Time1, so let's try that next.
```

Model 4c. Partial Residual Variance Invariance Model (error variances held equal for all except non-invariant items, v5T2/T3, v6T1)

```
MODEL: ! Model 4c: Residual Variances
       ! except for non-invariant items, v5T2-v5T3, v6T1
! Factor loadings still constrained equal over time except v1T1
 Time1 BY v1T1* v2T1* v3T1* v4T1* v5T1* v6T1* (L1a L2-L6);
 Time2 BY v1T2* v2T2* v3T2* v4T2* v5T2* v6T2* (L1-L6);
 Time3 BY v1T3* v2T3* v3T3* v4T3* v5T3* v6T3* (L1-16);
! Item intercepts still constrained equal over time
! no v1T1 v5T1 v4T1 v2T1
  [v1T1*]; [v1T2* v1T3*] (I1); ! 3a: I1 applies only to 2 and 3
  [v2T1*]; [v2T2* v2T3*] (I2); ! 3d: I2 applies only to 2 and 3
           v3T2* v3T3*] (I3);
  [v3T1*
  [v4T1*]; [v4T2* v4T3*] (I4); ! 3c: I4 applies only to 2 and 3
  [v5T1*]; [v5T2* v5T3*] (I5); ! 3b: I5 applies only to 2 and 3
  [v6T1*
           v6T2* v6T3*] (I6);
! Residual variances NOW CONSTRAINED EQUAL ACROSS TIME
  (WHEN POSSIBLE) except v5T2-v5T3, v6T1
 v1T1*; v1T2* v1T3* (E1); !4a: E1 applies only to 2 and 3
 v2T1*; v2T2* v2T3* (E2); !4a: E2 applies only to 2 and 3
 v3T1* v3T2* v3T3* (E3);
 v4T1*; v4T2* v4T3* (E4); !4a: E4 applies only to 2 and 3
 v5T1*; v5T2*; v5T3*;
                            !4b: 2 and 3 now also separate
 v6T1*; v6T2* v6T3* (E6); !4c: E6 applies only to 2 and 3
! Factor variance AT TIME 1 fixed=1 for identification
 Time1@1 Time2* Time3*;
! Factor mean AT TIME 1 fixed=0 for identification
  [Time1@0 Time2* Time3*];
! Factor covariances all freely estimated
 Time1 Time2 Time3 WITH Time1* Time2* Time3*;
! Residual covariances estimated for same item over time
 v1T1 v1T2 v1T3 WITH v1T1* v1T2* v1T3*;
 v2T1 v2T2 v2T3 WITH v2T1* v2T2* v2T3*;
 v3T1 v3T2 v3T3 WITH v3T1* v3T2* v3T3*;
 v4T1 v4T2 v4T3 WITH v4T1* v4T2* v4T3*;
 v5T1 v5T2 v5T3 WITH v5T1* v5T2* v5T3*;
 v6T1 v6T2 v6T3 WITH v6T1* v6T2* v6T3*;
                                     ■ Time 1
 E 4
                                     ■ Time 2
                                     ■ Time 3
  3
      v1
           v2
```

-	INFORMATION Free Parameters	54	
Loglikeli	.hood H0 Value H0 Scaling Correction Factor for MLR H1 Value H1 Scaling Correction Factor for MLR	-4284.045	
Informati	On Criteria Akaike (AIC) Bayesian (BIC) Sample-Size Adjusted BIC (n* = (n + 2) / 24)	8987.942 9150.876 8979.971	
Chi-Squar	re Test of Model Fit Value Degrees of Freedom P-Value Scaling Correction Factor for MLR	296.084* 135 0.0000 1.0533	
RMSEA (Ro	eot Mean Square Error Of Approx Estimate 90 Percent C.I. Probability RMSEA <= .05	ximation) 0.089 0.075 0.000	0.103
CFI/TLI	CFI TLI	0.908 0.895	
SRMR (Sta	andardized Root Mean Square Re Value	sidual) 0.092	

Does the partial residual model (4c) fit *better* than the partial residual model (4b)? Yes, $-2\Delta LL(df=1) = 11.20$, p < .01

Does the partial residual model (4c) fit worse than the partial scalar model (3d)? No, $-2\Delta LL(df=6) = 3.38$, p = .76

No invariance-related modification indices remain, so we are done! The residual variances at the end of Model 4c are shown on the left. Next is structural invariance.

