CLDP945 Example 8a page 1 Three Level Models for Longitudinal Twin Data (Time within Twin within Pair)

The data for this example come from the Octogenarian Twin Study of Aging, a longitudinal study. These models include 351 same-sex twin pairs initially age 79–100 years measured for up to four occasions every two years, over six possible years. We will be examining change over time in a measure of crystallized intelligence (information test), as well the extent of heritability (i.e., differences between MZ and DZ twins) in intercepts and change over time. These data are already stacked such that one row contains the data for one occasion for one person. The ID variables PairID and TwinID index which twin pair and which twin (1 or 2), respectively. Time is not balanced across persons, so REPEATED will not be used until we get to the heritability models (i.e., that include different variances by zygosity).

Model 1a: Empty Means, Two-Level Model for Information Test Outcome

Level 1: In Level 2:	$ \begin{aligned} &\text{fo}_{\text{ti}} = \beta_{0\text{i}} + e_{\text{ti}} \\ &\beta_{0\text{i}} = \gamma_{00} + U_{0\text{i}} \end{aligned} $	This model h assumes that	as two variance of all people are ind	components: l dependent (i.e	evel-1 residu ., it does not	al and level-2 random intercept. It account for twin pair membership).
TITLE "SAS PROC MIXED CLAS MODE RAND ODS	Model 1a: Emp DATA=work.Exa S PairID Twin L info = / OM INTERCEPT OUTPUT InfoCr	ty Means, Tw mple8a NOCLI ID; SOLUTION DDF / VCORR TYPE it=Fit2L; *	wo-Level Mode PRINT COVTEST M=Satterthwa =UN SUBJECT= Save fit sta	el for Info <mark>NAMELEN=1</mark> ite; PairID*Twin ts for LRT	rmation T 00 IC MET nID; * Lev ; RUN;	est Outcome"; HOD=REML; zel 2+3 combined;
ECHO "SPSS MIXED info /METHOD = /PRINT = /FIXED = /RANDOM =	Model 1a: Emp BY PairID Twi = REML = SOLUTION TES = = INTERCEPT	ty Means, Tw nID TCOV COVTYPE (UN)	wo-Level Mode SUBJECT(Pair	l for Info ID*TwinID)	rmation T	est Outcome".
* STATA Mo mixed info esta esta esti	odel 1a: Empty , Case: , t ic, n(702) t icc mates store T	Means, Two- covariance // Givin // Reque woLevel	-Level Model (unstructured og STATA high ssting intrac. se is a person-lev	for Inform variance est-level s lass corres el ID variable	ation Tes reml sample siz lation needed just	t Outcome ze to use for BIC for this model in STATA.
Covariance P Columns in X	Dimensions arameters	2 1				
Subjects Max Obs Per	Per Subject Subject	1 702 → n 4	umber of perso	ns so far		Calculate the ICC for the proportion of between-person variation in Info:
Cov Parm UN(1,1) Residual Null Model DF Ch 1	Covari Subject PairID*TwinID Likelihood Rat i-Square F 1333.46	ance Paramete Estimate 136.53 23.9167 tio Test r > ChiSq <.0001 Information C	er Estimates Standard Error 8.5293 1.0694	Z Value 16.01 22.36	Pr > Z <.0001 <.0001	ICC = $\frac{136.53}{136.53 + 23.92} = .85$ The "Null Model" LRT below tells us that the random intercept variance is significantly greater than 0, and thus so is the ICC for the correlation of occasions within persons (and pairs).
Neg2LogLike 11389.5	Parms 2 113 Solution	AIC AI 93.5 11393	CC HQIC 8.5 11397.0	BIC 11402.6	CAIC 11404.6	
Effect Intercept	Solution St Estimate 25.5469	i tor Fixed Ef andard Error E 0.4911 60	FTECTS OF t Value 05 52.02	Pr > t <.0001		

Model 1b: Empty Means, Three-Level Model for Information Test Outcome

Level 1: Inf	$o_{tii} = \beta_{0ii} + e_{tii}$	This madel	ow here?	naa aama	ater lavel 1 maridual lavel 2	7
Level 2.	$\delta = \delta + U$	twin random	intercent and	level-3 pair ra	ndom intercent It now	
	$v_{0ij} = v_{00j} + v_{0ij}$	allows a corr	elation between	n people from	the same twin nair	
Level 3: δ_0	$\gamma_{00j} = \gamma_{000} + \mathbf{V}_{00j}$				the sume twin puil.	
TITLE "SAS 1	Model 1b: Empty	Means, Thr	ee-Level Mo	del for In	formation Test Outcom	ne";
PROC MIXED I	DATA=work.Examp	le8a NOCLPR	INT COVTEST	NAMELEN=1	00 IC METHOD=REML;	
MODEL	pairid twintd	;	Sattorthwai	ito.		
RANDO	M INTERCEPT /	TYPE=UN SUB	ECT=PairID	;	* Level 3;	
RANDO	M INTERCEPT /	TYPE=UN SUB	ECT=PairID	TwinID;	* Level 2;	
ODS C	UTPUT InfoCrit	=Fit3L CovPa	arms=CovEmpt	cy; * Save	<pre>for LRT, Pseudo-R2;</pre>	RUN;
* Compare th	nree-level empt	to two-le	vel empty;			
oficiest(fi	LFEWEI-FILZL, F	ICMOIE-FICS	L),			
ECHO "SPSS I	Model 1b: Empty	Means, Thr	ee-Level Mo	del for In	formation Test Outcom	ne".
MIXED info 1	BY PairID TwinI	ID				
/METHOD =	REML					
/PRINT =	SOLUTION TESTC	:00				
/RANDOM =	INTERCEPT CC	OVTYPE (UN) S	JBJECT (Pair	ID)		
/RANDOM =	INTERCEPT CC	OVTYPE (UN) S	JBJECT (Pair	ID*TwinID)		
* STATA Mod	lel 1b: Empty M	leans, Three	-Level Mode	l for Info. ed) ///	rmation Test Outcome	
MIXEd INIO	, TwinID: ,	covariance	(unstructur	ed) varian	ce reml	
estat	ic, n(351)		· ID ·			
estin	ates store Thr	eeLevel IV	iniD is sufficie	ent for level 2	r the first are posted within	nes the
lrtes	t ThreeLevel T	woLevel all	t whereas SA	s written arte	o pot	ule
г	imensions	1113	st, whereas SA		0 1101.	
Covariance Pa	rameters	3				
Columns in X		1				
Columns in Z	Per Subject	3				
Subjects		351 → now	number of t	win pairs (f	amilies)	
Max Obs Per S	ubject	8 → per	twin pair (4	4 occasions	* 2 persons)	
	. ·					
	Covarian	ice Parameter	Estimates	7		
Cov Parm	Subject	Estimate	Frror	Z Value	Pr > 7	
UN(1.1)	PairID	87.2970	9.9794	8.75	$<.0001 \rightarrow$ level-3 betwee	en-pair
UN(1,1)	PairID*TwinID	49.9360	5.3371	9.36	<.0001 → level-2 with	in-pair
Residual		23.9684	1.0735	22.33	<.0001 \rightarrow level-1 with:	in-person
	I	nformation Cr	iteria			
Neg2LogLike	Parms A	AIC AICC	HQIC	BIC	CAIC	
11278.1	3 11284	11284.1	11288.7	11295.7	11298.7	
	Solution T Stan	or Fixed Ette	CTS			
Effect	Estimate F	rror DF	t Value	Pr > t		
Intercept	25.2203 0.	6017 331	41.92	<.0001		
						1.10
Likelihood Ba	ntio Test for Fit	21 vs. Fit31	Is the 3-leve	el model a be	tter fit than the 2-level mo	del?
Neg2	Log		$Yes, -2\Delta LL($	$(\sim I) = III.3/$, <i>p</i> < .001	
Name Lik	ce Parms	AIC	BIC Dev	Diff DFd	iff Pvalue	
Fit2L 1138	9.5 2	11393.5 11	402.6			
Fit3L 1127	8.1 3	11284.1 11	295.7 111	.373	1 0	
Proportion va	ariance at each lev	el:	CC _{L2} for time	within perso	on and pair =	
Total = 87.30	+49.94 + 23.97 = 1	161.20	87.30 + 49.94)	/(161.20) =	.85	
Level 3 (pair)	= 87.30 / 161.2	0 = .54	CC- for nor	on within no	ir = 87.30 / (87.30 + 40.04)	- 64
Level 2 (perso	(n) = 49.94 / 161.20	0=.31	CC_{L3} for pers	is significant	$\mathbf{u} = 0/.30/(0/.30 + 49.94)$	04
Level 1 (time)	i = 23.97 / 161.2	0 = .15		is significanti	y steater than 0 via 20LL	101 5- 18. 2-16161.

Now let's do the same thing for our time-varying predictor of age:

```
TITLE "SAS Age Model: Empty Means, Three-Level Model for Age Predictor";
PROC MIXED DATA=work.Example8a NOCLPRINT COVTEST NAMELEN=100 IC METHOD=REML;
       CLASS PairID TwinID;
      MODEL age = / SOLUTION DDFM=Satterthwaite;
      RANDOM INTERCEPT / TYPE=UN SUBJECT=PairID;
                                                              * Level 3:
       RANDOM INTERCEPT / TYPE=UN SUBJECT=PairID*TwinID;
                                                              * Level 2; RUN;
ECHO "SPSS Age Model: Empty Means, Three-Level Model for Age Predictor".
MIXED age BY PairID TwinID
  /METHOD = REML /PRINT = SOLUTION TESTCOV /FIXED =
  /RANDOM = INTERCEPT | COVTYPE(UN) SUBJECT(PairID)
  /RANDOM = INTERCEPT | COVTYPE(UN) SUBJECT(PairID*TwinID).
 * STATA Age Model: Empty Means, Three-Level Model for Age Predictor
             || PairID: , covariance(unstructured) ///
mixed age ,
             || TwinID: , covariance (unstructured) variance reml
                                                            Because there is no age variance at level 2, age
                       Covariance Parameter Estimates
                                                           will be a predictor at levels 1 and 3 only.
                                       Standard
                                                      Ζ
                                                             Pr > Z
Cov Parm
            Subject
                           Estimate
                                         Error
                                                  Value
            PairID
                             8.5256
                                        0.7193
                                                11.85
                                                             <.0001 level-3 between-pair = 63%
UN(1,1)
UN(1,1)
            PairID*TwinID
                               0
                                                                   level-2 within-pair = 0%
                                                   .
Residual
                             4.9682
                                        0.1693
                                                   29.35
                                                             <.0001 level-1 within-person = 37%
```

Below we create our predictors: level-1 (time-varying) age will be time-in-study (0=baseline), and level-3 (betweenpair) age will be baseline age centered at 85 years. This creates a clear demarcation of age at baseline as the crosssectional effect of age, and time-in-study as the longitudinal effect of age.

SAS Data Manipulation:

```
DATA work.Example8a; SET work.Example8a;
```

```
* Centering age at time 1 at 85 to use at level 3;
BFage85 = agew1 - 85; LABEL BFage85= "BFage85: Age at Time1 (0=85)";
* Within-person centering age at level-1 (VARIABLE-BASED CENTERING);
```

- time = age agew1; LABEL time= "time: Time Since Entry (0= Age Wave 1)";
- * Make string version of zygosity for easier output reading; IF zygosity=1 THEN zyg="MZ"; IF zygosity=2 THEN zyg="DZ";
- * Selecting only cases with complete data; IF NMISS(agew1, age, info)>0 THEN DELETE; RUN;

SPSS Data Manipulation:

- * Centering age at time 1 at 85 to use at level 3. COMPUTE BFage85 = agew1 - 85.
- * Within-person centering age at level-1 (VARIABLE-BASED CENTERING). COMPUTE time = age - agew1. VARIABLE LABELS BFage85 "BFage85: Age at Time1 (0=85)"
- time "time: Time Since Entry (0= Age Wave 1)".
 * Selecting only complete cases.

```
SELECT IF (NMISS(agew1, age, info)=0).
```

STATA Data Manipulation:

```
* Centering age at time 1 at 85 to use at level 3
gen BFage85 = agew1 - 85
label variable BFage85 "BFage85: Age at Time1 (0=85)"
```

- * Within person centering age at level-1 (VARIABLE-BASED CENTERING) gen time = age - agew1
- label variable time "time: Time since entry (0= Age Wave 1)"
 * Recode zygosity so 0=DZ, 1=MZ, will be treated as numeric
- gen zyg = zygosity-1
 * Selecting only cases with complete data
 egen nummiss = rowmiss(agew1 age, info)
 drop if nummiss>0

Model 1c: Saturated Means for Wave, Random Intercepts at Levels 2 and 3

Using SAS GLIMMIX instead of SAS MIXED to get a means plot directly



Model 2a: Fixed Quadratic Time, Random Intercepts at Levels 3 (Pair) and 2 (Twin)