4c UNSTANDARDIZED FINAL MEASUREMENT INVARIANCE SOLUTION

TIME1 BY V1T1 V2T1 V3T1 V4T1 V5T1 V6T1 TIME2 BY V1T2 V2T2	3.214 1.945 1.983 1.913 0.987	0.259 0.200 0.196	Est./S.E. 12.409 9.735	Two-Tailed P-Value	Means (F1CTOD	Estimate	S.E.	Est./S.E.	Wo-Tailed P-Value
V1T1 V2T1 V3T1 V4T1 V5T1 V6T1 TIME2 BY V1T2	1.945 1.983 1.913 0.987	0.200 0.196		0.000	Means (FACTOR				
V1T1 V2T1 V3T1 V4T1 V5T1 V6T1 TIME2 BY V1T2	1.945 1.983 1.913 0.987	0.200 0.196		0.000	Means (FACTOD				
V2T1 V3T1 V4T1 V5T1 V6T1 TIME2 BY V1T2	1.945 1.983 1.913 0.987	0.200 0.196		0.000	,	MEAN AT TIME1 FIX			,
V3T1 V4T1 V5T1 V6T1 TIME2 BY V1T2	1.983 1.913 0.987	0.196	9.735		TIME1	0.000	0.000	999.000	999.000
V4T1 V5T1 V6T1 TIME2 BY V1T2	1.913 0.987			0.000	TIME2	0.295	0.081	3.654	0.000
V5T1 V6T1 TIME2 BY V1T2	0.987		10.094	0.000	TIME3	0.520	0.092	5.668	0.000
V6T1 TIME2 BY V1T2		0.219	8.741	0.000					
TIME2 BY V1T2		0.138	7.154	0.000	-	V3 AND V6 ARE HOL			
V1T2	1.470	0.123	11.975	0.000	V1T1	16.089	0.275	58.597	0.000
V1T2					V1T2	16.418	0.283	58.056	0.000
					V1T3	16.418	0.283	58.056	0.000
V2T2	2.644	0.230	11.473	0.000	V2T1	8.675	0.294	29.523	0.000
	1.945	0.200	9.735	0.000	V2T2	9.416	0.262	35.991	0.000
V3T2	1.983	0.196	10.094	0.000	V2T3	9.416	0.262	35.991	0.000
V4T2	1.913	0.219	8.741	0.000	V3T1	11.950	0.225	53.170	0.000
V5T2	0.987	0.138	7.154	0.000	V3T2	11.950	0.225	53.170	0.000
V6T2	1.470	0.123	11.975	0.000	V3T3	11.950	0.225	53.170	0.000
					V4T1	-3.024	0.266	-11.352	0.000
TIME3 BY					V4T2	-3.750	0.298	-12.565	0.000
V1T3	2.644	0.230	11.473	0.000	V4T3	-3.750	0.298	-12.565	0.000
V2T3	1.945	0.200	9.735	0.000	V5T1	-1.213	0.131	-9.275	0.000
V3T3	1.983	0.196	10.094	0.000	V5T2	-1.803	0.207	-8.720	0.000
V4T3	1.913	0.219	8.741	0.000	V5T3	-1.803	0.207	-8.720	0.000
V5T3	0.987	0.138	7.154	0.000	V6T1	-2.851	0.160	-17.815	0.000
V6T3	1.470	0.123	11.975	0.000	V6T2	-2.851	0.160	-17.815	0.000
					V6T3	-2.851	0.160	-17.815	0.000
TIME1 WITH	I								
TIME2	0.843	0.078	10.745	0.000	Residual Vari	ances - ITEM VARI	ANCE THAT	IS NOT THE	FACTOR
TIME3	0.683	0.124	5.505	0.000	V1T1	0.285	0.342	0.831	0.406
					V1T2	0.539	0.233	2.316	0.021
TIME2 WITH	I				V1T3	0.539	0.233	2.316	0.021
TIME3	0.692	0.126	5.489	0.000	V2T1	8.562	1.004	8.526	0.000
					V2T2	5.592	0.502	11.132	0.000
*** Residual o	covariances among	same item	n over time '	***	V2T3	5.592	0.502	11.132	0.000
	_				V3T1	2.312	0.271	8.534	0.000
V1T1 WITH					V3T2	2.312	0.271	8.534	0.000
V1T2	-0.165	0.230	-0.716	0.474	V3T3	2.312	0.271	8.534	0.000
V1T3	0.014	0.212	0.066	0.948	V4T1	7.139	1.043	6.842	0.000
					V4T2	6.686	0.870	7.684	0.000
V1T2 WITH	Ι				V4T3	6.686	0.870	7.684	0.000
V1T3	0.153	0.230	0.667	0.505	V5T1	1.829	0.448	4.078	0.000
					V5T2	4.705	1.455	3.233	0.001
					V5T3	2.908	0.749	3.881	0.000
Variances (FAC	CTOR VARIANCE AT T	IME1=1 FO	R IDENTIFICA	ATION)	V6T1	1.664	0.233	7.138	0.000
TIME1	1.000	0.000	999.000	999.000	V6T2	0.957	0.136	7.039	0.000
TIME2	1.159	0.186	6.231	0.000	V6T3	0.957	0.136	7.039	0.000
TIME3	0.934	0.151	6.171	0.000	1.120	0.30	1,100		2.000

STRUCTURAL INVARIANCE TESTS

Model 5a. Factor Variance Invariance Model

Model 6a. Factor Covariance Invariance Model

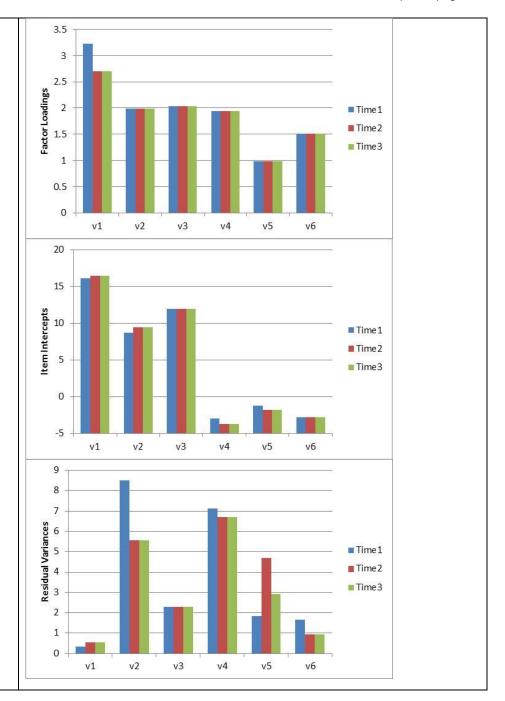
MODEL: ! Model 5a:	Factor Varia			•	MODEL: ! Model 6a: Factor Covariance Invariance						
(rest of code befor	e and after	is same as	4C)		(rest of code before and after is same as 5a)						
! Model 5a: Factor Time1@1 Time2@1		ariance (al	ll fixed t	o 1 now)	! Model 6a: Factor Covariance Invariance (all constrained equal) Time1 Time2 Time3 WITH Time1* Time2* Time3* (Fcov);						
MODEL FIT INFORMATI	ON				MODEL FIT IN	FORMATION					
Number of Free Para	meters		52		Number of Fre	ee Parameters		5	0		
Loglikelihood					Loglikelihoo	d					
H0 Value		-	-4441.238		_	Value		-4443.65	4		
H0 Scalin	g Correction	Factor	1.5848		HO	Scaling Corre	ction Facto	r 1.564	9		
for MLR						for MLR					
H1 Value		-	-4284.045		H1	Value		-4284.04	5		
H1 Scalin	g Correction	Factor	1.2029		H1	Scaling Corre	ction Facto	r 1.202	9		
for MLR						for MLR					
Information Criteri	.a				Information (Criteria					
Akaike (A	IC)		8986.475		Aka	aike (AIC)		8987.30	8		
Bayesian	(BIC)		9143.374		Ва	yesian (BIC)		9138.17	2		
Sample-Si	ze Adjusted	BIC	8978.799			mple-Size Adju		8979.92	7		
$(n^* = ($	(n + 2) / 24)					(n* = (n + 2)					
Chi-Square Test of						est of Model F					
Value			297.152*		Val	lue		297.56	8*		
Degrees o	of Freedom		137		Dec	grees of Freed	om	13	9		
P-Value			0.0000			Value		0.000	0		
Scaling C for MLR	Correction Fa	ctor	1.0580			aling Correcti for MLR	on Factor	1.072	8		
RMSEA (Root Mean Sq	uare Error O	f Approxima	ation)		RMSEA (Root I	Mean Square Er	ror Of Appr	oximation)			
Estimate	•	11	0.088			timate	- 1	0.08	7		
90 Percen	ıt C.I.		0.074	0.102	90	Percent C.I.		0.07	3 0.101		
	ty RMSEA <=	.05	0.000			obability RMSE	A <= .05				
CFI/TLI					CFI/TLI						
CFI			0.908		CF	I		0.90	9		
TLI			0.897		TL			0.90			
SRMR (Standardized	Root Mean So	uare Residu				- rdized Root Me	an Square R				