Level 1: Info _{tij} = $\beta_{0ij} + \beta_{1ij} \left(Age_{tij} - PairAgel_j \right) + \beta_{2ij} \left(Age_{tij} - PairAgel_j \right)^2 + e_{tij}$	
Level 2:	
Intercept: $\beta_{0ij} = \delta_{00j} + U_{0ij}$	
Linear Time: $\beta_{1ij} = \delta_{10j}$	
Quadratic Time: $\beta_{2ij} = \delta_{20j}$	
Level 3:	
Intercept: $\delta_{00j} = \gamma_{000} + V_{00j}$	
Linear Time: $\delta_{10j} = \gamma_{100}$	
Quadratic Time: $\delta_{20j} = \gamma_{200}$	

```
TITLE "SAS Model 2a: Fixed Quadratic Time, Random Intercepts for Pair and Twin";
PROC MIXED DATA=work.Example8a NOCLPRINT COVTEST NAMELEN=100 IC METHOD=REML;
    CLASS PairID TwinID;
    MODEL info = time time*time / SOLUTION DDFM=Satterthwaite;
    RANDOM INTERCEPT / TYPE=UN SUBJECT=PairID; * Level 3;
    RANDOM INTERCEPT / TYPE=UN SUBJECT=PairID*TwinID; * Level 2;
    ODS OUTPUT InfoCrit=Fit_RI2_RI3 CovParms=CovFQuad; * Save for LRT, pseudo-R2; RUN;
* Pseudo-R2 for time;
%PseudoR2(Ncov=3, CovFewer=CovEmpty, CovMore=CovFQuad);
ECHO "SPSS Model 2a: Fixed Quadratic Time, Random Intercepts for Pair and Twin".
```

```
MIXED info BY PairID TwinID WITH time

/METHOD = REML /PRINT = SOLUTION TESTCOV /FIXED = time time*time

/RANDOM = INTERCEPT | COVTYPE(UN) SUBJECT(PairID)

/RANDOM = INTERCEPT | COVTYPE(UN) SUBJECT(PairID*TwinID).
```

	C	ovariance Pa	arameter	Estimates				
				Standard	Z			
Cov Parm	Subject	Est	imate	Error	Value	Pr > Z		
UN(1,1)	PairID	88	.0484	10.1556	8.67	<.0001		
UN(1,1)	PairID*Tw	inID 52	.9334	5.5159	9.60	<.0001		
Residual		21	.9701	0.9854	22.30	<.0001		
		Infor	mation Cr	iteria				
Neg2LogLike	Parms	AIC	AICC	HQIC	BIC	CA	IC	
11211.6	3	11217.6	11217.6	11222.2	11229.2	11232	.2	
	Sol	ution for F:	ixed Effe	cts				
		Standard				The le	evel-1 fixed	linear and
Effect	Estimate	Error	DF	t Value	Pr > t	quadra	atic effects of	of time
Intercept	26.1212	0.6233	369	41.91	<.0001	explai	ned 8.33% o	of the level-1
time	-0.3216	0.1834	1040	-1.75	0.0797	residu	al variance.	The level-2
time*time	-0.03673	0.03077	1027	-1.19	0.2329	twin i	ntercept vari	ance
						increa	sed as a con	sequence.
PsuedoR2 (%	Reduction)	for CovEmp	ty vs. Co	vFQuad				
Name	CovParm	Subject	E	stimate	StdErr	ZValue	ProbZ	PseudoR2
CovEmpty	UN(1,1)	PairID		87.2970	9.9794	8.75	<.0001	
CovEmpty	UN(1,1)	PairID*Tw:	inID	49.9360	5.3371	9.36	<.0001	
CovEmpty	Residual			23.9684	1.0735	22.33	<.0001	
CovFQuad	UN(1,1)	PairID		88.0484	10.1556	8.67	<.0001	-0.008607
CovFQuad	UN(1,1)	PairID*Tw:	inID	52.9334	5.5159	9.60	<.0001	-0.060025
CovFQuad	Residual			21.9701	0.9854	22.30	<.0001	0.083373

Model 2b: Fixed Quadratic Time, Random Linear Time Slope at Level 2

Level 1: $Info_{tij} = f$	$\beta_{0ij} + \beta_{1ij} \left(Age_{tij} - PairAgel_j \right) + \beta_{2ij} \left(Age_{tij} - PairAgel_j \right)^2 + e_{tij}$
Level 2:	
Intercept:	$\beta_{0ij} = \delta_{00j} + U_{0ij}$
Linear Time:	$\beta_{1ij} = \delta_{10j} + U_{1ij}$
Quadratic Time:	$\beta_{2ij} = \delta_{20j}$
Level 3:	
Intercept:	$\delta_{00j} = \gamma_{000} + V_{00j}$
Linear Time:	$\delta_{10j} = \gamma_{100}$
Quadratic Time:	$\delta_{20j} = \gamma_{200}$

TITLE "SAS Model 2b: Add Random Linear Time for Twin";
PROC MIXED DATA=work.Example8a NOCLPRINT COVTEST NAMELEN=100 IC METHOD=REML;
 CLASS PairID TwinID;
 MODEL info = time time*time / SOLUTION DDFM=Satterthwaite;
 RANDOM INTERCEPT / TYPE=UN SUBJECT=PairID; * Level 3;
 RANDOM INTERCEPT time / TYPE=UN SUBJECT=PairID*TwinID; * Level 2;
 ODS OUTPUT InfoCrit=Fit_RL2_RI3; * Save for LRT, pseudo-R2; RUN;
* Test random linear time at level 2;
%FitTest(FitFewer=Fit_RI2_RI3, FitMore=Fit_RL2_RI3);

```
ECHO "SPSS Model 2b: Add Random Linear Time for Twin".
MIXED info BY PairID TwinID WITH time
  /METHOD = REML /PRINT = SOLUTION TESTCOV /FIXED = time time*time
  /RANDOM = INTERCEPT
                              | COVTYPE (UN) SUBJECT (PairID)
  /RANDOM = INTERCEPT time | COVTYPE(UN) SUBJECT(PairID*TwinID).
* STATA Model 2b: Add Random Linear Time for Twin
mixed info c.time c.time#c.time , || PairID: , covariance(unstructured) ///
        || TwinID: time , covariance(unstructured) variance reml
       estat ic, n(351)
       estimates store RL2 RI3
       lrtest RI2_RI3_RL2_RL3
                     Covariance Parameter Estimates
                                           Standard
                                                            Ζ
Cov Parm
             Subject
                               Estimate
                                              Error
                                                        Value
                                                                     Pr 7
             PairID
                                             9.7835
                                                         8.77
                                                                    <.0001 \rightarrow level-3 intercept var
UN(1,1)
                                85.7639
                                                                    <.0001 \rightarrow level-2 intercept var
UN(1,1)
             PairID*TwinID
                                47.6649
                                             5.2082
                                                         9.15
                                                                    0.0596 \rightarrow level-2 int-linear cov
UN(2,1)
             PairID*TwinID
                                1.6668
                                             0.8848
                                                         1.88
             PairID*TwinID
                                1.5662
                                             0.2151
                                                         7.28
                                                                    <.0001 \rightarrow level-2 linear time var
UN(2,2)
Residual
                                13.5083
                                             0.8175
                                                        16.52
                                                                    <.0001 \rightarrow level-1 residual var
                            Information Criteria
Neg2LogLike
               Parms
                            AIC
                                       AICC
                                                  HQIC
                                                               BIC
                                                                         CAIC
    11075.1
                        11085.1
                                    11085.1
                   5
                                               11092.7
                                                          11104.4
                                                                      11109.4
                   Solution for Fixed Effects
                         Standard
Effect
             Estimate
                            Error
                                        DF
                                              t Value
                                                         Pr > |t|
Intercept
              26.1799
                           0.5991
                                       338
                                                43.70
                                                           <.0001
time
              -0.3147
                           0.1583
                                       929
                                                -1.99
                                                           0.0471
             -0.07075
                          0.02571
                                       722
                                                -2.75
                                                           0.0061
time*time
                                                          Do we need the random linear time slope for twin?
Likelihood Ratio Test for Fit_RI2_RI3 vs. Fit_RL2_RI3
                                                          Yes, -2\Delta LL(\sim 2) = 136.52, p < .001
               Neg2Log
                                                          DevDiff
   Name
                Like
                           Parms
                                        AIC
                                                   BIC
                                                                      DFdiff
                                                                                Pvalue
Fit_RI2_RI3
               11211.6
                             3
                                    11217.6
                                               11229.2
                                                                         2
                                                                                   0
Fit RL2 RI3
               11075.1
                             5
                                    11085.1
                                               11104.4
                                                           136.518
```

Model 2c: Fixed Quadratic, Random Linear Slope at Levels 2 and 3

```
Level 1: Info_{tij} = \beta_{0ij} + \beta_{1ij} (Age_{tij} - PairAgel_j) + \beta_{2ij} (Age_{tij} - PairAgel_j)^2 + e_{tij}
Level 2:
                         \beta_{0ii} = \delta_{00i} + U_{0ii}
  Intercept:
                        \beta_{1ij} = \delta_{10j} + U_{1ij}
  Linear Time:
   Quadratic Time: \beta_{2ij} = \delta_{20j}
Level 3:
   Intercept:
                         \delta_{00i} = \gamma_{000} + V_{00i}
                         \delta_{10\,i} = \gamma_{100} + V_{10\,j}
   Linear Time:
   Quadratic Time: \delta_{20i} = \gamma_{200}
TITLE "SAS Model 2c: Add Random Linear Time for Pair";
PROC MIXED DATA=work.Example8a NOCLPRINT COVTEST NAMELEN=100 IC METHOD=REML;
         CLASS PairID TwinID;
```

```
MODEL info = time time*time / SOLUTION DDFM=Satterthwaite;
RANDOM INTERCEPT time / TYPE=UN SUBJECT=PairID; * Level 3;
RANDOM INTERCEPT time / TYPE=UN SUBJECT=PairID*TwinID; * Level 2;
ODS OUTPUT InfoCrit=Fit_RL2_RL3; * Save for LRT, pseudo-R2; RUN;
* Test random linear time at level 3;
```

```
%FitTest(FitFewer=Fit_RL2_RI3, FitMore=Fit_RL2_RL3);
```

ECHO "SPSS	ECHO "SPSS Model 2c: Add Random Linear Time for Pair".									
MIXED info BY PairID TwinID WITH time										
/METHOD =	= REML /PI	RINT = SOLU	JTION TE	STCOV /FI	XED = time	e time*tim	e			
/RANDOM =	= INTERCEPT	r time C	OVTYPE (U	N) SUBJECT	(PairID)					
/RANDOM =	= INTERCEPT	r time Co	OVTYPE (U	N) SUBJECT	(PairID*Tw	vinID).				
* 57777 Moo		d Bandom I	incar Ti	mo for Pai	-					
mixed info	c time c t	time#c time		airTD: tim	⊥ e. covaria	nce (unstr	uctured) ///		
T	winID: tim	ne , covari	ance (un:	structured)	variance	reml	uoouzeu	, , , ,		
esta	t ic, n(35	51)								
esti	mates stor	e RL2 RL3			ICC ₁₂ for	correlation	of twins v	vithin nairs.		
lrtest RL2 RL3 RL2 RI3 For Intercent = $85.40 / (85.40 + 47.80) = 64$										
					For Linear	Time = 0.1	1/(011	(-1.45) = .07		
	Co	variance Pa	rameter E	Estimates	I of Efficar	Time = 0.1	17(0.11	(1.43) = .07 (100)		
			5	Standard	Z					
Cov Parm	Subject	Esti	mate	Error	Value	Pr Z				
UN(1,1)	PairID	85.	4911	9.8263	8.70	<.0001 →	level-3	intercept var		
UN(2,1)	PairID	0.	2432	1.0615	0.23	0.8188 →	level-3	int-linear cov		
UN(2,2)	PairID	0.	1066	0.2203	0.48	0.3143 →	level-3	linear time var		
UN(1,1)	PairID*Twi	nID 47.	7968	5.2453	9.11	<.0001 →	level-2	intercept var		
UN(2,1)	PairID*Twi	nID 1.	5559	0.9849	1.58	0.1142 →	level-2	int-linear cov		
UN(2,2)	PairID*Twi	nID 1.	4534	0.3050	4.77	<.0001 →	level-2	linear time var		
Residual		13.	5251	0.8191	16.51	<.0001 →	level-1	residual var		
		Inform	ation Cri	iteria						
Neg2LogLike	Parms	AIC	AICC	HQIC	BIC	CAIC				
11074.8	7	11088.8	11088.8	11099.5	11115.8	11122.8				
	Solu	tion for Fi	xed Effec	cts						
		Standard								
Effect	Estimate	Error	DF	t Value	Pr > t					
Intercept	26.1810	0.5987	336	43.73	<.0001					
time	-0.3181	0.1589	860	-2.00	0.0455					
time*time	-0.07055	0.02573	721	-2.74	0.0062					
					Do we nee	d the rando	m linear s	slope for pair, too?		
Likelihood Ratio Test for Fit_RL2_RI3 vs. Fit_RL2_RL3 Neg2Log				Nope, -2Δ	$LL(\sim 2) = 0.2$	29, p = .80	5			
Name	Like	Parms	AIC	BIC	DevDiff	DFdiff	Pval	ue		
Fit_RL2_RI3	11075.1	5	11085.1	11104.4						
Fit BI2 BI3	11074 8	7	11088 8	11115 8	0 20080	2	0 864	68		

I then tested random quadratic time slopes at the twin and pair levels, but neither was significant. Given our interest in examining heritability of intercept and time slopes, we will retain the nonsignificant random linear time slope at level 3 (pairs) for now. So we continue by adding level-3 baseline age as a predictor of intercept and linear slope differences.