Value			0.100		· ·	lue		0.10	0		
Does the factor varian model (4c)? No, -2ΔLl			an the part	ial residual		or covariance mo o, -2ΔLL(df=2) =		vorse than the	factor variance		
Factor Covariances.					FACTOR COVAR	IANCES FROM MO	DEL 6a (REP	RESENT CORRE	LATIONS):		
TIME1 WITH						IME2 0.724			0.000		
TIME2	0.778	0.042	18.374	0.000		IME3 0.724			0.000		
TIME3	0.713	0.087	8.214	0.000	TIME2 WITH T				0.000		
TIME2 WITH					FACTOR MEANS	FROM MODEL 6a	•		ENCES):		
TIME3	0.662	0.095	6.929	0.000	TIME1	0.000	0.000	999.000	999.000		
					TIME2	0.284			0.000		
					TIME3	0.520	0.091	5.700	0.000		

Model 7a. Factor Mean Invariance Model

```
MODEL: ! Model 7a: Factor Mean Invariance
       ! Testing Diff between Time2 and Time3
! Factor loadings still constrained equal over time except v1T1
 Time1 BY v1T1* v2T1* v3T1* v4T1* v5T1* v6T1* (L1a L2-L6);
 Time2 BY v1T2* v2T2* v3T2* v4T2* v5T2* v6T2* (L1-L6);
 Time3 BY v1T3* v2T3* v3T3* v4T3* v5T3* v6T3* (L1-16);
! Item intercepts still constrained equal over time
! no v1T1 v5T1 v4T1
  [v1T1*]; [v1T2* v1T3*] (I1); ! 3a: I1 applies only to 2 and 3
  [v2T1*]; [v2T2* v2T3*] (I2); ! 3d: I2 applies only to 2 and 3
           v3T2* v3T3*] (I3);
  [v3T1*
  [v4T1*]; [v4T2* v4T3*] (I4); ! 3c: I4 applies only to 2 and 3
  [v5T1*]; [v5T2* v5T3*] (I5); ! 3b: I5 applies only to 2 and 3
  [v6T1*
           v6T2* v6T3*] (I6);
! Residual variances still constrained equal over time
  (WHEN POSSIBLE) except v5T2-v5T3, v6T1
 v1T1*; v1T2* v1T3* (E1); !4a: E1 applies only to 2 and 3
 v2T1*; v2T2* v2T3* (E2); !4a: E2 applies only to 2 and 3
 v3T1* v3T2* v3T3* (E3);
 v4T1*; v4T2* v4T3* (E4); !4a: E4 applies only to 2 and 3
 v5T1*; v5T2*; v5T3*;
                           !4b: 2 and 3 now also separate
 v6T1*; v6T2* v6T3* (E6); !4c: E6 applies only to 2 and 3
! Factor variance fixed=1 for structural invariance
 Time1@1 Time2@1 Time3@1;
! Testing factor mean difference between Time2 and Time3
  [Time1@0]; [Time2* Time3*] (Fmean); ! NEW CONSTRAINT
! Factor covariances held equal for structural invariance
 Time1 Time2 Time3 WITH Time1* Time2* Time3* (Fcov):
! Residual covariances estimated for same item over time
 v1T1 v1T2 v1T3 WITH v1T1* v1T2* v1T3*;
 v2T1 v2T2 v2T3 WITH v2T1* v2T2* v2T3*;
 v3T1 v3T2 v3T3 WITH v3T1* v3T2* v3T3*;
 v4T1 v4T2 v4T3 WITH v4T1* v4T2* v4T3*;
 v5T1 v5T2 v5T3 WITH v5T1* v5T2* v5T3*;
 v6T1 v6T2 v6T3 WITH v6T1* v6T2* v6T3*;
```