Model 3a: Add Baseline Age as a Predictor of Pair-Level Intercept and Time Slope Differences

```
Level 1: Info_{tij} = \beta_{0ij} + \beta_{1ij} (Age_{tij} - PairAgel_j) + \beta_{2ij} (Age_{tij} - PairAgel_j)^2 + e_{tij}

Level 2:

Intercept: \beta_{0ij} = \delta_{00j} + U_{0ij}

Linear Time: \beta_{1ij} = \delta_{10j} + U_{1ij}

Quadratic Time: \beta_{2ij} = \delta_{20j}

Level 3:

Intercept: \delta_{00j} = \gamma_{000} + \gamma_{001} (PairAgel_j - 85) + V_{00j}

Linear Time: \delta_{10j} = \gamma_{100} + \gamma_{101} (PairAgel_j - 85) + V_{10j}

Quadratic Time: \delta_{20j} = \gamma_{200}
```

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```
TITLE "SAS Model 3a: Add Baseline Age as Predictor of Pair Intercepts and Linear Time Slopes";
PROC MIXED DATA=work.Example8a NOCLPRINT COVTEST NAMELEN=100 IC METHOD=REML;
       CLASS PairID TwinID;
       MODEL info = time time *time BFage85 time *BFage85 / SOLUTION DDFM=Satterthwaite;
       RANDOM INTERCEPT time / TYPE=UN SUBJECT=PairID;
                                                                     * Level 3;
       RANDOM INTERCEPT time / TYPE=UN SUBJECT=PairID*TwinID; * Level 2;
       CONTRAST "Trajectory Diffs by Age" BFage85 1, time*Bfage85 1 / CHISQ;
       ODS OUTPUT InfoCrit=Fit_Age CovParms=Cov_Age; * Save for LRT, pseudo-R2; RUN;
* Pseudo-R2 for age; % PseudoR2 (Ncov=7, CovFewer=Cov_RL2_RL3, CovMore=Cov_Age);
ECHO "SPSS Model 3a: Add Baseline Age as Predictor of Pair Intercepts and Linear Time Slopes".
MIXED info BY PairID TwinID WITH BFage85 time
  /METHOD = REML /PRINT = SOLUTION TESTCOV /FIXED = time time*time BFage85 time*BFage85
  /RANDOM = INTERCEPT time | COVTYPE(UN) SUBJECT(PairID)
  /RANDOM = INTERCEPT time | COVTYPE(UN) SUBJECT(PairID*TwinID)
  /TEST = "Trajectory Diffs by Age" BFage85 1; time*Bfage85 1.
* STATA Model 3a: Add Baseline Age as Predictor of Pair Intercepts and Linear Time Slopes
mixed info c.time c.time#c.time c.BFage85 c.time#c.BFage85, ///
       || PairID: time, covariance(unstructured) ///
       || TwinID: time, covariance (unstructured) variance reml
       estat ic, n(351)
       test (c.BFage85=0) (c.time#c.BFage85=0) // Trajectory diffs by age
                     Covariance Parameter Estimates
                                          Standard
                                                           Ζ
Cov Parm
             Subject
                              Estimate
                                             Frror
                                                       Value
                                                                    Pr 7
                               78.7908
                                            9.3017
                                                        8.47
                                                                  <.0001
UN(1,1)
             PairID
UN(2,1)
             PairID
                              -0.02415
                                            1.0154
                                                       -0.02
                                                                  0.9810
UN(2,2)
             PairID
                               0.07234
                                            0.2193
                                                        0.33
                                                                  0.3707
             PairID*TwinID
                               47,6089
                                            5.2158
                                                        9.13
                                                                  <.0001
UN(1,1)
             PairID*TwinID
                                                        1.70
                                1.6686
                                            0.9812
                                                                  0.0890
UN(2,1)
UN(2,2)
             PairID*TwinID
                                1.4534
                                            0.3052
                                                        4.76
                                                                  <.0001
                                            0.8236
                                                       16.48
                                                                  <.0001
Residual
                               13.5712
                            Information Criteria
                                     AICC
                            AIC
Neg2LogLike
              Parms
                                                 HOTC
                                                             BIC
                                                                       CATC
    11056.3
                        11070.3
                                   11070.4
                                              11081.1
                                                         11097.4
                                                                    11104.4
                   7
                    Solution for Fixed Effects
                            Standard
                                                                      The level-3 main effect of age and its
                                                           Pr > |t|
                               Frror
                                          DF
                                                t Value
Effect
                Estimate
                                                                      interaction with time explained 7.84%
                                                             <.0001
                              0.6473
                                         345
Intercept
                 24.8887
                                                  38.45
                                                                      and 32.11% of the level-3 pair intercept
                              0.1681
                                         892
                                                  -2.55
                                                             0.0110
time
                 -0.4284
                                                                      and time slope variance, respectively. I
time*time
                -0.07124
                             0.02580
                                         717
                                                  -2.76
                                                             0.0059
                                                                      also tried quadratic effects of age in
                             0.1864
                                         348
                                                  -4.61
                                                             <.0001
BFage85
                 -0.8602
                                                                      predicting the intercept and linear time
                                                             0.0683
time*BFage85
                -0.05655
                             0.03089
                                         267
                                                  -1.83
                                                                      slope, but neither was significant.
                                        Contrasts
                            Num
                                    Den
                                     DF
                                           Chi-Square
                                                                                    Pr > F
Label
                             DF
                                                         F Value
                                                                      Pr > ChiSq
Trajectory Diffs by Age
                              2
                                    302
                                                25.80
                                                           12.90
                                                                          <.0001
                                                                                    <.0001
PsuedoR2 (% Reduction) for Cov_RL2_RL3 vs. Cov_Age
Name
              CovParm
                           Subject
                                            Estimate
                                                          StdErr
                                                                    7Value
                                                                               Prob7
                                                                                        Pseudo<sub>R2</sub>
Cov RL2 RL3
              UN(1,1)
                           PairID
                                             85.4911
                                                          9.8263
                                                                      8.70
                                                                              <.0001
Cov RL2 RL3
                           PairID
                                              0.1066
                                                          0.2203
                                                                      0.48
                                                                              0.3143
              UN(2,2)
Cov_RL2_RL3
                                             47,7968
                                                                      9.11
                                                                              <.0001
              UN(1,1)
                           PairID*TwinID
                                                          5.2453
                                                                      4.77
Cov RL2 RL3
              UN(2,2)
                           PairID*TwinID
                                              1.4534
                                                          0.3050
                                                                              <.0001
Cov RL2 RL3
              Residual
                                             13.5251
                                                          0.8191
                                                                     16.51
                                                                              <.0001
Cov_Age
              UN(1,1)
                           PairID
                                             78.7908
                                                          9.3017
                                                                      8.47
                                                                              <.0001
                                                                                         0.07837
                                                                      0.33
                           PairID
                                             0.07234
                                                          0.2193
                                                                              0.3707
                                                                                         0.32109
Cov_Age
              UN(2,2)
                                             47.6089
                                                                      9.13
                                                                              <.0001
                                                                                         0.00393
Cov_Age
              UN(1,1)
                           PairID*TwinID
                                                          5.2158
               UN(2,2)
                           PairID*TwinID
                                              1.4534
                                                          0.3052
                                                                      4.76
                                                                              <.0001
                                                                                        -0.00003
Cov Age
               Residual
                                             13.5712
                                                          0.8236
                                                                     16.48
                                                                              <.0001
                                                                                        -0.00340
Cov_Age
```

```
Model 3b: Add Zygosity as a Predictor of Pair-Level Intercept and Time Slope Differences
```

```
Level 1: Info_{tii} = \beta_{0ii} + \beta_{1ii} (Age_{tii} - PairAgel_i) + \beta_{2ii} (Age_{tii} - PairAgel_i)^2 + e_{tii}
Level 2:
                    \beta_{0ii} = \delta_{00i} + U_{0ii}
  Intercept:
  Linear Time:
                   \beta_{111} = \delta_{101} + U_{111}
  Quadratic Time: \beta_{2ij} = \delta_{20j}
Level 3:
                    \delta_{00j} = \gamma_{000} + \gamma_{001} \left( \text{PairAgel}_{j} - 85 \right) + \gamma_{002} \left( \text{MZvDZ}_{j} \right) + \gamma_{003} \left( \text{PairAgel}_{j} - 85 \right) \left( \text{MZvDZ}_{j} \right) + V_{00j}
  Intercept:
                    \delta_{10j} = \gamma_{100} + \gamma_{101} (PairAgel_j - 85) + \gamma_{102} (MZvDZ_j) + \gamma_{103} (PairAgel_j - 85) (MZvDZ_j) + V_{10j}
  Linear Time:
  Ouadratic Time: \delta_{20i} = \gamma_{200}
TITLE "SAS Model 3b: Add Zygosity as Predictor of Pair Intercepts and Linear Time Slopes";
PROC MIXED DATA=work.Example8a NOCLPRINT COVTEST NAMELEN=100 IC METHOD=REML;
        CLASS PairID TwinID zyg;
       MODEL info = time time*time BFage85 time*BFage85
                       zyg zyg*time zyg*BFage85 zyg*time*BFage85 / SOLUTION DDFM=Satterthwaite;
       RANDOM INTERCEPT time / TYPE=UN SUBJECT=PairID;
                                                                             * Level 3;
        RANDOM INTERCEPT time / TYPE=UN SUBJECT=PairID*TwinID; * Level 2;
CONTRAST "Diffs by Zyg" zyg -1 1, time*zyg -1 1, BFage85*zyg -1 1, time*BFage85*zyg -1 1 / CHISQ;
ODS OUTPUT InfoCrit=Fit Zyg CovParms=Cov Zyg; * Save for LRT, pseudo-R2; RUN;
* Pseudo-R2 for zygosity;
%PseudoR2(Ncov=7, CovFewer=Cov_Age, CovMore=Cov_Zyg);
ECHO "SPSS Model 3b: Add Zygosity as Predictor of Pair Intercepts and Linear Time Slopes".
MIXED info BY PairID TwinID zyg WITH BFage85 time
  /METHOD = REML /PRINT = SOLUTION TESTCOV
  /FIXED = time time *time BFage85 time *BFage85 zyg zyg *time zyg *BFage85 zyg *time *BFage85
  /RANDOM = INTERCEPT time | COVTYPE (UN) SUBJECT (PairID)
  /RANDOM = INTERCEPT time | COVTYPE(UN) SUBJECT(PairID*TwinID)
  /TEST = "Diffs by Zyg" zyg -1 1; time*zyg -1 1; BFage85*zyg -1 1; time*BFage85*zyg -1 1.
* STATA Model 3b: Add Zygosity as Predictor of Pair Intercepts and Linear Time Slopes
mixed info c.time c.time#c.time c.BFage85 c.time#c.BFage85 ///
            c.zyg c.zyg#c.time c.zyg#c.BFage85 c.zyg#c.time#c.BFage85, ///
     || PairID: time, covariance(unstructured) ///
     || TwinID: time, covariance (unstructured) variance reml
        estat ic, n(351) // Trajectory diffs by zygosity
        test (c.zyg=0) (c.zyg#c.time=0) (c.zyg#c.BFage85=0) (c.zyg#c.time#c.BFage85=0)
        estimates store Fit Zyg
                      Covariance Parameter Estimates
                                            Standard
                                                              Ζ
Cov Parm
             Subject
                               Estimate
                                               Error
                                                          Value
                                                                        Pr Z
             PairID
                                              9.2255
                                                           8.34
                                                                      <.0001
UN(1,1)
                                76,9815
             PairID
UN(2,1)
                                 0.1952
                                              1.0214
                                                           0.19
                                                                      0.8484
UN(2,2)
             PairID
                                 0.07385
                                              0.2177
                                                           0.34
                                                                      0.3672
UN(1,1)
             PairID*TwinID
                                 47.8176
                                              5.2339
                                                           9.14
                                                                      <.0001
             PairID*TwinID
                                 1.6538
                                              0.9833
                                                           1.68
                                                                     0.0926
UN(2,1)
             PairID*TwinID
                                              0.3021
UN(2,2)
                                 1.4464
                                                           4.79
                                                                      <.0001
Residual
                                 13.5287
                                              0.8181
                                                          16.54
                                                                      <.0001
                             Information Criteria
Neg2LogLike
               Parms
                             AIC
                                        AICC
                                                   HQIC
                                                                BIC
                                                                           CAIC
    11048.7
                   7
                         11062.7
                                     11062.7
                                                11073.4
                                                            11089.7
                                                                        11096.7
                                             Contrasts
                                   Num
                                           Den
Label
                                    DF
                                            DF
                                                  Chi-Square
                                                                 F Value
                                                                               Pr > ChiSq
                                                                                              Pr > F
```

Trajectory Diffs by Zygosity

4

276

11.30

2.83

0.0234

0.0253

			Solution for	Fixed Effects				
				Standard				
Effect		zyg	g Estimate	Error	DF t	Value	Pr > t	
Intercept			26.2390	0.9772	327	26.85	<.0001	
time			-0.3668	0.2039	646	-1.80	0.0724	
time*time			-0.07171	0.02577	720	-2.78	0.0055	
BFage85			-1.0161	0.2820	328	-3.60	0.0004	
time*BFag	e85		0.01414	0.04557	212	0.31	0.7566	
zyg		DZ	-2.3236	1.2924	333	-1.80	0.0731	
zyg		ΜZ	0				· [
time*zyg		DZ	-0.1225	0.2061	262	-0.59	0.5529	The level-3 main effect
time*zyg		ΜZ	0					of zygosity explained
BFage85*z	уg	DZ	0.2774	0.3737	341	0.74	0.4584	2.61% of the level-3 pair
BFage85*z	уg	ΜZ	0					intercept variance, but
time*BFag	e85*zyg	DZ	-0.1308	0.06181	257	-2.12	0.0352	zygosity by time actually
time*BFag	e85*zyg	ΜZ	0					increased the level-3 pair
								slope variance instead.
PsuedoR2	(% Reducti	on)	for Cov_Age vs	. Cov_Zyg			L	
Name	CovParm		Subject	Estimate	StdErr	ZValue	ProbZ	PseudoR2
Cov_Age	UN(1,1)		PairID	78.7908	9.3017	8.47	<.0001	
Cov_Age	UN(2,2)		PairID	0.07234	0.2193	0.33	0.3707	
Cov_Age	UN(1,1)		PairID*TwinID	47.6089	5.2158	9.13	<.0001	
Cov_Age	UN(2,2)		PairID*TwinID	1.4534	0.3052	4.76	<.0001	
Cov_Age	Residual			13.5712	0.8236	16.48	<.0001	
Cov_Zyg	UN(1,1)		PairID	76.7361	9.2038	8.34	<.0001	0.026078
Cov_Zyg	UN(2,2)		PairID	0.07387	0.2196	0.34	0.3683	-0.021145
Cov_Zyg	UN(1,1)		PairID*TwinID	47.8637	5.2448	9.13	<.0001	-0.005352
Cov_Zyg	UN(2,2)		PairID*TwinID	1.4538	0.3048	4.77	<.0001	-0.000289
Cov_Zyg	Residual			13.5682	0.8232	16.48	<.0001	0.000220

Model 3c: Add Heterogeneous Variances by Zygosity (to quantify heritability)

Note: SPSS and STATA versions each required extra dummy codes for MZ and DZ to be used in the variance model. SPSS version does not have heterogeneous residual variances (I could not get the code to work like it should have).