Does the factor mean model (7a) fit worse than the factor covariance model (6a)? Yes, $-2\Delta LL(df=1) = 11.15$, p < .01, so we keep Model 6a instead.

```
MODEL FIT INFORMATION
Number of Free Parameters
Loglikelihood
          HO Value
                                          -4448.472
          HO Scaling Correction Factor
                                             1.5792
            for MLR
Means
    TIME1
                       0.000
                                   0.000
                                             999.000
                                                        999,000
    TIME2
                       0.378
                                   0.075
                                               5.014
                                                          0.000
                                                          0.000
    TIME3
                       0.378
                                   0.075
                                               5.014
```



6a UNSTANDARDIZED FINAL STRUCTURAL INVARIANCE SOLUTION

oa UNSTAL	NDARDIZED	FINAL STRUCTU	KAL INVAL	TANCE SOLUT	Two-Tailed					Two-Tailed
		Estimate	S.E.	Est./S.E.	P-Value		Estimate	S.E.	Est./S.E.	P-Value
		претшаес	0.1.	дос., о.д.	ı varac		DD CIMA CC	0.1.	шос., о.ш.	1 Value
TIME1	BY					Means (FACTOR	MEAN AT TIME1 FIX	ED=0 FOR	IDENTIFICAT	ION)
V1T1		3.229	0.243	13.272	0.000	TIME1	0.000	0.000	999.000	999.000
V2T1		1.993	0.170	11.754	0.000	TIME2	0.284	0.079	3.605	0.000
V3T1		2.029	0.169	12.022	0.000	TIME3	0.520	0.091	5.700	0.000
V4T1		1.939	0.214	9.077	0.000		****			
V5T1		0.986	0.147	6.701	0.000	Intercepts -	V3 AND V6 ARE HOL	DING THIS	TOGETHER W	ITH TIME1
V6T1		1.508	0.109	13.821	0.000	V1T1	16.099	0.271	59.420	0.000
						V1T2	16.428	0.281	58.488	0.000
TIME2	BY					V1T3	16.428	0.281	58.488	0.000
V1T2		2.704	0.232	11.677	0.000	V2T1	8.681	0.292	29.694	0.000
V2T2		1.993	0.170	11.754	0.000	V2T2	9.423	0.259	36.368	0.000
V3T2		2.029	0.169	12.022	0.000	V2T3	9.423	0.259	36.368	0.000
V4T2		1.939	0.214	9.077	0.000	V3T1	11.956	0.223	53.706	0.000
V5T2		0.986	0.147	6.701	0.000	V3T2	11.956	0.223	53.706	0.000
V6T2		1.508	0.109	13.821	0.000	V3T3	11.956	0.223	53.706	0.000
						V4T1	-3.018	0.263	-11.463	0.000
TIME3	BY					V4T2	-3.737	0.292	-12.784	0.000
V1T3		2.704	0.232	11.677	0.000	V4T3	-3.737	0.292	-12.784	0.000
V2T3		1.993	0.170	11.754	0.000	V5T1	-1.210	0.131	-9.269	0.000
V3T3		2.029	0.169	12.022	0.000	V5T2	-1.791	0.203	-8.807	0.000
V4T3		1.939	0.214	9.077	0.000	V5T3	-1.791	0.203	-8.807	0.000
V5T3		0.986	0.147	6.701	0.000	V6T1	-2.847	0.159	-17.889	0.000