```
TITLE "SAS Model 3c: Add Heterogeneous G and R matrices by Zygosity";
PROC MIXED DATA=work.Example8a NOCLPRINT COVTEST NAMELEN=100 IC METHOD=REML;
      CLASS PairID TwinID zyg;
      MODEL info = time time*time BFage85 time*BFage85
                   zyg zyg*time zyg*BFage85 zyg*time*BFage85 / SOLUTION DDFM=Satterthwaite;
      RANDOM INTERCEPT time / TYPE=UN SUBJECT=PairID GROUP=zyg;
                                                                  * Level 3;
      RANDOM INTERCEPT time / TYPE=UN SUBJECT=PairID*TwinID GROUP=zyg; * Level 2;
      REPEATED / GROUP=zyg;
      ODS OUTPUT InfoCrit=Fit Het CovParms=Cov Het; * Save for LRT, pseudo-R2;
      ESTIMATE "Age on Intercept: DZ" BFage85 1 BFage85*zyg 1 0;
      ESTIMATE "Age on Time Slope: DZ" time*BFage85 1 time*BFage85*zyg 1 0; RUN;
* Test het variances;
%FitTest(FitFewer=Fit_Zyg, FitMore=Fit_Het);
ECHO "SPSS Model 3c: Add Heterogeneous G and R matrices by Zygosity".
MIXED info BY PairID TwinID zyg WITH BFage85 time MZ DZ
  /METHOD = REML /PRINT = SOLUTION TESTCOV
  /FIXED = time time *time BFage85 time *BFage85 zyg zyg *time zyg *BFage85 zyg *time *BFage85
  /RANDOM = MZ MZ*time | COVTYPE(UN) SUBJECT(PairID)
  /RANDOM = DZ DZ*time | COVTYPE(UN) SUBJECT(PairID)
  /RANDOM = MZ MZ*time | COVTYPE(UN) SUBJECT(PairID*TwinID)
  /RANDOM = DZ DZ*time | COVTYPE(UN) SUBJECT(PairID*TwinID)
  /TEST "Age on Intercept: DZ" BFage85 1 BFage85*zyg 1 0
  /TEST "Age on Time Slope: DZ" time*BFage85 1 time*BFage85*zyg 1 0.
* STATA Model 3c: Add Heterogeneous G and R matrices by Zygosity
mixed info c.time c.time#c.time c.BFage85 c.time#c.BFage85 ///
          c.zyg c.zyg#c.time c.zyg#c.BFage85 c.zyg#c.time#c.BFage85, ///
       || PairID: mz mztime, noconstant covariance(unstructured) ///
       || PairID: dz dztime, noconstant covariance (unstructured) ///
```