V6T3		1.508	0.109	13.821	0.000	V6T2	-2.847	0.159	-17.889	0.000
						V6T3	-2.847	0.159	-17.889	0.000
TIME1	WITH									
TIME2	2	0.724	0.053	13.748	0.000	Residual Vari	lances - ITEM VARI.	ANCE THAT	IS NOT THE	FACTOR
TIMES	3	0.724	0.053	13.748	0.000	V1T1	0.351	0.331	1.060	0.289
						V1T2	0.562	0.231	2.432	0.015
TIME2	WITH					V1T3	0.562	0.231	2.432	0.015
TIME	3	0.724	0.053	13.748	0.000	V2T1	8.506	0.999	8.511	0.000
						V2T2	5.563	0.494	11.261	0.000
*** Resid	dual cova	riances among	same item	across tim	e ****	V2T3	5.563	0.494	11.261	0.000
						V3T1	2.288	0.269	8.507	0.000
V1T1	WITH					V3T2	2.288	0.269	8.507	0.000
V1T2		-0.106	0.225	-0.471	0.638	V3T3	2.288	0.269	8.507	0.000
V1T3		0.038	0.215	0.175	0.861	V4T1	7.134	1.041	6.853	0.000
						V4T2	6.694	0.873	7.666	0.000
V1T2	WITH					V4T3	6.694	0.873	7.666	0.000
V1T3		0.130	0.243	0.534		V5T1	1.825	0.446	4.092	0.000
0.593						V5T2	4.705	1.454	3.235	0.001
						V5T3	2.921	0.752	3.887	0.000
	•	VARIANCES CON		'		V6T1	1.656	0.235	7.054	0.000
TIME1		1.000	0.000	999.000	999.000	V6T2	0.942	0.131	7.188	0.000
TIME2		1.000	0.000	999.000	999.000	V6T3	0.942	0.131	7.188	0.000
TIME	3	1.000	0.000	999.000	999.000					

Example results section for these analyses:

The extent to which a confirmatory factor model measuring social functioning (with six observed indicators) exhibited measurement invariance and structural invariance over time (i.e., across three occasions at six-month intervals) was examined using Mplus v. 8.8 (Muthén & Muthén, 1998–2017). Robust maximum likelihood (MLR) estimation was used for all analyses; accordingly, nested model comparisons were conducted using the rescaled difference in the model –2LL values with degrees of freedom equal to the difference in the number of model parameters. A configural invariance model was initially specified in which three correlated factors (i.e., one factor for each occasion) were estimated simultaneously; all factor means were fixed to 0 and all factor variances were fixed to 1 for identification. Residual covariances for the same indicator across occasions were estimated as well. As shown in Table 1, although the configural invariance model had marginal fit, theoretically reasonable attempts to improve the fit were unsuccessful. Thus, the analysis proceeded by applying parameter constraints in successive models to examine potential decreases in fit resulting from measurement or structural non-invariance constraints over the three occasions.

Equality of the unstandardized indicator factor loadings across occasions was then examined in a metric invariance model. The factor variance was fixed to 1 at time 1 for identification but was freely estimated at times 2 and 3. The factor means were all fixed to 0 for identification. All factor loadings were constrained equal across time; all intercepts and residual variances still varied over time. Factor covariances and residual covariances were estimated as described previously. The metric invariance model fit significantly worse than the configural invariance model $-2\Delta LL(10) = 19.14$, p = .04. Modification indices suggested that the loading of indicator 1 at time 1 was a source of misfit and should be freed. After doing so, the partial metric invariance model fit significantly better than the full metric invariance model, $-2\Delta LL(1) = 7.16$, p < .001, and the partial metric invariance model did not fit worse than the configural invariance model, $-2\Delta LL(9) = 8.98$, p = .44. The fact that partial metric invariance (i.e., "weak invariance") held indicates that the same latent factor was being measured at each occasion, or that the indicators were related to their latent factor equivalently across time (except for indicator 1, which was more related to its factor at time 1 than at times 2 or 3).

Equality of the unstandardized indicator intercepts across time was then examined in a scalar invariance model. The factor mean and variance at time 1 were fixed to 0 and 1, respectively, for identification, but the factor mean and variance were then estimated at times 2 and 3. All factor loadings and indicator intercepts were constrained equal across time (except for indicator 1 at time 1); all residual variances still differed over time. Factor covariances and residual covariances were estimated as described previously. The scalar invariance model fit significantly worse than the partial metric invariance model, $-2\Delta LL(9) =$ 55.13, p < .01. Modification indices suggested that the intercept of indicator 5 at time 1 was the largest source of the misfit and should be freed. After doing so, although the partial scalar invariance model had significantly better fit than the full scalar invariance model, $-2\Delta LL(1) = 15.16$, p < .01, it still fit worse than the partial metric invariance model, -2ΔLL(8) = 27.84, p < 001. Modification indices suggested that the intercept of indicator 4 at time 1 was the largest remaining source of the misfit and should be freed. After doing so, although the new partial scalar invariance model (with the intercepts for indicators 1, 4, and 5 freed at time 1) fit significantly better than the previous partial scalar invariance model (without the intercept for indicator 4 freed at time 1), $-2\Delta LL(1) = 9.24$, p < .01, it still fit marginally worse than the partial metric invariance model, $-2\Delta LL(7) = 13.99$, p = 05. Modification indices suggested that the intercept of indicator 2 at time 1 was the largest remaining source of the misfit and should be freed. After doing so, the new partial scalar invariance model (with the intercepts for indicators 1, 2, 4 and 5 freed at time 1) fit significantly better than the previous partial scalar invariance model (without the intercept for indicator 2 freed at time 1), $-2\Delta LL(1) = 8.73$, p < .01, and it did not fit significantly worse than the partial metric invariance model, $-2\Delta LL(6) = 4.35$, p = .63. The fact that partial scalar invariance (i.e., "strong invariance") held indicates that all occasions have the same expected response for each indicator at the same absolute level of the trait, or that the observed difference in the indicator means between times 2 and 3 was due to factor mean differences only. However, indicators 1 and 2 had a lower expected response at the same absolute level of social functioning at time 1 than at time 2 or 3, while indicators 4 and 5 had a higher expected response.