```
|| TwinID: mz mztime, noconstant covariance(unstructured) ///
|| TwinID: dz dztime, noconstant covariance(unstructured) ///
variance reml residuals(independent,by(zyg))
estat ic, n(351)
lincom c.BFage85*1 + c.zyg#c.BFage85*1 // Age on Intercept: DZ
lincom c.time#c.BFage85*1 + c.zyg#c.time#c.BFage85*1 // Age on Time Slope: DZ
estimates store Fit_Het
lrtest Fit_Het Fit_Zyg
```

Covariance Parameter Estimates

				Standard	Z	
Cov Parm	Subject	Group	Estimate	Error	Value	Pr Z
UN(1,1)	PairID	zyg DZ	55.0442	11.8158	4.66	<.0001
UN(2,1)	PairID	zyg DZ	-0.4171	1.3047	-0.32	0.7492
UN(2,2)	PairID	zyg DZ	0			
UN(1,1)	PairID	zyg MZ	105.88	15.0698	7.03	<.0001
UN(2,1)	PairID	zyg MZ	0.9788	1.7090	0.57	0.5668
UN(2,2)	PairID	zyg MZ	0.6152	0.3648	1.69	0.0459
UN(1,1)	PairID*TwinID	zyg DZ	70.8603	9.5620	7.41	<.0001
UN(2,1)	PairID*TwinID	zyg DZ	2.4174	1.3398	1.80	0.0712
UN(2,2)	PairID*TwinID	zyg DZ	1.1609	0.2462	4.71	<.0001
UN(1,1)	PairID*TwinID	zyg MZ	18.5869	4.0696	4.57	<.0001
UN(2,1)	PairID*TwinID	zyg MZ	0.4866	1.0519	0.46	0.6436
UN(2,2)	PairID*TwinID	zyg MZ	1.3806	0.4153	3.32	0.0004
Residual		zyg DZ	13.9688	1.1309	12.35	<.0001
Residual		zyg MZ	12.9889	1.1721	11.08	<.0001

	Information Criteria								
Neg2LogLike	Parms	AIC	AICC	HQIC	BIC	CAIC			
11005.0	13	11031.0	11031.2	11051.0	11081.2	11094.2			

Solution for Fixed Effects						
			Standard			
Effect	zyg	Estimate	Error	DF	t Value	Pr > t
Intercept		26.1032	1.0277	139	25.40	<.0001
time		-0.3426	0.2169	289	-1.58	0.1154
time*time		-0.07051	0.02570	722	-2.74	0.0062
BFage85		-1.0285	0.2963	139	-3.47	0.0007
time*BFage85		0.03232	0.05169	102	0.63	0.5332
zyg	DZ	-2.1640	1.3125	289	-1.65	0.1003
zyg	MZ	0				
time*zyg	DZ	-0.1410	0.2154	228	-0.65	0.5135
time*zyg	MZ	0				
BFage85*zyg	DZ	0.2888	0.3799	295	0.76	0.4477
BFage85*zyg	MZ	0				
time*BFage85*zyg	DZ	-0.1515	0.06481	221	-2.34	0.0203
time*BFage85*zyg	MZ	0				

Estimates								
Standard								
Label	Estimate	Error	DF	t Value	Pr > t			
Age on Intercept: DZ	-0.7397	0.2378	212	-3.11	0.0021			
Age on Time Slope: DZ	-0.1192	0.03919	236	-3.04	0.0026			

Likelihood	Ratio Test Neg2Log	for Fit_	_Zyg vs. Fit_	Het	Is the Yes, -	e heterogen −2∆LL(7) =	eous varian 43.66, p < .	ce model a bet 001 (note SAS d	ter fit? lidn't count the 0)
Name	Like	Parms	AIC	BI	С	DevDiff	DFdiff	Pvalue	
Fit_Zyg	11048.7	7	11062.7	11089.	7				
Fit_Het	11005.0	13	11031.0	11081.	2	43.6599	6	8.6337E-8	

Heritability (A or H²), or the contribution of genetics, can be found as twice the difference of the intraclass correlation (ICC) between MZ and DZ twins. **Common environment** (C²) can be found as the difference between the ICC for MZ twins and the heritability estimate (usually constrained to be ≥ 0), and the **unique environment** (E²) can be found as the remainder (i.e., 1 – [heritability + common environment]). Applying these calculations to our results reveals evidence for heritability in both the intercept and the linear time slope, but with much greater uncertainty in the latter.

	Intercept			Linea	Linear Time Slope		
Intercept	DZ	MZ	HCE	DZ	MZ	HCE	
Level-3 Pair Variance	55.044	105.880		0.000	0.615		
Level-2 Twin Variance	70.860	18.587		1.161	1.381		
ICC = L3 / (L3 + L2)	0.437	0.851		0.000	0.308		
$H^2 = 2*(ICC MZ - ICC DZ)$			0.827			0.616	
$C^2 = ICC MZ - H^2$			0.024			-0.308	
$E^2 = 1 - (H^2 + C^2)$			0.149			0.692	

Sample Results Section:

The extent of individual change in crystallized intelligence (as measured by the information test) and the extent of heritability therein was examined in a sample of 351 same-sex twin pairs measured every two years for up to four occasions. Multilevel models were estimated using residual maximum likelihood in SAS MIXED. Accordingly, the significance of fixed effects was evaluated with Wald tests using Satterthwaite denominator degrees of freedom, whereas the significance of random effects was evaluated via likelihood ratio tests (i.e., $-2\Delta LL$ with degrees of freedom equal to the number of new random effects variances and covariances). Pseudo-R² effect sizes for the fixed effects were calculated as the proportion reduction in each variance component.

A two-level empty means, random intercept model of occasions at level 1 nested in persons at level 2 was initially estimated; its intraclass correlation (ICC) indicated that 83% of the outcome variance was between persons. The addition of a level-3 random intercept for twin pair resulted in significantly better model fit, $-2\Delta LL(1) = 111.37$, p < .001, and revealed that, of 85% of the outcome variance that was between persons, 64% was actually due to twin pair (i.e., shared variance between twins). Stated more directly, of the total variance, 15% was at level 1 (within persons over time), 31% was at level 2 (between twins), and 54% was at level 3 (between pairs). A three-level empty means, random intercept model to partition the variance in time-varying age revealed that 63% was between pairs (given that the twins varied in age from 80 to 100 at baseline), whereas the remaining 37% was within persons over time; there was no level-2 age variance in these twins. Thus, the level-3 (cross-sectional) and level-1 (longitudinal) effects of age were modeled separately using baseline age (centered so 0 = 85) and time in study (with 0 = baseline), respectively.

Based on the pattern of model-estimated means, fixed linear and quadratic effects of time were first added, which accounted for 8.33% of the level-1 residual variance. Although adding a variance for the level-2 (twin) random linear time slope (and its covariance with the level-2 twin intercept) significantly improved model fit, $-2\Delta LL(2) = 136.52$, p < .001, the subsequent addition of a variance for the level-3 (pair) random linear time slope (and its covariance with the level-3 pair intercept) did not significantly improve model fit, $-2\Delta LL(2) = 0.29$, p = .86, indicating that the 7% of the random linear time slope variance that was due to twin pair was not distinguishable from 0. Given our interest in examining heritability, though, both random linear time slope variances were retained. Random quadratic time slopes were not significant at either level 2 or level 3, and these were not retained.

The effect of baseline age on the intercept and linear time slope was then added, which explained 7.84% and 32.11% of the level-3 intercept and linear time slope variance, respectively, and which resulted in significant model improvement, F(2,302) = 12.90, p < .001. We then added zygosity mean differences in the intercept, linear time slope, and the effects of baseline age on the intercept and linear time slope. Although these four new fixed effects also resulted in significant model improvement, F(4,276) = 2.83, p < .001, only the level-3 pair intercept variance was reduced (by 2.61%); the level-3 pair time slope variance increased by 2.11% instead. Finally, we added zygosity differences in all variance model parameters—three at level 3, three at level 2, and in residual variance at level 1, which resulted in significant model improvement, $-2\Delta LL(7) = 43.66$, p < .001.

Results for the final model are given in Table X. Given the centering of the model predictors, the reference for the intercept and linear time slope is an MZ twin pair who were 85 years at baseline (when time = 0). Older age at baseline was related to a significantly lower intercept at time 0, equivalently so in both MZ and DZ twins. In contrast, the interaction of age by linear time differed significantly by zygosity: older age at baseline was related to a significantly more negative linear time slope in DZ twins, but not in MZ twins (in which the interaction of age by time was nonsignificantly positive instead). There was also a significant fixed quadratic effect of time, which indicated that the linear rate of decline became more negative by twice the quadratic coefficient of 0.07 per year (i.e., steeper longitudinal decline later in the study, unconditional by baseline age or zygosity). (see text above for interpretation of heritability results)