Equality of the unstandardized indicator residual variances across time was then examined in a residual variance invariance model. As in the partial scalar invariance model, the factor mean and variance were fixed to 0 and 1, respectively, for identification at time 1, but the factor mean and variance were still estimated at times 2 and 3. All factor loadings (except for indicator 1 at time 1), indicator intercepts (except for indicators 1, 2, 4, and 5 at time 1), and all residual variances (except for indicators 1, 2, 4, and 5 at time 1) were constrained to be equal over time. Factor covariances and residual covariances were estimated as described previously. The residual variance invariance model fit significantly worse than the last partial scalar invariance model, $-2\Delta LL(8) = 24.72$, p < .01. Modification indices suggested that the residual variance of indicator 5 at time 2 versus time 3 was the largest remaining source of the misfit and should be freed. After doing so, the partial residual variance invariance model fit significantly better than the residual invariance model, $-2\Delta LL(1) = 10.06$, p < 10.06

.01, but still fit marginally worse than the last partial scalar invariance model, $-2\Delta LL(7) = 14.14$, p = .05. Modification indices suggested that the residual variance of indicator 6 at time 1 was the largest remaining source of the misfit and should be freed. After doing so, the new partial residual variance invariance model (with residual variances for indicators 1, 2, 4, 5, and 6 free at time 1; indicator 5 free at times 2 and 3 also) fit significantly better than the partial residual invariance model (without the residual variance for indicator 6 at time 1 freed), $-2\Delta LL(1) = 11.20$, p < .01, and did not fit worse than the last partial scalar invariance model, $-2\Delta LL(6) = 3.38$, p = .76. The fact that partial residual variance invariance (i.e., "strict invariance") held indicates that the amount of indicator variance not accounted for by the factor was the same across time (except for indicator 5, for which there was more residual variance at time 2). However, 5 out of 6 indicators did not have residual variance invariance at time 1 (although this was required because of a lack of metric or scalar invariance for indicators 1, 2, 4, and 5).

After achieving partial measurement invariance as was just described, structural invariance was then tested with three additional models. First, the factor variance at times 2 and 3 (which had been estimated freely) was constrained to 1 (i.e., to be equal to the factor variance at time 1), resulting in a nonsignificant decrease in fit relative to the last partial residual invariance model, $-2\Delta LL(2) = 1.84$, p = .40. Thus, equivalent amounts of individual differences in social functioning were found across time. Second, the factor covariances across time were constrained to be equal (which become factor correlations given a variance of 1 for each factor across time), resulting in a nonsignificant decrease in fit relative to the factor variance model, $-2\Delta LL(2) = 2.32$, p = .31. Third, the factor means at times 2 and 3 (which had been estimated freely) was constrained to be equal to each other, resulting in a significant decrease in fit relative to the factor covariance invariance model $-2\Delta LL(1) = 11.15$, p < .01, indicating that the factor mean at time 3 was significantly higher than at time 2. The factor mean at time 2 was already significantly different from 0 (the factor mean at time 1), and thus, the three factor means were significantly different, increasing over time.

In conclusion, these analyses showed that partial measurement invariance was obtained over time—that is, the relationships of the indicators to the latent factor of social functioning were equivalent at times 2 and 3, although primarily not equivalent at time 1, as previous described. These analyses also showed that partial structural invariance was obtained over time, such that the same amount of individual differences variance in social functioning was observed with equal covariance over time across occasions (i.e., compound symmetry of the latent factor), although the amount of social functioning on average increased significantly over time. Model parameters from the final model are given in Table 2.

Reference: Muthén, L. K., & Muthén, B.O. (1998–2017). Mplus user's guide (8th ed.). Los Angeles, CA: Muthén & Muthén.

(see excel worksheet for Table 1; Table 2 would have unstandardized and standardized estimates and their SEs)

You might also replace all the nested model comparisons tests in the text with a table that provides them instead.